

Unit 1

From the school book

Exercise 4 On scientific notation of the rational number

1 In each of the following, tick (✓) in front of the numbers which are in the standard form:

- | | | | | | |
|----------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| (1) 5.3×10^7 | <input type="checkbox"/> | (2) 0.2×10^{-4} | <input type="checkbox"/> | (3) 0.025×10^8 | <input type="checkbox"/> |
| (4) 20.5×10^5 | <input type="checkbox"/> | (5) 7×10^{-4} | <input type="checkbox"/> | (6) 10×10^{-10} | <input type="checkbox"/> |
| (7) 4.25×10 | <input type="checkbox"/> | (8) 33.9×10^6 | <input type="checkbox"/> | (9) -5.782×10^2 | <input type="checkbox"/> |
| (10) -0.0003×10^3 | <input type="checkbox"/> | | | | |

2 Write each of the following numbers in the standard form :

- | | | |
|-----------------|----------------|----------------|
| (1) 600 000 | (2) - 20 000 | (3) 7 millions |
| (4) 19 millions | (5) 46 870 000 | (6) 58 |

3 Write each of the following numbers in the standard form :

- | | | |
|------------|--------------|---------------|
| (1) 0.0006 | (2) 0.000053 | (3) 0.000864 |
| (4) 0.421 | (5) 25.0003 | (6) - 300.501 |

4 The number of inhabitants in Egypt is about 83 000 000 persons. Write this number in the standard form.

5 The area of the surface of the Earth is about 510 000 000 km². Express this number by the standard form.

6 The mass of the Hydrogen atom is about 0.000000000000000000000000167 gm. Write this number in the standard form.

7 The light velocity is about 300 000 km/s. Express this velocity by m/s. in the standard form.

8 Dr. Ahmed Zewail discovered the femto second which is a millionth of a miliardth of a second. Express it by the standard form.

9 At writing the number 2.74×10^{20} as a whole number, find the number of zeroes that are on the right of the digit 4

10 Write the following numbers in the standard form :

- | | | |
|---------------------------------|-----------------------------|-----------------------------|
| (1) 68×10^5 | (2) 68×10^{-5} | (3) 720×10^6 |
| (4) 750×10^{-9} | (5) -32.4×10^4 | (6) -702.5×10^{-8} |
| (7) 0.4×10^{-10} | (8) 0.0005×10^{15} | (9) 0.0036×10^{-4} |
| (10) 0.0020205×10^{12} | | |

11 Put the suitable sign (<) or (>) :

(1) 6.4×10^3 4.6×10^3

(2) 6.2×10^4 4.1×10^5

(3) 0.0041 3.2×10^{-2}

(4) 4370 3.41×10^4

(5) 2.10×10^{-5} 1.82×10^{-5}

(6) 9.1×10^{-4} 1.2×10^{-5}

(7) 6.920×10^5 96230

(8) 3.69×10^{-4} 0.0000623

12 Arrange the following numbers in a descending order :

3.6×10^{-3} , 5.2×10^{-5} , 1×10^{-2} , 8.35×10^{-2} , 6.08×10^{-8}

13 Choose the correct answer from those given :

(1) $3.04 \times 10^7 = \dots\dots\dots$

(a) 340 000

(b) 304 000

(c) 3 400 000

(d) 30 400 000

(2) $2.37 \times 10^{-4} = \dots\dots\dots$

(a) 0.00237

(b) 0.000237

(c) 23700

(d) 0.0000237

(3) If $0.00079 = 7.9 a$, then $a = \dots\dots\dots$

(a) 10^{-1}

(b) 10^{-3}

(c) 10^{-4}

(d) 10^4

(4) If $0.0000503 = m \times 10^{-5}$, then $m = \dots\dots\dots$

(a) 503

(b) 5.03

(c) 50.3

(d) 0.503

(5) If the thickness of a sheet of paper is 0.012 cm. , then a ream of 400 sheets is of height

(a) 48×10^{-3} cm.

(b) 48×10^{-2} cm.

(c) 4.8×10^0 cm.

(d) 48 cm.

(6) Which of the following equals $\frac{1}{2}$ milliard ?

(a) 50×10^8

(b) 5×10^8

(c) 0.5×10^8

(d) 500×10^7

(7) Which of the following is the greatest ?

(a) 6.3×10^5

(b) 9.8×10^4

(c) 5.2×10^5

(d) 7.3×10^4

(8) Which of the following is the smallest ?

(a) 0.6×10^5

(b) 0.25×10^5

(c) 7×10^4

(d) 17.5×10^4

(9) $6\ 000 \times 50 = \dots\dots\dots$

(a) 300×10^2

(b) 30×10^5

(c) 3×10^5

(d) 30×10^4

(10) $45 \times 900 = \dots\dots\dots$

(a) 4.05×10^2

(b) 4.05×10^3

(c) 4.05×10^4

(d) 45×10^2

(11) $0.7 \times 0.005 = \dots\dots\dots$

(a) 3.5×10^3

(b) 3.5×10^{-2}

(c) 3.5×10^2

(d) 3.5×10^{-3}

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14 Write the result of each of the following in the standard form :

(1) $(6.4 \times 10^8) \times (1.5 \times 10^5)$

(2) $(8.2 \times 10^7) \times (2.1 \times 10^{-4})$

(3) $(5.02 \times 10^{-4}) \times (0.1 \times 10^{-3})$

(4) $(4.4 \times 10^3) \times (2 \times 10^5)$

(5) $(3.8 \times 10^8) \div (1.9 \times 10^6)$

(6) $(125.5 \times 10^{-3}) \div (5 \times 10^4)$

(7) $(8.8 \times 10^{25}) \div (8.8 \times 10^{22})$

(8) $(5 \times 10)^4 \div (2.5 \times 10^{-3})$

15 Write the result of each of the following in the standard form :

(1) $(3.8 \times 10^5) + (4.6 \times 10^4)$

(2) $(4.54 \times 10^4) + (3.76 \times 10^3)$

(3) $(5.3 \times 10^8) - (0.8 \times 10^7)$

(4) $(2.65 \times 10^{-2}) - (6.34 \times 10^{-3})$

16 Write the result of each of the following in the standard form :

(1) 5000×3000

(2) 400×0.00007

(3) $8000 \div 0.004$

(4) $0.000033 \div 500$

(5) $(20\ 000)^3$

(6) $(0.002)^2$

(7) $(0.1)^{-8}$

17 Find the value of n in each of the following :

(1) $800\ 000 = 8 \times 10^n$

(2) $0.00000006 = 6 \times 10^n$

(3) $0.00052 = 5.2 \times 10^n$

(4) $0.000357 = 3.57 \times 10^n$

(5) $(0.004)^2 = 1.6 \times 10^n$

(6) $76293 = n \times 10^4$



Life Applications

18 If the diameter of the Earth equals 1.27×10^4 km. long and the length of the diameter of Mars is 6.79×10^3 km. Which of the two planets is the greater and what is the difference between the two diameter lengths in the standard form ?

19 If light travels at a speed of 3×10^8 m/s. :

(a) Calculate the distance from the Sun to the Earth if you know that the light of the Sun takes 8 minutes to reach the Earth.

(b) If the distance between planet Venus and the Sun is 108 million kilometres , calculate the elapsed time (in minutes) that light takes to reach Venus from the Sun.



For excellent pupils

20 Find the result of the following in the standard form : $\frac{9.02 \times 10^3 + 4.98 \times 10^4}{2.5 \times 10^{-5}}$

21 Without using the calculator , write each of the following numbers in the standard form :

(1) $10^{29} - 10^{28}$

(2) $2^{19} \times 5^{15}$

22 If $X = 5 + (3 \times 10) + (4 \times 10^2) + (6 \times 10^3) + (9 \times 10^4) + (4 \times 10^5) + (2 \times 10^6)$

Write X in the standard form without using the calculator.

Exercise 5 On order of mathematical operations

1 Calculate the value of each of the following :

(1) $3 + 12 \div 6$

(2) $-5 + 2 \times 3$

(3) $2 \times 6 - 4 \div 2$

(4) $4 \times 7 - 3^2$

(5) $4 \times 2^3 - 20$

(6) $9 + 4 \times 3^2$

(7) $144 - 8 \div 2^3$

2 Calculate the value of each of the following :

(1) $196 \div (7 - 5)^2$

(2) $18 \div (9 - 6) \times (1 + 2)$

(3) $20 \div 5 + 8 - (4 - 1)$

(4) $10 \times 4 - (2 \times 6 - 8)$

(5) $(7 - 4) \times 2 \div (5 - 3)$

(6) $(30 - 6) \div 6 \times 30 \div 3$

(7) $7(6^2 \div 2 \times 3)$

(8) $12(2^2) \div 24 + 3^2$

(9) $9(4)^2 \div 2^2 \times 3$

(10) $9 \times 10 + 20 \div 2 - 3$

(11) $6 + 9 \div 3 + 2 \times 3^2 + 11 - 8$

(12) $6 - 5 + 72 \div 9 + 24 \div 2^3 + 4 \times 1 + 10 \times 1 + 5$

3 Calculate the value of each of the following :

(1) $2 - [(7 - 3) - 2]$

(2) $[4 - (5 - 2)] - 1$

(3) $3 + [5 + 2(8 \div 4)]$

(4) $2^3 + [4 + (2 - 1)]$

(5) $[(2 + 23 - 7) \times 2] \div 4$

(6) $10 \times 3 \div [4 - (9 - 8)]$

(7) $(26 + 1) \div [3(4 - 3)]$

(8) $(15 \times 2) \div [5 - (9 - 7)]$

(9) $2 + 3[4 + (6 \times 3 - 8)] \times 2$

(10) $2[(5^2 + 1) - (4^2 - 1)]$

(11) $5[(2^2 - 1) - (2^2 - 2)]$

(12) $6 \div 3 + [7 + 20 \div (6 - 2^2)]$

4 Calculate the value of each of the following :

(1) $[-6 \div (-3)] \times [-30 \div (-3)]$

(2) $(-10 + 3) \div (-8 + 7)$

(3) $7 - [10 - (-8)] - 3$

(4) $[(11 - (-10)) \times 2] \div (-6)$

(5) $2 \div (-1) - (-4)^2$

(6) $-6 - [-2 - 5]^2$

5 Calculate the value of each of the following :

(1) $\frac{15 + 7}{15 - 4}$

(2) $\frac{8 + 20 - 4}{8 - 4}$

(3) $\frac{-4 \times (-10)}{-9 + 7}$

(4) $\frac{1 + 15}{8 - (2 - 2)}$

(5) $\frac{11 - (5 - 4)}{1 + 4}$

(6) $(3 - 1)^3 + \frac{7 \times 3}{-1 - 6} - \frac{2 \times 15}{6}$

(7) $\frac{5^2 - 5 \times 2}{(15 + 3) \div 6}$

(8) $\frac{5 + 2 \times 5}{2^2 + 1} + 5^2 - 5$

(9) $\frac{3^2 \times 6 \div 3}{2 \times 1 + (3 + 1)^2}$

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6 Calculate the value of each of the following :

$$(1) \left(\frac{3}{2} \times 3\frac{1}{2}\right) \div \left(\frac{6}{5} - 1\right)$$

$$(3) 16 + 4 \div 2 - 3 \times 10^{-2}$$

$$(2) 15 \div \frac{1}{3} - \frac{3}{4} \times 10^3 + 27$$

$$(4) 9 \div \frac{1}{2} \times 2 - 3 \div \frac{1}{5}$$

7 If $x = 3$, what is the numerical value of the expression : $2 \left(\frac{5x+3}{4x-3}\right)$ « 4 »

8 Evaluate the expressions when $t = 2$ and $s = 5$:

$$(1) (t + s)^2$$

$$(2) (s - t)^3$$

$$(3) \left(\frac{s}{t}\right)^3$$

$$(4) \frac{6^2}{s-1}$$

$$(5) \frac{s-t}{s^3}$$

$$(6) \frac{12}{4s^2}$$

9 Evaluate : $16t \div (4s) + 3st$, for $t = 9$ and $s = 6$ « 168 »

10 If $x = 4(5 + 6) - 6$ and $y = 9(36 \div 12) \div 3$,
find the value of the expression : $2x + 4y$ « 112 »

11 If $x = 3(5 + 7) - 4$ and $y = 4(8 + 2) \div 5$,
find the numerical value of the expression : $x - 4y$ « zero »

12 If $x = 18 - 4 \times 2 \div 2 + 1$ and $y = 8 + 9 \times 3 - 4^2 + 11$,
find the numerical value of the expression : $\left(\frac{y}{x}\right)^{-3}$ « $\frac{1}{8}$ »

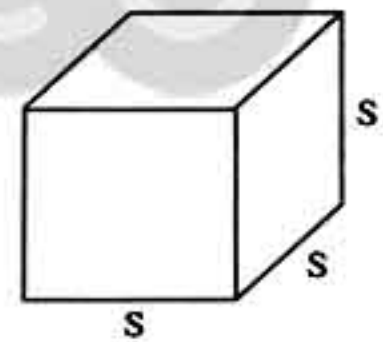
Geometric Applications

13 In the opposite figure :

The total area of a cube
is $T = 6s^2$, find T when :

$$(1) s = 3 \text{ m.}$$

$$(2) s = 0.8 \text{ cm.}$$



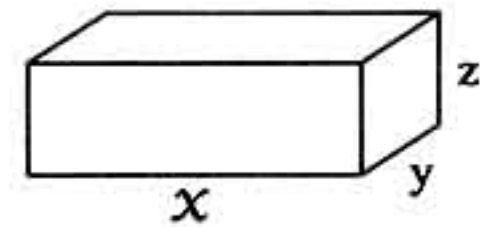
« 54 m.^2 , 3.84 cm.^2 »

14 In the opposite figure :

The total area of a cuboid
is $T = 2(xy + yz + zx)$ find T when :


$$(1) x = 2 \text{ cm.}, y = 3 \text{ cm. and } z = 5 \text{ cm.}$$

$$(2) x = \frac{3}{5} \text{ m.}, y = 0.4 \text{ m. and } z = \frac{1}{5} \text{ m.}$$



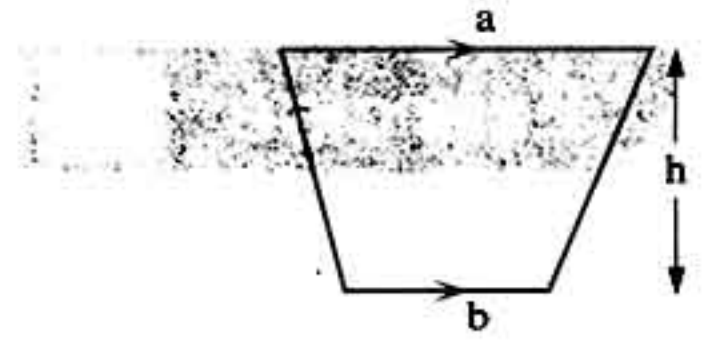
« 62 cm.^2 , $\frac{22}{25} \text{ m.}^2$ »

Lesson Five

15  In the opposite figure :

The area of a trapezium
is $A = \frac{1}{2} h (a + b)$, find A when :

- (1) $h = 2$ metres , $a = \frac{3}{4}$ metre and $b = \frac{1}{4}$ metre.
(2) $h = 4$ metres , $a = \frac{1}{2}$ metre and $b = \frac{1}{2}$ metre.



« 1 m.² , 2 m.² »



For excellent pupils

16 Rewrite each of the following mathematical statements after putting the parentheses in the places which make them true :

- (1) $3 + 96 \div 12 \times 4 = 5$
(2) $3 + 96 \div 12 \times 4 = 35$
(3) $3 + 96 \div 12 \times 4 = 33$

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Unit 1

From the school book

Exercise 6 On the square root of a perfect square rational number

1 Find each of the following :

① $\sqrt{16}$

② $-\sqrt{25}$

③ $\pm\sqrt{2500}$

④ $\pm\sqrt{40000}$

⑤ $\sqrt{\frac{9}{49}}$

⑥ $-\sqrt{\frac{64}{25}}$

⑦ $\sqrt{0.81}$

⑧ $\pm\sqrt{1.44}$

⑨ $\sqrt{6\frac{1}{4}}$

⑩ $-\sqrt{1\frac{11}{25}}$

⑪ $-\sqrt{4^2}$

⑫ $\pm\sqrt{8^2}$

⑬ $\sqrt{\left(\frac{81}{100}\right)^2}$

⑭ $\sqrt{\left(-\frac{3}{4}\right)^2}$

⑮ $\pm\sqrt{\frac{576}{1225}}$

⑯ $-\sqrt{\frac{2.5}{40}}$

⑰ $-\sqrt{\frac{49a^4}{25b^6}}$

⑱ $\pm\sqrt{\frac{16b^8}{121h^2}}$

⑲ $\sqrt{\frac{49a^4b^2}{9}}$

⑳ $\sqrt{\frac{25x^2y^2}{36}}$

2 Find the two square roots of each of the following numbers :

① 64

② 144

③ $\frac{9}{25}$

④ $6\frac{1}{4}$

⑤ 0.25

⑥ 0.0049

3 Find each of the following :

① $\sqrt{9} + \sqrt{16}$

② $\sqrt{36 + 64}$

③ $\sqrt{25 - 9}$

④ $-\sqrt{225 - 81}$

⑤ $\sqrt{3^2 + 4^2}$

⑥ $-\sqrt{(10)^2 - 8^2}$

⑦ $\sqrt{\frac{9}{16} + 1}$

⑧ $-\sqrt{\frac{1}{4} \left(1 - \frac{3}{4}\right)}$

⑨ $\sqrt{\frac{5^4 \times 5^3}{5^5}}$

⑩ $\sqrt{\left(\frac{1}{2}\right)^2 \div \left(\frac{1}{5}\right)^2}$

⑪ $\sqrt{\left(\frac{1}{2}\right)^4 \times \left(\frac{1}{3}\right)^4}$

⑫ $\sqrt{\left(\frac{1}{4}\right)^2 \times \left(\frac{1}{4}\right)^3}$

4 Complete the following :


① $\frac{3}{4} \times \sqrt{\frac{16}{9}} = \dots\dots\dots$

② $\sqrt{\frac{81}{49}} \times \frac{14}{27} = \dots\dots\dots$


③ $\sqrt{\frac{9}{4}} - \frac{3}{2} + \left(\frac{3}{2}\right)^{\text{zero}} = \dots\dots\dots$

④ $\sqrt{36} + \sqrt{16} = \sqrt{\dots\dots\dots}$

⑤ $\sqrt{(81)^2 - 81 \times 2 + 1} = \dots\dots\dots$

- (6) The multiplicative inverse of $\sqrt{\frac{4}{25}}$ in the simplest form equals
- (7) The multiplicative inverse of $\sqrt{0.49}$ in the simplest form equals
- (8)  The multiplicative inverse of the rational number $\sqrt{\frac{10}{2.5}}$ equals
- (9) The additive inverse of the number $-\sqrt{\frac{9}{16}}$ in the simplest form equals
- (10) The rational number $6\frac{1}{4}$ in the form $(\frac{a}{b})^2$ is
- (11) $\sqrt{\frac{25}{64}} = \sqrt{(\frac{\dots\dots\dots}{\dots\dots\dots})^2} = \dots\dots\dots$ (12) $\sqrt{(-3)^2} = \dots\dots\dots$
- (13) $\sqrt{a^4b^8} = \dots\dots\dots$
- (14) If $a = \sqrt{\frac{1}{4}}$ and $b = 2$, then $ab = \dots\dots\dots$
- (15) If $a = -\frac{1}{2}$ and $b = -\frac{9}{8}$, then $\sqrt{ab} = \dots\dots\dots$ (16) If $2x = \sqrt{36}$, then $x = \dots\dots\dots$
- (17) If $a = 0.000625$, then $\sqrt{a} = 2.5 \times 10^{\dots\dots\dots}$
- (18) $\sqrt{(2009)^2 + 2(2009) \times 213 + (213)^2} = \dots\dots\dots$

5 Choose the correct answer from those given :

- (1) $\sqrt{1\frac{9}{16}} = \dots\dots\dots$
 (a) $1\frac{3}{4}$ (b) $-1\frac{3}{4}$ (c) $1\frac{1}{4}$ (d) $-1\frac{1}{4}$
- (2)  $\sqrt{10^2 - 6^2} = \dots\dots\dots$
 (a) 4 (b) 8 (c) ± 4 (d) ± 8
- (3) $\sqrt{18 \times 10 \times 10 \times 18} = \dots\dots\dots$
 (a) 18 (b) 180 (c) 10 (d) 100
- (4) $\sqrt{\sqrt{81}} = \dots\dots\dots$
 (a) 81 (b) 27 (c) 9 (d) 3
- (5) $\sqrt{2^2 + \sqrt{25}} = \dots\dots\dots$
 (a) 3 (b) -3 (c) 9 (d) -9
- (6) If : $\frac{x}{2} = \frac{8}{x}$, then $x = \dots\dots\dots$
 (a) 4 (b) -4 (c) ± 4 (d) 16

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(7) If : $x = \sqrt{\frac{1}{4}}$, then $x^3 = \dots\dots\dots$

- (a) $\frac{3}{8}$ (b) $\frac{1}{8}$ (c) $\frac{1}{16}$ (d) $\frac{1}{64}$

(8) $\sqrt{(a+b)^3(a+b)} = \dots\dots\dots$

- (a) $(a+b)^2$ (b) $a^4 + b^4$ (c) $-(a+b)^2$ (d) $\pm (a+b)^2$

(9) $\sqrt{1} + \sqrt{4} + \sqrt{9} + \sqrt{16} + \sqrt{25} + \sqrt{36} + \sqrt{49} + \sqrt{64} = \dots\dots\dots$

- (a) 6 (b) $\sqrt{204}$ (c) $\sqrt{81}$ (d) 6^2

(10) The side length of the square whose area is $16x^2 \text{ cm.}^2 = \dots\dots\dots \text{ cm.}$

- (a) $8x$ (b) $4x$ (c) $2x$ (d) $8x^2$

6 Simplify each of the following to the simplest form :

(1) $(-\frac{1}{2})^3 \times \sqrt{\frac{64}{9}}$

(2) $\sqrt{\frac{49}{4}} \times (\frac{2}{7})^{\text{zero}} \times (-\frac{2}{7})^2$

(3) $\frac{2}{5} \times \sqrt{\frac{9}{16}} \div (-\frac{1}{2})^3$

(4) $(-\frac{1}{3})^2 + \sqrt{\frac{64}{81}} - (\frac{3}{4})^{\text{zero}}$

(5) $\frac{3}{4} \times (-\frac{2}{3})^3 \times (\frac{3}{\sqrt{4}})^2$

(6) $\sqrt{(\frac{25}{4})^2} \times (\frac{2}{5})^2$

7 Simplify each of the following to the simplest form :

(1) $\sqrt{16} + \sqrt{25}$

(2) $\sqrt{\sqrt{16} + \sqrt{25}}$

(3) $\sqrt{(\sqrt{16} + \sqrt{25})^2}$

8 Find two rational numbers lying between : $\sqrt{\frac{4}{9}}$ and $\frac{3}{4}$

9 Which is greater : $\frac{3}{5}$ or $\sqrt{\frac{4}{9}}$? Find the difference between them.

10 Which is smaller : $\sqrt{2\frac{1}{4}}$ or $(-\frac{2}{3})^2$? Find their difference.

11 Find each of the following :

(1) $\sqrt{5^2 - 2 \times 5 + 1}$

(2) $\sqrt{(\frac{1}{4})^2 - 2 \times \frac{1}{4} + 1}$






(3) $\sqrt{20 \div 5 + 8 - (4 - 1)}$

(4) $\sqrt{8 \times (5 + 11) \div (2 + 6)}$

(5) $\sqrt{2 \times 8 + 10 - 3 + 12 + 11 \times 6 + 88 \div 2^3 + 99 \div 11}$


(6) $\sqrt{6 + 3\sqrt{100} - \sqrt{121}}$

Geometric Applications

- 12 (1)  \overline{XY} is a line segment where $(XY)^2 = 25 \text{ cm}^2$, E is the midpoint of \overline{XY}
Find the length of : \overline{XE} « 2.5 cm. »
- (2)  If : $(AB)^2 = 144 \text{ cm}^2$, $(BC)^2 = 625 \text{ cm}^2$ and $B \in \overline{AC}$
Find the length of : \overline{AC} « 37 cm. »
- (3) The area of a square is 0.49 cm^2 . Find its perimeter. « 2.8 cm. »
- (4)  The area of a square is equal to the area of a triangle with base = 9 cm. long
and its height = 8 cm. find the side length of the square. « 6 cm. »
- (5) The area of a circle 154 cm^2 . Calculate its radius length ($\pi = \frac{22}{7}$) « 7 cm. »
- (6) The area of a circle 78.5 cm^2 . Calculate its diameter length ($\pi = 3.14$) « 10 cm. »
- (7) The area of a circle 616 cm^2 . Calculate its circumference ($\pi = \frac{22}{7}$) « 88 cm. »
- (8)  If three quarters of the area of a square is $1\frac{11}{64} \text{ m}^2$.
Calculate the side length of the square. « $1\frac{1}{4} \text{ m}$. »
- (9)  The length of a rectangle is twice its width and its area is 24.5 cm^2 .
Calculate each of its width and length. « 3.5 cm. , 7 cm. »



For excellent pupils

- 13  If $\frac{m}{n}$ is a rational number and $\frac{m^2}{n^2} = 0.16$, find the value of $(\frac{m}{n})^3$ « ± 0.064 »

Unit 1

From the school book

Exercise 7 On solving equations of the first degree in one unknown in \mathbb{Q}

1 Find the solution set of each of the following equations :

(1) $x - 7 = 3$ where $x \in \mathbb{N}$

(3) $5x = 20$ where $x \in \mathbb{Q}$

(5) $-4 + y = 13$ where $y \in \mathbb{N}$

(7) $x - 7 = 0$ where $x \in \mathbb{Z}$

(9) $x - 6\frac{1}{4} = 12\frac{1}{2}$ where $x \in \mathbb{Q}$

(2) $x + 17 = 13$ where $x \in \mathbb{N}$

(4) $\frac{2}{5}x = \frac{1}{5}$ where $x \in \mathbb{Q}$

(6) $m - (-3) = 1$ where $m \in \mathbb{Z}$

(8) $y - (-5) = -3$ where $y \in \mathbb{Q}$

(10) $8.91 + x = 11.09$ where $x \in \mathbb{Q}$

2 Solve each of the following equations :

(1) $2x - 1 = 5$ where $x \in \mathbb{Q}$

(3) $3x - 13 = 26$ where $x \in \mathbb{N}$

(5) $8 + 2x = 14$ where $x \in \mathbb{Z}$

(7) $8 - 2x = -2$ where $x \in \mathbb{Z}$

(9) $2x + 3x + 25 = 5$ where $x \in \mathbb{Z}$

(2) $8x + 4 = 12$ where $x \in \mathbb{Q}$

(4) $2x + 14 = 14$ where $x \in \mathbb{N}$

(6) $\frac{5}{6}x - 4 = 11$ where $x \in \mathbb{Q}$

(8) $2 - 5x = 0$ where $x \in \mathbb{Q}$

(10) $6x - 2x + 7 = 4$ where $x \in \mathbb{Z}$

3 Solve each of the following equations in \mathbb{Q} :

(1) $2(x - 3) = 4$

(3) $7(x - 2) - 3(x + 1) = 3$

(5) $4(x - 1) - (x + 3) = 0$

(7) $2(x - 3) + 3(x - 2) - 4x = -3$

(2) $3x + 2(5x - 3) = 7$

(4) $3(x + 2) + 7(x - 1) = 12$

(6) $5(x - 2) + 2(x + 4) = -16$

(8) $3y + 6(y + 3) - (8y - 16) = 60$

4 Find in \mathbb{Q} the solution set of each of the following equations :

(1) $2x + 5 = x + 9$

(3) $x + 3 = 18 - 3x$

(5) $4(x + 1) = 2(x - 1)$

(7) $a + 5a - 2 = 2(3 - a)$

(9) $\frac{x+1}{3} = \frac{x-1}{4}$

(2) $5x - 4 = 2x + 11$

(4) $3x + 6 = 30 - 5x$

(6) $3(x - 2) = 5x - 10$

(8) $3(2x - 8) - (2x + 2) = x - 3$

(10) $\frac{5}{4+4x} = \frac{3}{1-2x}$

5 Complete the following :

(1) If $x + 5 = 7$, then $x = \dots\dots\dots$

(2) If $3t = 6$, then the value of $6t = \dots\dots\dots$

(3) If $2x = 5$, then the value of $4x = \dots\dots\dots$

(4) If $x + 9 = 11$, then the value of $7x = \dots\dots\dots$

- (5) If $2t + 3 = 15$, then the value of $\frac{1}{3}t = \dots\dots\dots$
- (6) If $Z - 1\frac{1}{4} = 5\frac{1}{2}$, then the value of $4Z - 18 = \dots\dots\dots$
- (7) If $\frac{P}{4} = \frac{2}{3}$, then the value of $\frac{P}{2} = \dots\dots\dots$
- (8) If the age of a man now is X years, then his age 5 years ago is $\dots\dots\dots$
- (9) If the age of a man now is y years, then his age after 4 years is $\dots\dots\dots$
- (10) If the age of a man after 5 years is X years, then his age now is $\dots\dots\dots$
- (11) If the age of Youssef after 4 years is X years, then his age 2 years ago is $\dots\dots\dots$
- (12) A rectangle with length equals triple its width. if the length = X cm.
then its width = $\dots\dots\dots$ cm.
- (13) The rectangle whose width = X cm. and its length is twice its width, then its perimeter = $\dots\dots\dots$ cm.
- (14) Two integers, their sum is 5, if one of them is X , then the other one is $\dots\dots\dots$
- (15) Two integers, the difference between them is 2, if the small one is X , then the great one is $\dots\dots\dots$

6 Choose the correct answer from those given :

- (1) If $2X = 2$, then $3X - 1 = \dots\dots\dots$
(a) 2 (b) 3 (c) 4 (d) 5
- (2) If $2X = 0$, then $X = \dots\dots\dots$
(a) 2 (b) 3 (c) 5 (d) zero
- (3) If $2ab = 10$, then $3ab = \dots\dots\dots$
(a) 5 (b) 6 (c) 15 (d) 30
- (4) If $0.2 + a = 5$, then $\frac{a}{4} = \dots\dots\dots$
(a) 4.8 (b) 1.3 (c) 1.2 (d) 19.2
- (5) If $5X + 8X + 2X + 4X = 114$, then $5X + 3 = \dots\dots\dots$
(a) 33 (b) 35 (c) 47 (d) $8X$
- (6) The S.S. of the equation $\frac{2a}{3} = 8 + 4a$ in \mathbb{Q} is $\dots\dots\dots$
(a) $\{-2.4\}$ (b) $\{2.4\}$ (c) $\{-3\frac{1}{3}\}$ (d) $\{0\}$
- (7) Which of the following equations is equivalent to the equation $X + 3 = 12$?
(a) $X - 3 = -12$ (b) $X + (-3) = 12$
(c) $X - (-3) = 12$ (d) $X - (-3) = -12$
- (8) Which of the following equations is equivalent to the equation $X - 12 = 15$?
(a) $X + 12 = -15$ (b) $\frac{1}{3}X - 4 = 5$ (c) $X - 4 = -5$ (d) $X + 4 = 5$

Unit 1

Geometric Applications

- 7 Find the measure of each angle in each of the following triangles :

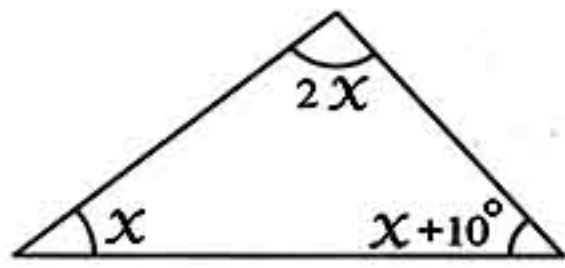


Fig. (1)

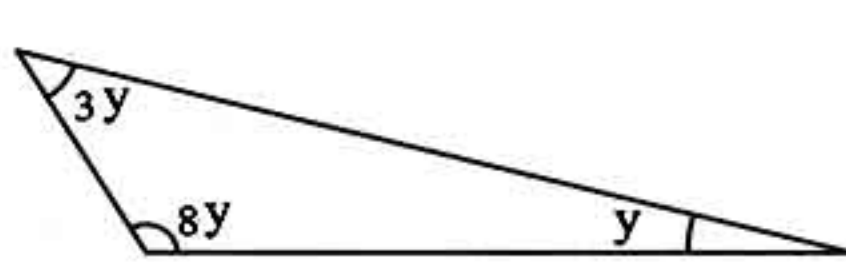


Fig. (2)

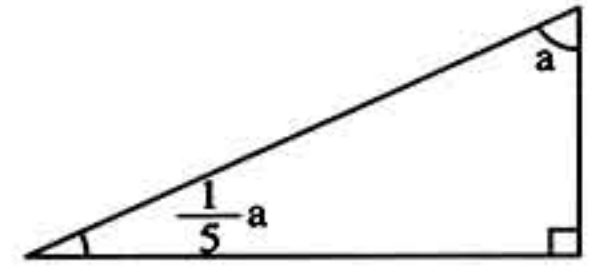
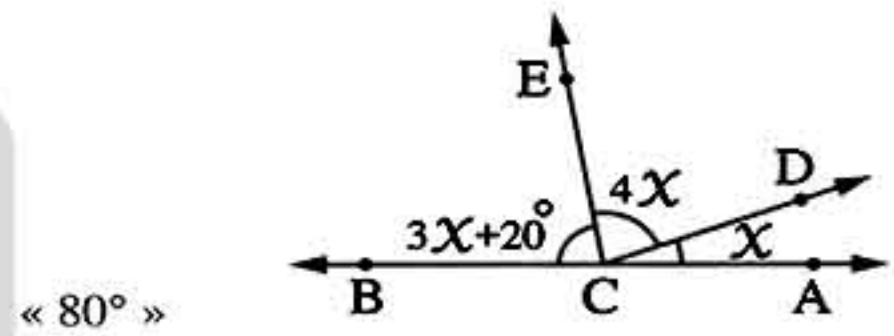


Fig. (3)

- 8 In the opposite figure :

If $C \in \overleftrightarrow{AB}$, find $m(\angle DCE)$



- 9 The length of a rectangle exceeds its width by 4 metres and its perimeter is 68 metres. Find the dimensions of the rectangle. « 19 m. , 15 m. »


- 10 The length of a rectangle decreases than the twice of its width by 4 cm., if its perimeter equals the perimeter of a square of side length 7 cm. Find the dimensions of the rectangle. « 6 cm. , 8 cm. »

- 11 The length of a rectangle is twice its width. If the length decreases 5 cm. and the width increases 6 cm. , then the rectangle becomes a square. Find the area of the rectangle. « 242 cm² »



Life Applications

- 12 Two integers , the smaller number is $2x$ and the greater number is $7x$, if the difference between them is 25 , find the two integers. « 10 , 35 »
- 13 Two natural numbers , one of them is twice the other and their sum is 108 Find the two numbers. « 36 , 72 »
- 14 The difference between two natural numbers is 5 and their sum is 21 What are the two numbers ? « 13 , 8 »
- 15 Find the number that if it is added to its triple the result is 32 « 8 »

- 16 Find the number which if we subtract 9 from its triple , the result will be 6 « 5 »
- 17 Three consecutive natural numbers whose sum is 213
What are these numbers ? « 70 , 71 , 72 »
- 18 Find three consecutive odd numbers if their sum is 357 « 117 , 119 , 121 »
- 19  A man's age now is three times his son's age and after two years , the sum of their ages will be 52 years. What is the age of each now ? « 12 years , 36 years »
- 20 Three brothers , Amgad , Bassim and Ayman , the sum of their ages is 89 years.
If Amgad was born before Bassim by 2 years and Bassim was born before Ayman by 6 years , what is the age of each of them now ? « 25 years , 31 years , 33 years »



For excellent pupils

- 21 Find in \mathbb{Q} the S.S. of each of the following equations :
- (1) $5 - \frac{6}{x} = -1$ (2) $-\frac{3}{5} + \frac{x}{10} = -\frac{1}{5} - \frac{x}{5}$
- 22 Find in \mathbb{Q} the S.S. of each of the following equations :
- (1) $(x + 3)^2 - (x - 2)^2 = 15$ (2) $(2x + 3)(2x - 1) - (2x - 1)^2 = 14$
- 23 If the S.S. of the equation $12x + 3 = 39$ in \mathbb{Q} equals the S.S. of the equation $a x - 12 = a$ in \mathbb{Q} , find the value of a « 6 »
- 24 If $a + 1$ is a solution of the equation $(x + a)(x - a) = x^2 - a x + 3$ in \mathbb{Q} ,
find the value of a « 3 »
- 25 Three brothers were born in 1980 , 1984 and 1986 , the required is finding the year in
which the sum of their ages became 41 years. « 1997 »

Unit 1

From the school book

Exercise 8 On solving inequalities in \mathbb{Q}

1 Which number would you add to each side of the inequality to obtain x in one side of it ?

- | | | | |
|------------------------|------------------------|---------------------------------------|--------------------------------------|
| (1) $x + 5 > 9$ | (2) $x - 4 < 6$ | (3) $x - 7 < 3$ | (4) $x + 9 > 12$ |
| (5) $x - 1.5 \leq 3.2$ | (6) $4.8 \leq x + 0.6$ | (7) $1\frac{1}{2} > x - 2\frac{1}{2}$ | (8) $x + \frac{1}{3} > -\frac{1}{6}$ |

2 Find the solution set of the inequality $x + 3 \leq 6$, where :

- (1) $x \in \mathbb{Z}$ (2) $x \in \mathbb{N}$

then represent the solution set on the number line.

3 Find the solution set of the following inequalities in \mathbb{Q} :

- | | | |
|-------------------|---------------------------|--|
| (1) $x + 2 > 5$ | (2) $x + 4 > 1$ | (3) $y - 5 > 7$ |
| (4) $19 < y + 14$ | (5) $-1 \geq x - 3$ | (6) $-5\frac{1}{2} > a + 1\frac{1}{4}$ |
| (7) $-2x < 12$ | (8) $\frac{2}{3}x \geq 1$ | (9) $-\frac{1}{4}x \leq \frac{1}{4}$ |

4 Solve each of the following inequalities in \mathbb{Q} :

- | | | |
|----------------------------|-----------------------------|---|
| (1) $3x - 2 < 1$ | (2) $2x + 3 < 9$ | (3) $4x + 2 \geq -10$ |
| (4) $3x - 2 \geq 5$ | (5) $3x - 9 < 0$ | (6) $1 + 2x \leq -3$ |
| (7) $9 - 6x < 15$ | (8) $2 - 3x \leq 4$ | (9) $\frac{3x - 2}{5} \geq \frac{1}{2}$ |
| (10) $8x - 3x + 1 \leq 29$ | (11) $4n - 2(n - 1) \geq 0$ | (12) $-3m + 6(m - 4) > 9$ |

5 Solve each of the following inequalities in \mathbb{Q} :

- | | |
|--|-------------------------------------|
| (1) $6d + 1 \leq 5d - 3$ | (2) $6x + 2 \geq 14 + 5x$ |
| (3) $3x - 2 < 5x - 8$ | (4) $8 - 2x \leq 5x$ |
| (5) $5x + 1 \geq 2(x + 2)$ | (6) $3(x + 2) < -x + 4$ |
| (7) $3(x + 2) \geq -2(x + 1)$ | (8) $2 - 3(x - 5) \geq x + 7$ |
| (9) $3(7y - \frac{1}{3}) \leq 20y - 1$ | (10) $\frac{x}{2} + 3 \leq 2x + 1$ |
| (11) $4 - 5(x - 2) \leq -2(-9 + 2x)$ | (12) $3(y + 2) + 8 < 10 - (2 - y)$ |
| (13) $1 - (4d - 1) > 2(d - 3)$ | (14) $x - 3(2x + 1) < 5(1 + x) + 2$ |

6 Find the S.S. of each of the following inequalities :

- | | |
|---|--|
| (1) $9 \leq 4x + 1 \leq 17, x \in \mathbb{Z}$ | (2) $9 \leq 3x + 2 < 12, x \in \mathbb{Q}$ |
| (3) $9 > x + 6 > 2, x \in \mathbb{N}$ | |

7 Complete :

- (1) If $x > y$, then $x + z \dots y + z$ (2) If $x < y$, then $x + z \dots y + z$
 (3) If $x < y$ and $y < z$, then $x < \dots$ (4) If $z > y$ and $y > x$, then $z > \dots$
 (5) If $a - 3 < 0$, then $\dots > \dots$ (6) If $a + 5 > 0$, then $\dots > \dots$
 (7) If $b < 0$, then $b + 3 \dots 3$
 (8) If $x > y$ and z is positive ($z > 0$), then $xz \dots yz$
 (9) If $x < y$ and z is negative ($z < 0$), then $xz \dots yz$

8 Choose the correct answer from those given :

- (1) If $-x < 5$, then
 (a) $x > 5$ (b) $x > -5$ (c) $x < 5$ (d) $x < -5$
 (2) If $x \in \mathbb{N}$, then the S.S. of the inequality $-x > 3$ is
 (a) $\{4, 5, \dots\}$ (b) $\{-4, -5, \dots\}$ (c) $\{-3\}$ (d) \emptyset
 (3) $\frac{x}{3} < 4$ is equal to
 (a) $x > \frac{4}{3}$ (b) $x < \frac{4}{3}$ (c) $x > 12$ (d) $x < 12$
 (4) If $x \in \mathbb{Z}$, then the S.S. of the inequality $20 < 5x < 25$ is
 (a) $\{4\}$ (b) $\{5\}$ (c) $\{4, 5\}$ (d) \emptyset
 (5) The S.S. of the inequality $-2x < \text{zero}$ in \mathbb{Q} is
 (a) \emptyset (b) \mathbb{Q}_+ (c) \mathbb{Q}_- (d) \mathbb{Z}_+
 (6) The number of solutions of the inequality $\frac{1}{5} < x < \frac{2}{3}$, where $x \in \mathbb{Q}$ is
 (a) zero (b) 1 (c) 2 (d) an infinite number.
 (7) If $x > y$, then $\frac{1}{x} \dots \frac{1}{y}$, where $x \neq 0, y \neq 0$
 (a) $>$ (b) $<$ (c) $=$ (d) \geq
 (8) The number 2 belongs to the S.S. of the inequality where x is an integer.
 (a) $x > 2$ (b) $x < 2$ (c) $-x > -3$ (d) $-x > 3$
 (9) If $x > 5$, then $-x \dots$
 (a) < -9 (b) ≥ -5 (c) < -5 (d) > -5

9 Show by using examples that if $a > b$ and $c > d$, then it is not always correct that $a - c > b - d$ 10 Put (\checkmark) for the correct statement and (\times) for the incorrect statement, when a statement is false, give an example that shows why it is false (given that $x > y$):

- (1) $y < x$ () (2) $x > 0$ () (3) $y^2 \geq 0$ () (4) $y^2 > y$ ()
 (5) $xy > 0$ () (6) $x + y > y$ () (7) $y^2 > x$ () (8) $y^2 < xy$ ()
 (9) $xy < x^2$ () (10) $x^3 < y^2$ ()

Unit 1



Life Application

- 11 Hany wants to buy a pair of shoes and some shirts , if Hany has L.E. 200 , the price of the pair of shoes is L.E. 70 and the price of one shirt is L.E. 40

What is the greatest number of shirts can Hany buy ?

« 3 »



For excellent pupils

- 12 If the S.S. of the inequality $a \leq 3x - 5 \leq b$ in \mathbb{Q} is $\{x : x \in \mathbb{Q}, 2 \leq x \leq 5\}$, find the values of a and b

« 1 , 10 »

- 13 If : $-4 \leq x \leq 5$ and $2 \leq y \leq 7$, where $x \in \mathbb{Q}$ and $y \in \mathbb{Q}$, find :

(1) The greatest possible value of the expression $x + y$

« 12 »

(2) The greatest possible value of the expression $y - x$

« 11 »

(3) The smallest possible value of the expression xy

« -28 »

(4) The smallest possible value of the expression $x^2 + y^2$

« 0 »

Rania Sayed



Worksheet 4 till lesson 4 unit 1

Answer the following questions :

1 Choose the correct answer from those given :

(1) The additive inverse of the number 3^{-1} is

- (a) $\frac{1}{3}$ (b) $-\frac{1}{3}$ (c) 3 (d) -3

(2) $(2a)^3 = \dots\dots\dots$

- (a) $2a^3$ (b) $8a$ (c) $8a^3$ (d) $32a$

(3) Which of the following = $\frac{1}{4}$ million ?

- (a) 25×10^5 (b) 0.25×10^5 (c) 0.25×10^6 (d) 0.25×10^7

(4) $(\frac{2}{5})^{-1} \div \frac{5}{2} = \dots\dots\dots$

- (a) 1 (b) $\frac{5}{2}$ (c) $\frac{25}{4}$ (d) $\frac{4}{25}$

(5) $2.37 \times 10^{-4} = \dots\dots\dots$

- (a) 0.00237 (b) 0.000237 (c) 23700 (d) 0.0000237

(6) $3y^{-1} = \dots\dots\dots$, $y \neq 0$

- (a) $\frac{1}{3}y$ (b) $\frac{3}{y}$ (c) y^{-3} (d) y^3

2 Write each of the following numbers on its standard form (scientific form) :

(1) -2540000 (2) 0.000046

(3) 0.7×10^{-7} (4) 0.0435×10^9

3 [a] If $a = -\frac{1}{2}$, $b = 2$, $c = \frac{3}{2}$, find the numerical value of the expression : $a^2 b^3 + (a + c)^5$

[b] Calculate the value of each of the following :

(1) $\frac{(3^{-2})^4}{3^{-5} \times 3^{-2}}$

(2) $(3^{\text{zero}} \times 2^{-2})^{-2}$

(3) $\frac{(-3)^7 \times (-3)^{-2}}{(-3)^5}$

4 Write the result of each of the following on the standard form :

(1) $(5.8 \times 10^7) + (3.2 \times 10^5)$ (2) $(65.5 \times 10^{-2}) \div (5 \times 10^2)$

(3) 60000×5000



The answer of worksheet

4



Total mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | |
|-------|---|---|---|
| (1) a | b | c | d |
| (2) a | b | c | d |
| (3) a | b | c | d |
| (4) a | b | c | d |
| (5) a | b | c | d |
| (6) a | b | c | d |



- 2 (1)
- (2)
- (3)
- (4)



- 3 [a]
-



- [b] (1)
- (2)
- (3)

- 4 (1)
- (2)
- (3)





Worksheet 5 till lesson 5 unit 1

Answer the following questions :

1 Choose the correct answer from those given :

(1) If $0.000237 = 2.37 \times 10^n$, then $n = \dots\dots\dots$

- (a) 4 (b) 2 (c) -4 (d) -2

(2) $(x^{-2})^3 = \dots\dots\dots$, $x \neq 0$

- (a) x^{-6} (b) x^{-5} (c) x (d) x^6

(3) $-11 + 3 \times 7 = \dots\dots\dots$

- (a) 11 (b) 10 (c) -56 (d) -1

(4) $3^2 + 3^2 + 3^2 = \dots\dots\dots$

- (a) 3^3 (b) 3^8 (c) 1^2 (d) 3^6

(5) The number $1\frac{9}{16} = (\dots\dots\dots)^2$

- (a) $1\frac{3}{4}$ (b) $\frac{4}{5}$ (c) $\frac{3}{4}$ (d) $\frac{5}{4}$

(6) Twice the number $2^{18} = \dots\dots\dots$

- (a) 2^9 (b) 2^{36} (c) 2^{10} (d) 2^{19}

2 Calculate the value of each of the following :

(1) $8 \times 2^2 - 7 \times (4 + 1)$

(2) $2((5^2 + 1) - (4^2 - 1))$

(3) $\frac{5 + 2 \times 5}{2^2 + 1} + 5^2 - 5$

(4) $16 \div \frac{1}{4} - \frac{3}{4} \times 10^2 + 25$

3 [a] Find the result in the standard form : $(4.4 \times 10^3) \times (2 \times 10^5)$

[b] Find the value of : $\frac{7^{-2} \times 7^5}{7^3}$

4 [a] If $x = -\frac{1}{2}$, $y = \frac{3}{4}$, find the numerical value of : $x^3 y^2$

[b] If $x = 5$, find the value of the expression : $2\left(\frac{3x+6}{4x-13}\right)$

Worksheets on Algebra & Statistics



The answer of worksheet

5

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| ① | a | b | c | d |
| ② | a | b | c | d |
| ③ | a | b | c | d |
| ④ | a | b | c | d |
| ⑤ | a | b | c | d |
| ⑥ | a | b | c | d |



- 2
- ①
- ②
- ③
- ④



- 3
- [a]
- [b]



- 4
- [a]
- [b]





Worksheet 6 till lesson 6 unit 1

Answer the following questions :

1 Choose the correct answer from those given :

(1) $\sqrt{(-7)^2} = \dots\dots\dots$

- (a) 49 (b) 7 (c) -7 (d) ± 7

(2) $\sqrt{10^2 - 8^2} = \dots\dots\dots$

- (a) 2 (b) 6 (c) ± 2 (d) ± 6

(3) $4 + 2 \times 3 = \dots\dots\dots$

- (a) 18 (b) 10 (c) 14 (d) 24

(4) The multiplicative inverse of the number 3^{-2} is $\dots\dots\dots$

- (a) $\frac{1}{3}$ (b) 9 (c) $\frac{1}{9}$ (d) 3

(5) If the thickness of a piece of paper = 0.012 cm. , then which of the following is the height of a ream of 600 pieces of paper ?

- (a) (72×10^{-3}) cm. (b) (72×10^{-2}) cm.
(c) 72 cm. (d) $(7.2 \times 10^{\text{zero}})$ cm.

(6) $\sqrt{\sqrt{16}} = \dots\dots\dots$

- (a) 16 (b) 8 (c) 4 (d) 2

2 Complete the following :

(1) $\frac{5^{-2} \times 5^3}{5^4} = 5^{\dots\dots\dots}$

(2) $-\sqrt{9+16} = -3 + \dots\dots\dots$

(3) $(4 \frac{1}{2})^3 \div (2 \frac{1}{4})^3 = \dots\dots\dots$

(4) A square is of side length $\frac{2x}{3}$ length unit , then its area is $\dots\dots\dots$ square unit.

(5) If $x = \frac{1}{2}$, $y = \frac{1}{4}$, then $(x - y)^{-1} = \dots\dots\dots$

(6) $2^5 \times \dots\dots\dots = 2^{10}$

3 [a] A circle whose area is 154 cm^2 . Find the length of its radius

[b] Reduce to the simplest form : $(-\frac{1}{2})^3 \times \sqrt{\frac{25}{9}} \times \sqrt{(\frac{8}{5})^2} \times 3^{-1}$

4 [a] If $a = \frac{1}{3}$, $b = -\frac{2}{3}$, find the value of : $|(a^3 \div b^3)^{-1}|$

[b] Calculate the value of : $5((2^2 - 1) - (2^2 - 2))$



The answer of worksheet

6

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| ① | a | b | c | d |
| ② | a | b | c | d |
| ③ | a | b | c | d |
| ④ | a | b | c | d |
| ⑤ | a | b | c | d |
| ⑥ | a | b | c | d |

3

- 2
- ①
- ②
- ③
- ④
- ⑤
- ⑥

3

- 3 [a]
-
- [b]
-

4

- 3 [a]
-
- [b]
-

5



Worksheet 7 till lesson 7 unit 1

Answer the following questions :

1 Choose the correct answer from those given :

① $\sqrt{10^2 - 6^2} = \dots\dots\dots$

- (a) 4 (b) 8 (c) ± 4 (d) ± 8

② The number 0.0000014 = $\dots\dots\dots$

- (a) 1.4×10^{-5} (b) 1.4×10^5 (c) 1.4×10^{-6} (d) 1.4×10^6

③ $\frac{9}{x^{-2}} \times \frac{x^{-4}}{3} = \dots\dots\dots$

- (a) $3x^{-6}$ (b) $\frac{3}{x^2}$ (c) $\frac{3}{x^6}$ (d) $\frac{3}{x^8}$

④ The S.S. of the equation : $2x = -6$ in \mathbb{Z} is $\dots\dots\dots$

- (a) $\{-3\}$ (b) \emptyset (c) $\{-6\}$ (d) $\{0\}$

⑤ $(a^3)^4 = \dots\dots\dots$

- (a) a^{43} (b) a^7 (c) a^{-1} (d) a^{12}

⑥ If : $3y = 6$, then $6y = \dots\dots\dots$

- (a) 2 (b) 3 (c) 6 (d) 12

2 Complete the following :

① $\sqrt{36} + \sqrt{16} = \sqrt{\dots\dots\dots}$

② If the middle number of three consecutive natural numbers is x , then the sum of these three numbers in the simplest form = $\dots\dots\dots$

③ $(2b^{-1})^{-1} = \dots\dots\dots$

④ $2 \times 6 - 4 \div 2$

3 [a] Two natural numbers , the difference between them is 5 and their sum is 15 find the two numbers.

[b] Reduce to the simplest form : $\sqrt{\frac{49x^2y^2}{25}}$

4 [a] Find the S.S. of the following equation in \mathbb{Q} : $3(2x - 1) = 15$

[b] Find the value of : $(-\frac{1}{3})^2 + \sqrt{\frac{64}{81}} - (\frac{3}{7})^{\text{zero}}$

Worksheets on Algebra & Statistics



The answer of worksheet

7

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| ① | a | b | c | d |
| ② | a | b | c | d |
| ③ | a | b | c | d |
| ④ | a | b | c | d |
| ⑤ | a | b | c | d |
| ⑥ | a | b | c | d |



2 ①

②

③

④



3 [a]

.....

[b]

.....



4 [a]

.....

[b]

.....



Worksheets on Algebra & Statistics



The answer of worksheet 8



Total mark

15



1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| ① | a | b | c | d |
| ② | a | b | c | d |
| ③ | a | b | c | d |
| ④ | a | b | c | d |
| ⑤ | a | b | c | d |
| ⑥ | a | b | c | d |

2 ①

②

③

④

3 [a]

[b]

4 [a]

[b]

Exercise 5

On the triangle

1 Complete the following :

- ① The sum of measures of the interior angles of a triangle =
- ② The measure of the exterior angle of a triangle is equal to the sum of
- ③ If the measure of an angle in a triangle equals the sum of measures of the other two angles in the triangle , then the triangle is
- ④ If the measure of an angle in a triangle is greater than the sum of measures of the other two angles , then the triangle is
- ⑤ In ΔABC : If $m(\angle A) + m(\angle C) = m(\angle B)$, then $m(\angle B) = \dots\dots\dots^\circ$
- ⑥ In ΔABC : If $m(\angle B) > m(\angle A) + m(\angle C)$, then $\angle B$ is
- ⑦ It is possible to find a triangle each of its interior angles is of measure

2 Choose the correct answer from the given ones :

- ① The triangle contains two angles at least.
 - (a) acute
 - (b) obtuse
 - (c) right
 - (d) reflex
- ② The sum of measures of the interior angles of a triangle equals the measure of angle.
 - (a) a right
 - (b) a straight
 - (c) an acute
 - (d) a reflex
- ③ In ΔXYZ , if : $m(\angle X) = 50^\circ$, $m(\angle Y) = 100^\circ$, then : $m(\angle Z) = \dots\dots\dots$
 - (a) 30°
 - (b) 50°
 - (c) 80°
 - (d) 100°
- ④ In ΔABC , if : $m(\angle A) + m(\angle B) = 110^\circ$, then : $m(\angle C) = \dots\dots\dots$
 - (a) 110°
 - (b) 90°
 - (c) 70°
 - (d) 55°
- ⑤ If the measures of two angles in a triangle are 35° and 45° , then the triangle is
 - (a) acute-angled
 - (b) right-angled
 - (c) obtuse-angled
 - (d) equilateral
- ⑥ The measure of the exterior angle of the equilateral triangle at any one of its vertices equals
 - (a) 60°
 - (b) 120°
 - (c) 150°
 - (d) 30°

Unit 3

3 In each of the following figures, find the measure of the angle marked by (?) :

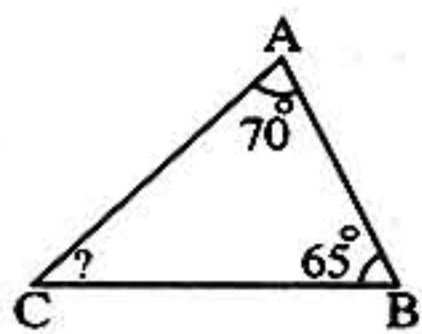


fig. (1)

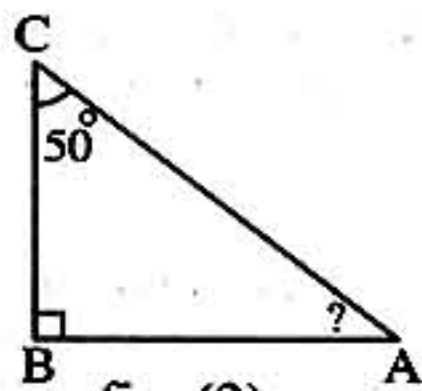


fig. (2)

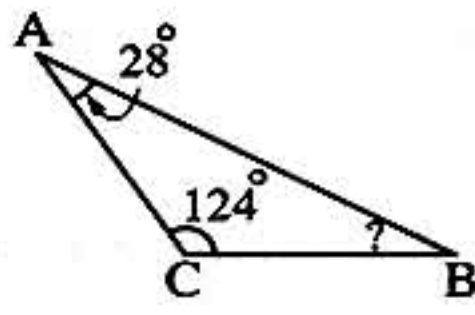


fig. (3)

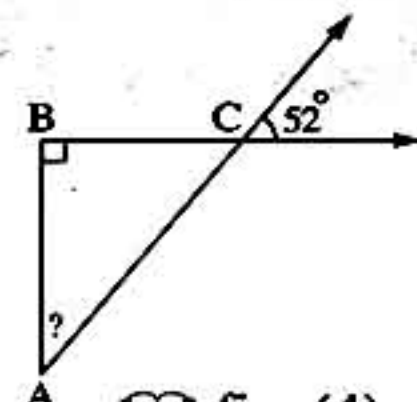


fig. (4)

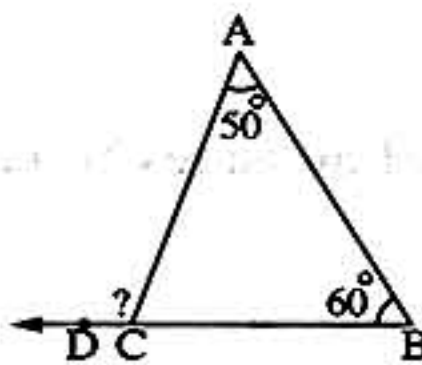


fig. (5)

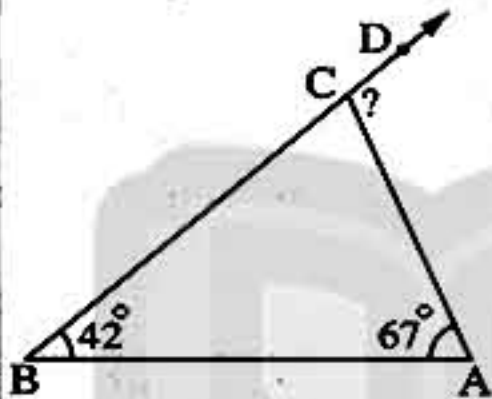


fig. (6)

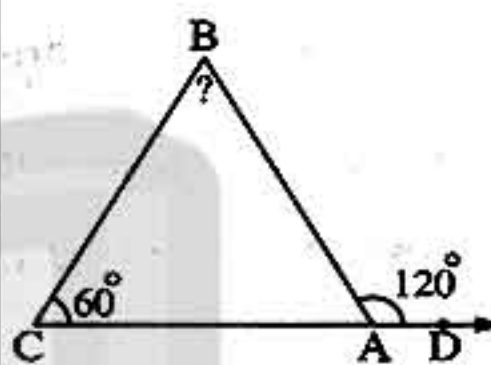


fig. (7)

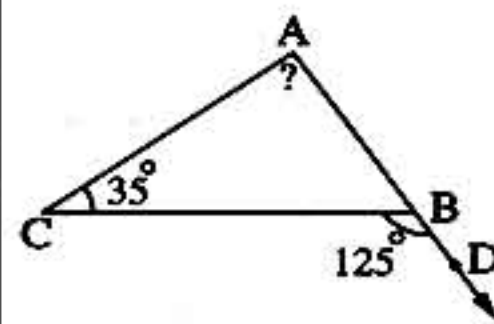


fig. (8)

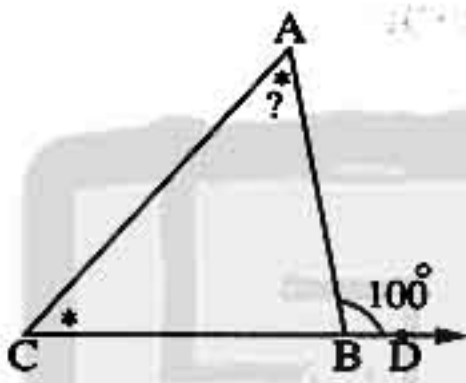


fig. (9)

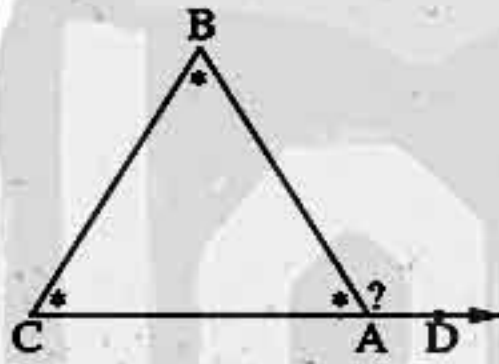


fig. (10)

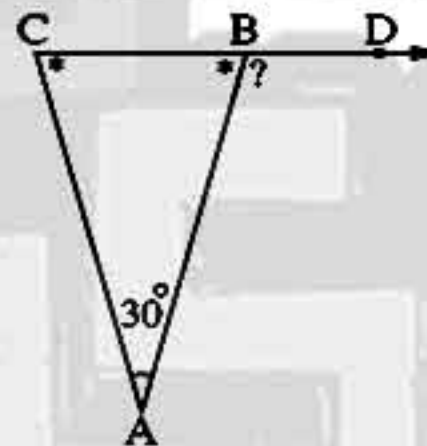


fig. (11)

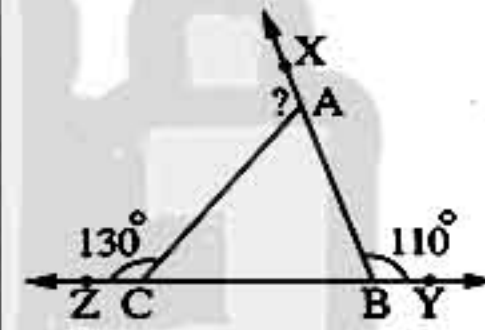


fig. (12)

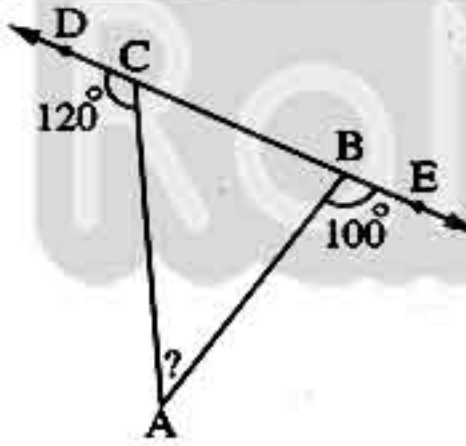


fig. (13)

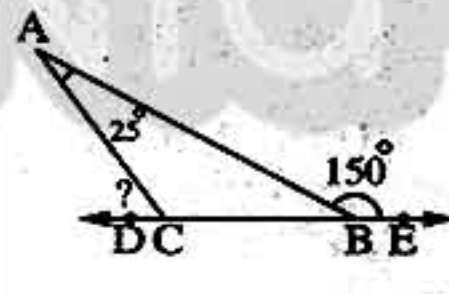


fig. (14)

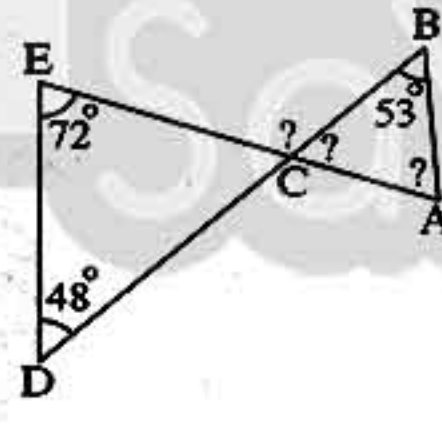


fig. (15)

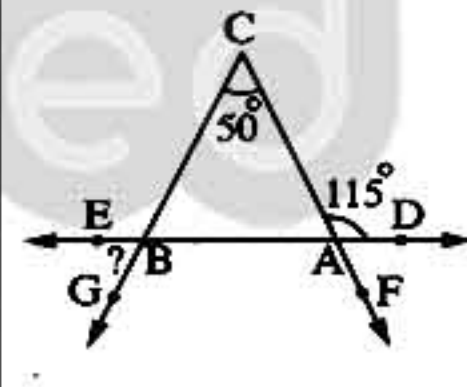


fig. (16)

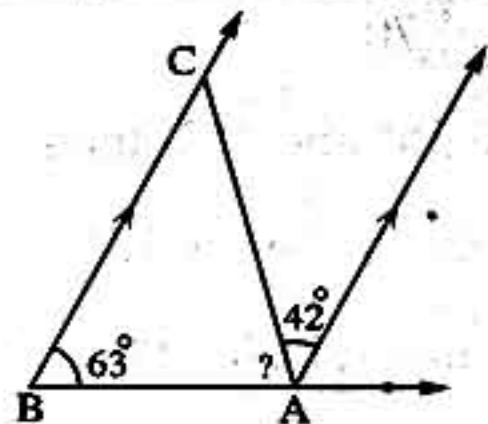


fig. (17)

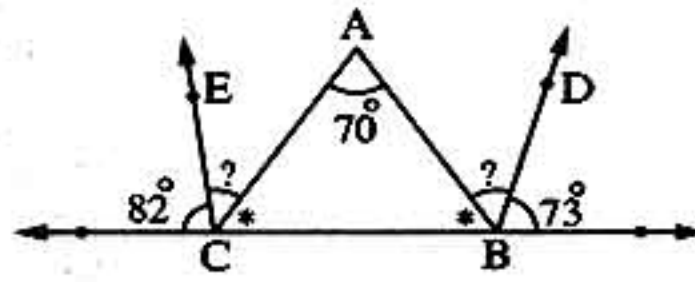
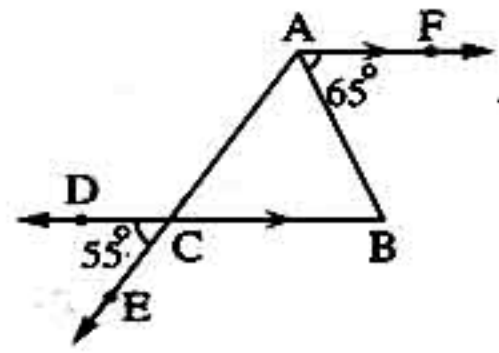


fig. (18)

Lesson Five

4 In the opposite figure :

$\overrightarrow{BD} \cap \overrightarrow{AE} = \{C\}$, $\overrightarrow{AF} \parallel \overrightarrow{BC}$, $m(\angle BAF) = 65^\circ$
 , $m(\angle DCE) = 55^\circ$



Complete the following proof to find :

the measures of the interior angles of ΔABC

Given

.....

R.T.F.

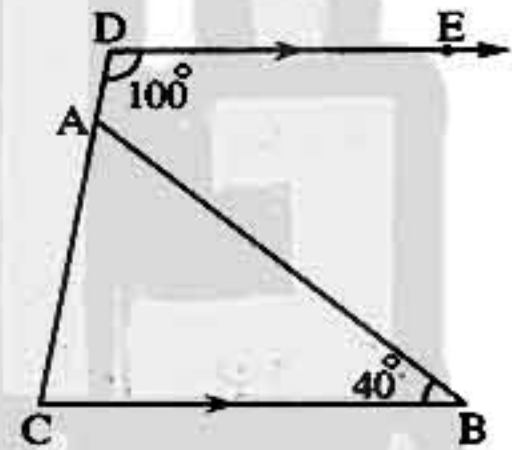
.....

Proof

$\therefore \overrightarrow{BD} \cap \overrightarrow{AE} = \{C\}$ (given)
 $\therefore m(\angle ACB) = m(\angle \dots) = \dots^\circ$ (.....)
 , $\therefore \overrightarrow{AF} \parallel \overrightarrow{BC}$, \overrightarrow{AB} is a transversal to them
 $\therefore m(\angle FAB) = m(\angle \dots) = \dots^\circ$ (..... angles)
 , \therefore The sum of measures of the interior angles of the triangle =
 $\therefore m(\angle BAC) = \dots^\circ - (\dots^\circ + \dots^\circ) = \dots^\circ$ (The req.)

5 In the opposite figure :

$A \in \overline{DC}$, $\overrightarrow{DE} \parallel \overrightarrow{CB}$, $m(\angle D) = 100^\circ$ and
 $m(\angle B) = 40^\circ$



Complete the following proof to find : $m(\angle BAD)$

Given

.....

R.T.F.

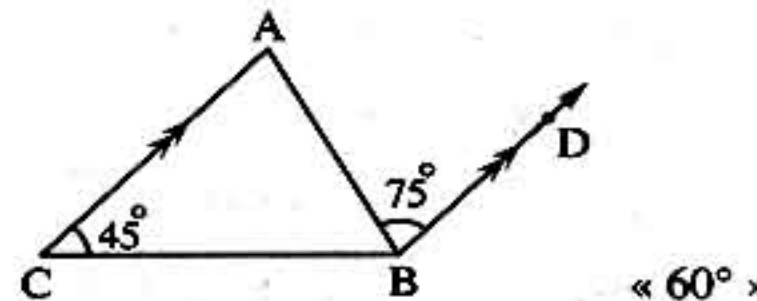
.....

Proof

$\therefore \overrightarrow{DE} \parallel \overrightarrow{\dots}$, $\overrightarrow{\dots}$ is a transversal.
 $\therefore m(\angle D) + m(\angle C) = \dots^\circ$
 (Two interior angles in the same side of the transversal)
 $\therefore m(\angle D) = \dots^\circ$
 $\therefore m(\angle C) = \dots - \dots = \dots^\circ$
 $\therefore \angle BAD$ is an exterior angle of $\Delta \dots$
 $\therefore m(\angle BAD) = m(\angle \dots) + m(\angle \dots)$
 $= \dots^\circ + \dots^\circ = \dots^\circ$ (The req.)

6 In the opposite figure :

$\overrightarrow{BD} \parallel \overrightarrow{CA}$, $m(\angle C) = 45^\circ$ and
 $m(\angle ABD) = 75^\circ$



Find : $m(\angle ABC)$

Unit 3

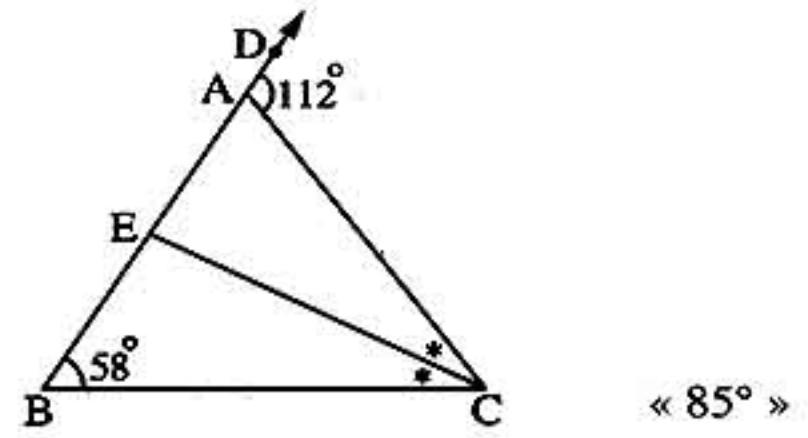
7 In the opposite figure :

ABC is a triangle in which : $m(\angle B) = 58^\circ$,

$E \in \overline{AB}$ such that \overline{CE} bisects $\angle ACB$,

$D \in \overline{BA}$ and $m(\angle CAD) = 112^\circ$

Find : $m(\angle AEC)$



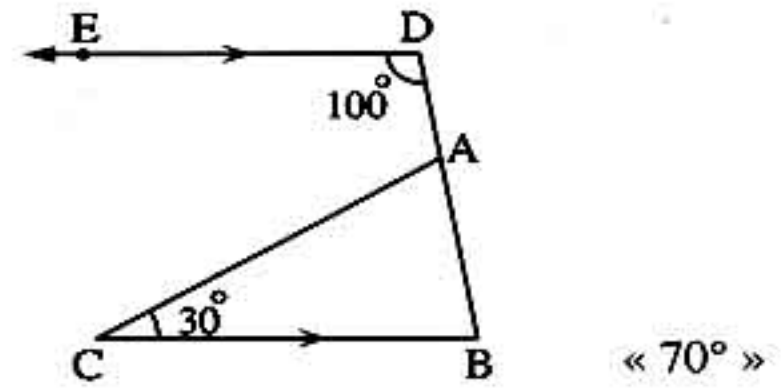
8 In the opposite figure :

$\overline{DE} \parallel \overline{BC}$, $m(\angle D) = 100^\circ$,

$m(\angle C) = 30^\circ$ and

$A \in \overline{DB}$

Find : $m(\angle BAC)$



9 In the opposite figure :

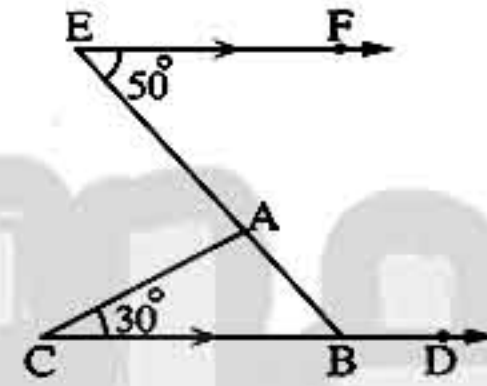
$\overline{EF} \parallel \overline{CD}$, $m(\angle E) = 50^\circ$ and

$m(\angle C) = 30^\circ$

Find the measures of the angles

of $\triangle ABC$ and $m(\angle ABD)$

« $m(\angle ABC) = 50^\circ$, $m(\angle BAC) = 100^\circ$, $m(\angle ABD) = 130^\circ$ »



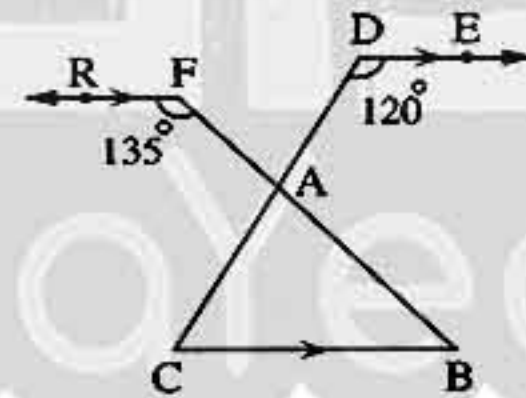
10 In the opposite figure :

$\overline{DE} \parallel \overline{FR} \parallel \overline{BC}$,

$m(\angle CDE) = 120^\circ$ and $m(\angle RFB) = 135^\circ$

Calculate the measures of the angles of $\triangle ABC$

« $m(\angle B) = 45^\circ$, $m(\angle C) = 60^\circ$, $m(\angle A) = 75^\circ$ »

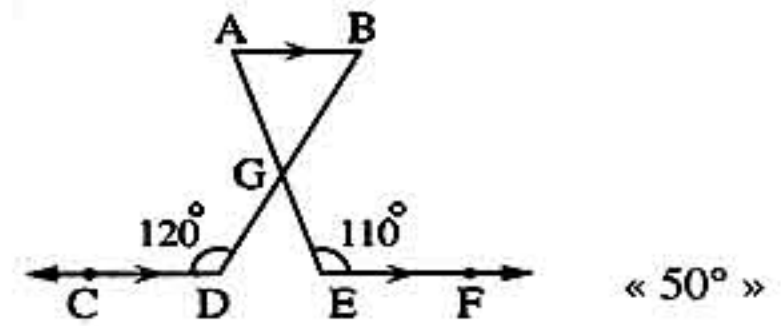


11 In the opposite figure :

$\overline{AB} \parallel \overline{DC} \parallel \overline{EF}$, $m(\angle E) = 110^\circ$ and

$m(\angle D) = 120^\circ$

Find : $m(\angle EGD)$



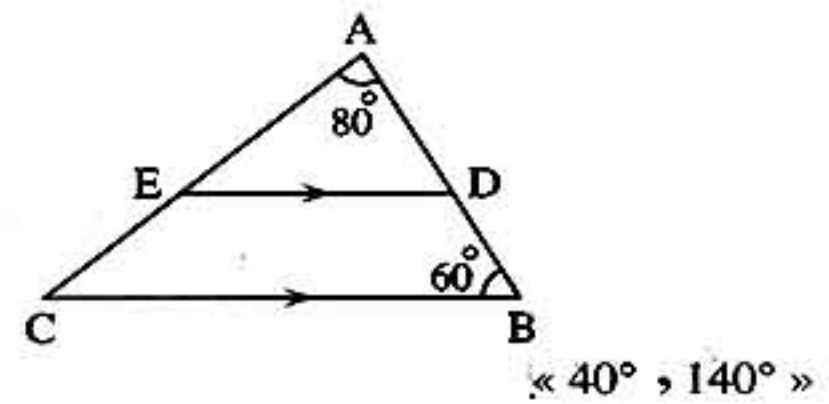
12 In the opposite figure :

ABC is a triangle in which : $m(\angle A) = 80^\circ$ and

$m(\angle B) = 60^\circ$

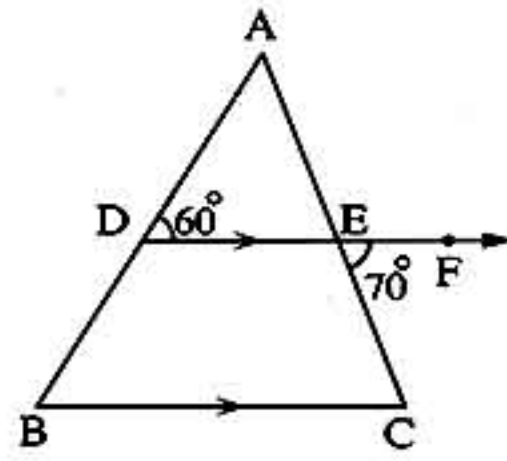
$\overline{DE} \parallel \overline{BC}$ where : $D \in \overline{AB}$ and $E \in \overline{AC}$

Find : $m(\angle AED)$ and $m(\angle DEC)$



13 In the opposite figure :

ABC is a triangle , $m(\angle ADE) = 60^\circ$,
 $m(\angle FEC) = 70^\circ$,
 $D \in \overline{AB}$, $\overline{DF} \parallel \overline{BC}$ and
 $\overline{AC} \cap \overline{DF} = \{E\}$

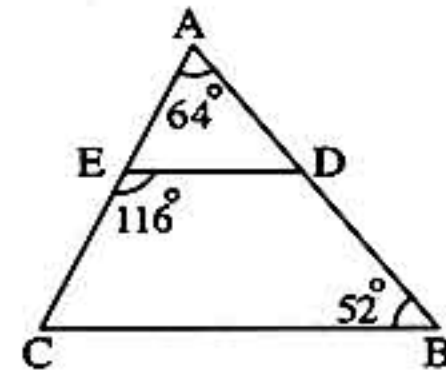


Find the measures of the interior angles of ΔABC

« $m(\angle C) = 70^\circ$, $m(\angle B) = 60^\circ$, $m(\angle A) = 50^\circ$ »

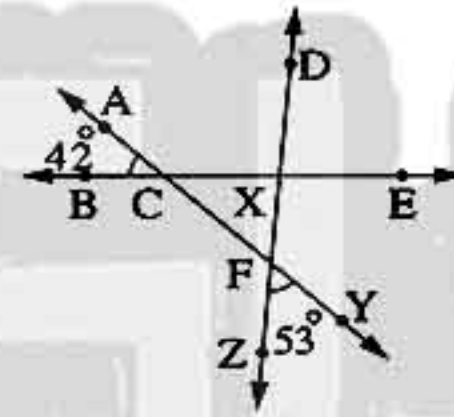
14 In the opposite figure :

ABC is a triangle in which $m(\angle A) = 64^\circ$,
 $m(\angle B) = 52^\circ$,
 $m(\angle DEC) = 116^\circ$, $E \in \overline{AC}$ and $D \in \overline{AB}$
Prove that : $\overline{DE} \parallel \overline{BC}$



15 In the opposite figure :

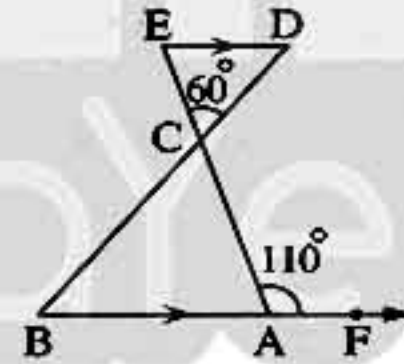
Prove that :
 $m(\angle DXE) = 85^\circ$,
 then calculate $m(\angle DXC)$
 and $m(\angle EXF)$



« 95° , 95° »

16 In the opposite figure :

$\overline{ED} \parallel \overline{BA}$, $m(\angle CAF) = 110^\circ$,
 $\overline{DB} \cap \overline{AE} = \{C\}$,
 $m(\angle DCE) = 60^\circ$ and $F \in \overline{BA}$

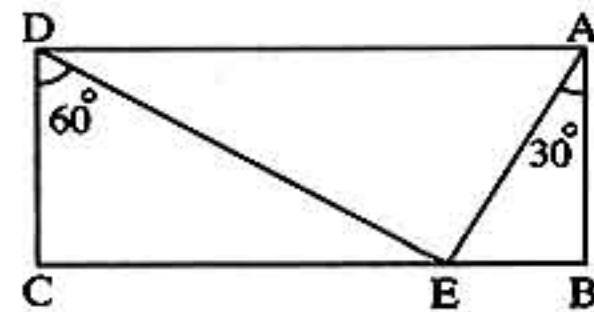


Find the measures of the angles of the two triangles DCE and ABC

« $m(\angle E) = 70^\circ$, $m(\angle D) = 50^\circ$, $m(\angle B) = 50^\circ$, $m(\angle ACB) = 60^\circ$, $m(\angle BAC) = 70^\circ$ »

17 In the opposite figure :

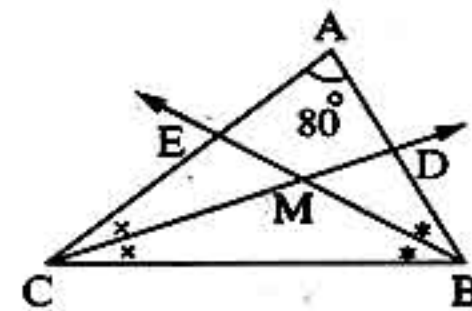
ABCD is a rectangle , $E \in \overline{BC}$ where :
 $m(\angle BAE) = 30^\circ$ and $m(\angle EDC) = 60^\circ$
Find : $m(\angle AED)$



« 90° »

18 In the opposite figure :

\overline{BM} bisects $\angle ABC$ and \overline{CM} bisects $\angle ACB$
 If $m(\angle A) = 80^\circ$,
find : $m(\angle EMD)$



« 130° »

Unit 3

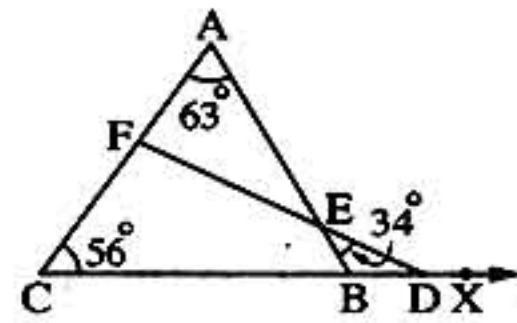
19) In the opposite figure :

ABC is a triangle , $D \in \overline{CB}$, $X \in \overline{CB}$,

$m(\angle A) = 63^\circ$, $m(\angle C) = 56^\circ$ and

$m(\angle DEB) = 34^\circ$

Find : $m(\angle EDX)$



« 153° »

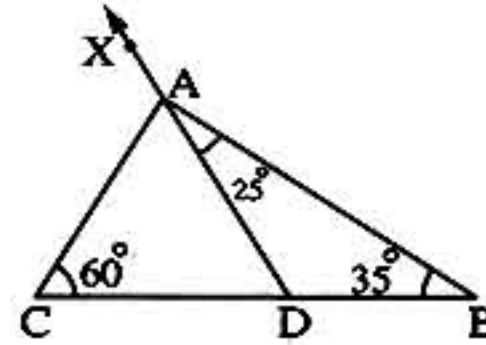
20) In the opposite figure :

ABC is a triangle , $m(\angle B) = 35^\circ$,

$m(\angle C) = 60^\circ$, $m(\angle BAD) = 25^\circ$,

$D \in \overline{BC}$ and $X \in \overline{DA}$

Find : $m(\angle XAC)$



« 120° »

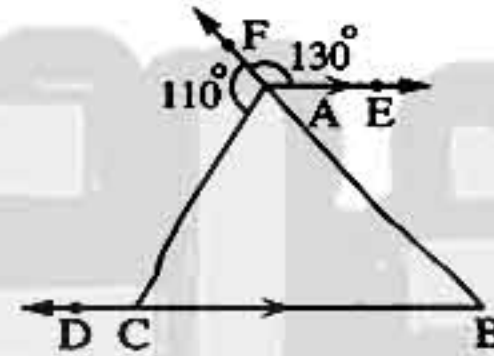
21) In the opposite figure :

ABC is a triangle , $\overline{AE} \parallel \overline{BC}$, $D \in \overline{BC}$,

$F \in \overline{BA}$, $m(\angle FAE) = 130^\circ$ and

$m(\angle FAC) = 110^\circ$

Find : $m(\angle ACD)$



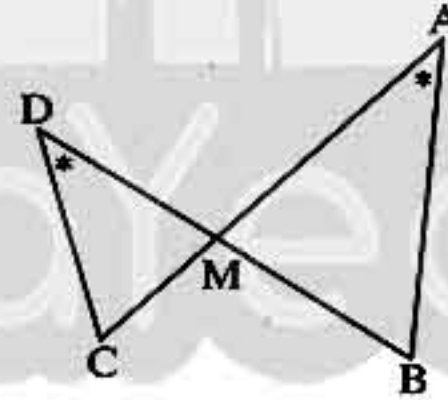
« 120° »

22) In the opposite figure :

$\overline{AC} \cap \overline{BD} = \{M\}$ and

$m(\angle A) = m(\angle D)$

Prove that : $m(\angle B) = m(\angle C)$

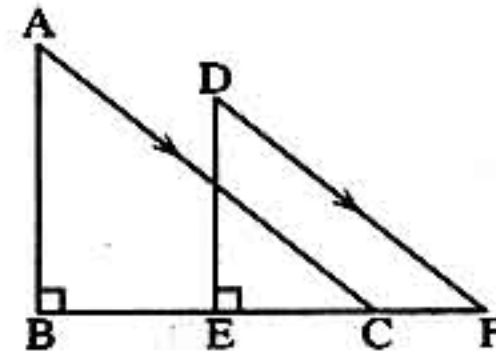


23) In the opposite figure :

The points F , C , E and B are collinear ,

$m(\angle B) = m(\angle DEC) = 90^\circ$ and $\overline{AC} \parallel \overline{DF}$

Prove that : $m(\angle A) = m(\angle D)$



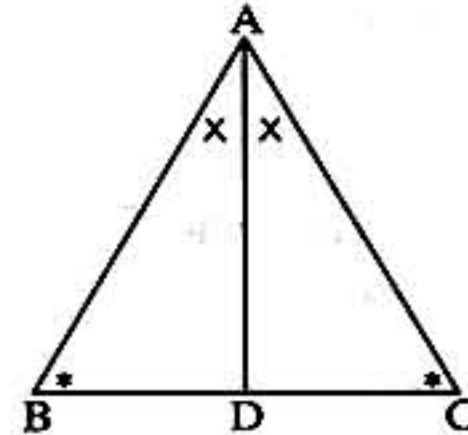
24) In the opposite figure :

ABC is a triangle ,

$m(\angle B) = m(\angle C)$ and

\overline{AD} is the bisector of $\angle A$

Prove that : $AB = AC$

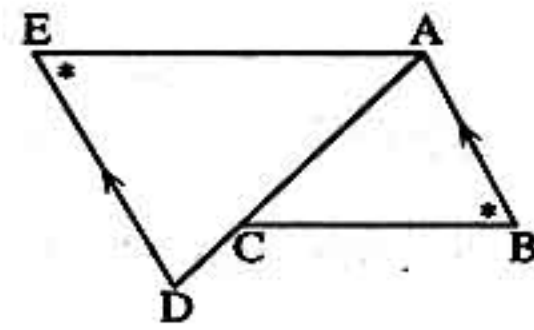


25 In the opposite figure :

$\overline{AB} \parallel \overline{ED}$ and

$m(\angle ABC) = m(\angle AED)$

Prove that : $\overline{BC} \parallel \overline{AE}$



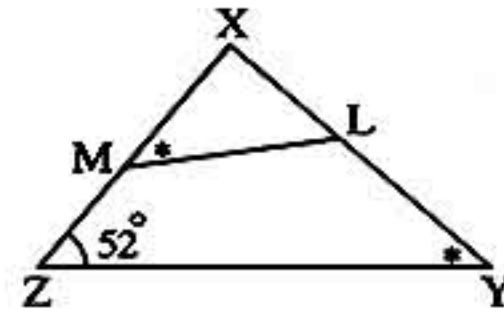
26 In the opposite figure :

XYZ is a triangle in which $m(\angle Z) = 52^\circ$,

$L \in \overline{XY}$ and $M \in \overline{XZ}$ such that :

$m(\angle Y) = m(\angle XML)$

Find : $m(\angle XLM)$



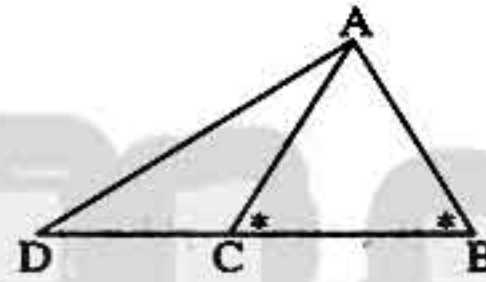
« 52° »

27 In the opposite figure :

ABC is a triangle in which :

$m(\angle B) = m(\angle ACB)$ and $D \in \overline{BC}$

Prove that : $m(\angle B) > m(\angle D)$



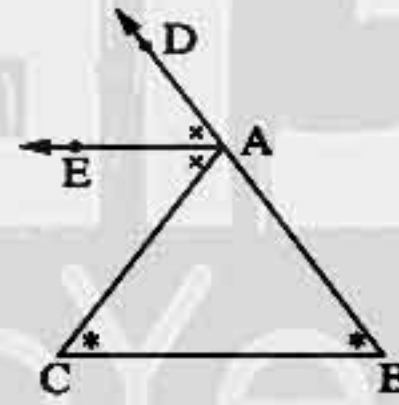
28 In the opposite figure :

ABC is a triangle in which :

$m(\angle B) = m(\angle C)$, $D \in \overline{BA}$ and

\overline{AE} bisects $\angle DAC$

Prove that : $\overline{AE} \parallel \overline{BC}$



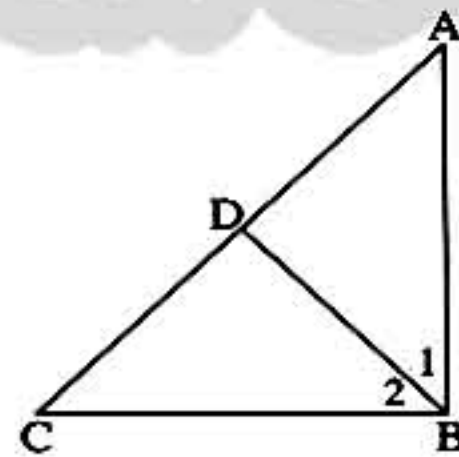
29 In the opposite figure :

ABC is a triangle in which : $D \in \overline{AC}$,

$m(\angle 1) = m(\angle A)$ and

$m(\angle 2) = m(\angle C)$

Prove that : $\angle ABC$ is a right angle.



Unit 3



For excellent pupils

- 30) ABC is a triangle in which : $m(\angle A) = 2m(\angle C)$ and $m(\angle B) = 4m(\angle C)$

Prove that : $\angle B$ is an obtuse angle.

- 31) ABC is a triangle in which : $m(\angle C) = 28^\circ$, $m(\angle A) = 4x^\circ$
 , $m(\angle B) = (2x + 2)^\circ$

Find : $m(\angle A)$ and $m(\angle B)$

« 100° , 52° »

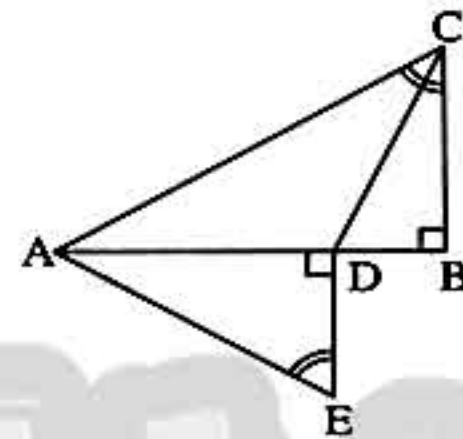
- 32) In the opposite figure :

ABC is a triangle in which : $D \in \overline{AB}$

$m(\angle B) = 90^\circ$, $m(\angle ADE) = 90^\circ$ and

$m(\angle ACB) = m(\angle E)$

Prove that : $m(\angle BDC) > m(\angle DAE)$



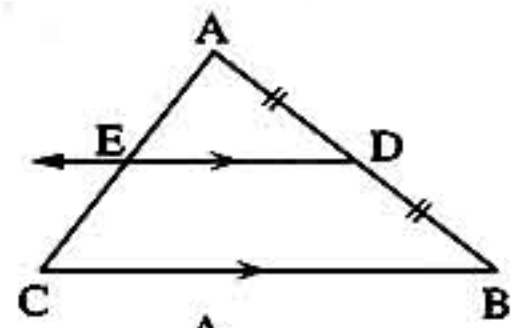
Exercise 6 On theorem 2 and its corollary, and theorem 3

1 Complete the following :

- ① The ray drawn from the midpoint of a side of a triangle parallel to another side
- ② The line segment joining the midpoints of two sides of a triangle is the third side.
- ③ The length of the line segment joining the midpoints of two sides of a triangle equals

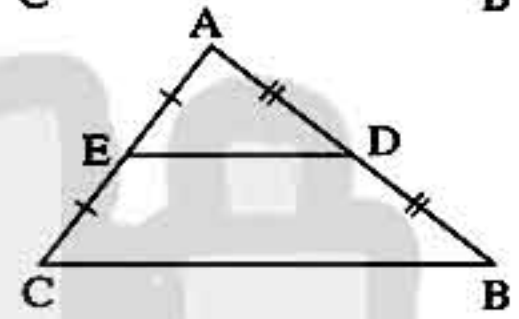
④ In the opposite figure :

If D is the midpoint of \overline{AB} , $\overline{DE} \parallel \overline{BC}$,
then : is the midpoint of



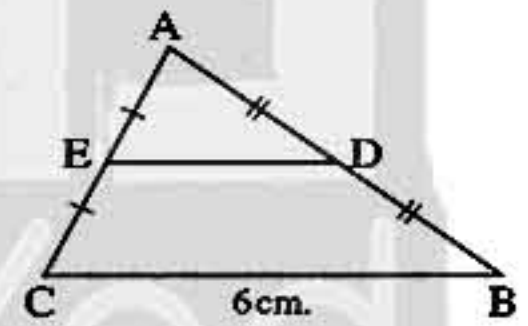
⑤ In the opposite figure :

If D and E are the midpoints of \overline{AB} and \overline{AC} respectively,
then : //



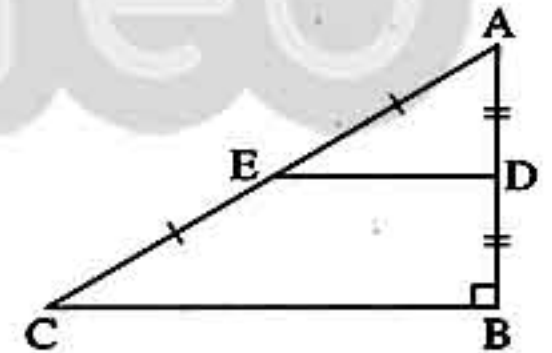
⑥ In the opposite figure :

\because D and E are the midpoints of \overline{AB} and \overline{AC} respectively,
 $\therefore BC = 6$ cm.
 $\therefore DE =$ cm



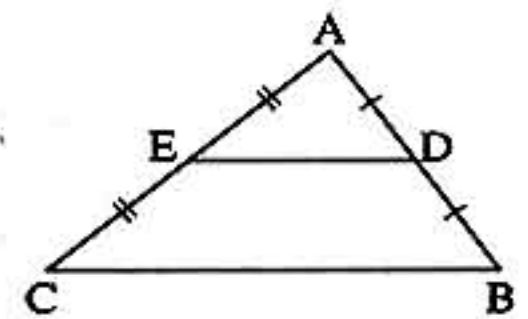
⑦ In the opposite figure :

If : $m(\angle B) = 90^\circ$, D and E are the
midpoints of \overline{AB} and \overline{AC} respectively,
then : $m(\angle ADE) =$



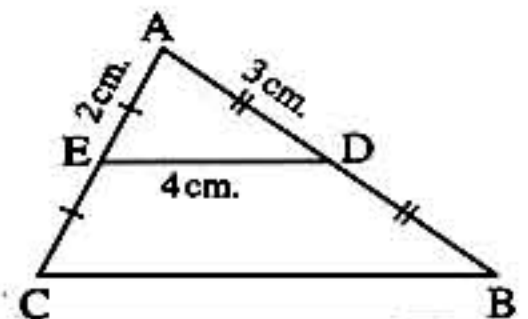
⑧ In the opposite figure :

If : D and E are the midpoints of \overline{AB} and \overline{AC} respectively,
and the perimeter of the triangle ABC = 24 cm.
then the perimeter of the triangle ADE = cm.



⑨ In the opposite figure :

\because D and E are the midpoints of \overline{AB} and \overline{AC} respectively,
 $\therefore AD = 3$ cm., $AE = 2$ cm. and $DE = 4$ cm.
 \therefore The perimeter of the figure DBCE = cm.



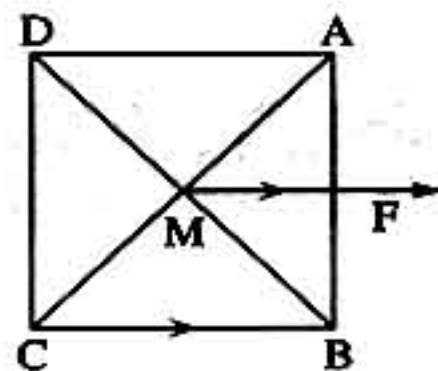
Unit 3

● In the opposite figure :

If the perimeter of the square ABCD = 20 cm.

, $\overline{MF} \parallel \overline{CB}$ where $F \in \overline{AB}$

, then : AF = cm.

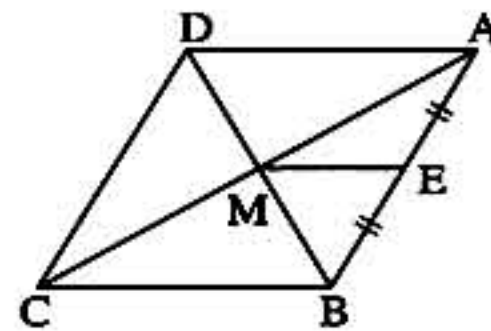


● In the opposite figure :

∴ The perimeter of the rhombus ABCD = 24 cm.,

E is the midpoint of \overline{AB}

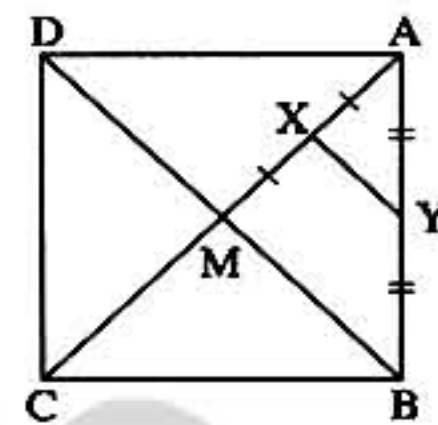
∴ ME = cm.



● In the opposite figure :

∴ ABCD is a square, X and Y are the midpoints of \overline{AM} and \overline{AB} respectively and AC = 12 cm.

∴ XY = cm., $m(\angle A Y X) = \dots\dots\dots^\circ$



2) In the opposite figure :

ABCD is a parallelogram, DC = 5 cm.

, $F \in \overline{BC}$, $\overline{DF} \cap \overline{AB} = \{E\}$,

if : DF = FE

Complete the following proof to find the length of \overline{BE}

Given

R.T.F.

Proof ∴ ABCD is a

∴ $\overline{AD} \parallel \dots\dots\dots$ ∴ $\overline{BF} \parallel \dots\dots\dots$

, In ΔAED :

∴ F is the midpoint of, $\overline{BF} \parallel \dots\dots\dots$

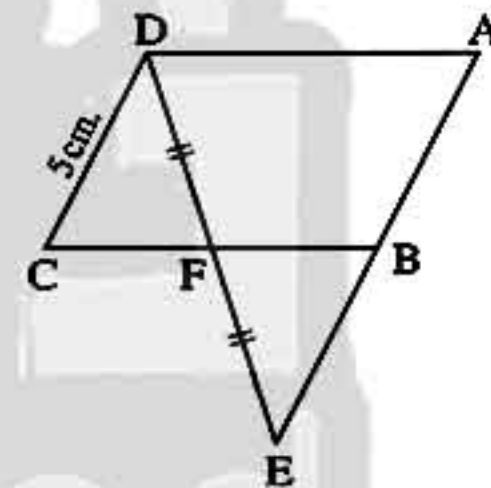
∴ B is the midpoint of

∴ AB =

, ∴ AB = = cm. (Properties of

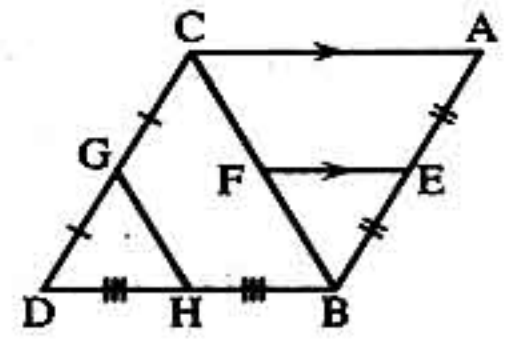
∴ BE = cm.

(The req.)



3 In the opposite figure :

ABC is a triangle in which $CA = CB$,
 E is the midpoint of \overline{AB} , $\overline{EF} \parallel \overline{AC}$,
 H and G are the two midpoints of \overline{BD} and \overline{CD} respectively.



Complete the following proof to prove that : $EF = GH$

Given

R.T.P.

Proof In ΔABC :

\therefore E is the midpoint of, $\overline{EF} \parallel$

\therefore F is the midpoint of

$\therefore EF = \frac{1}{2}$

, In ΔBDC :

\therefore H is the midpoint of

, is the midpoint of \overline{CD}

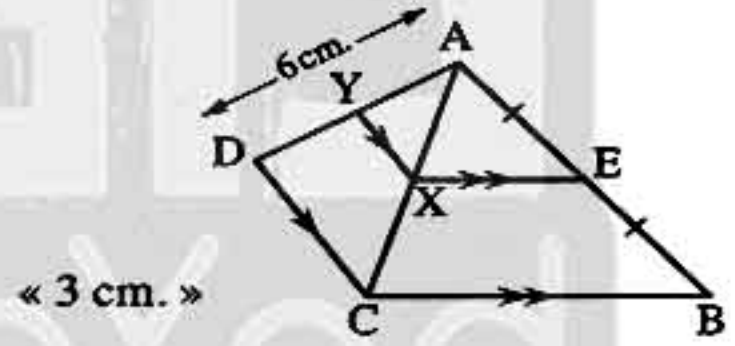
$\therefore GH = \frac{1}{2}$

$\therefore CA =$ $\therefore EF =$ (Q.E.D.)

4 In the opposite figure :

$AE = EB$, $\overline{EX} \parallel \overline{BC}$, $\overline{XY} \parallel \overline{CD}$
 and $AD = 6$ cm.

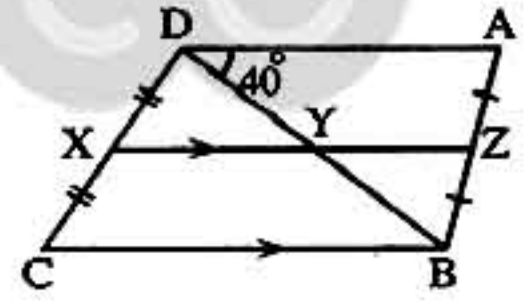
Find the length of : \overline{AY}



5 In the opposite figure :

X is the midpoint of \overline{CD}
 , Z is the midpoint of \overline{AB}
 , $\overline{XY} \parallel \overline{CB}$, $m(\angle ADB) = 40^\circ$

Find : $m(\angle ZYB)$



6 In the opposite figure :

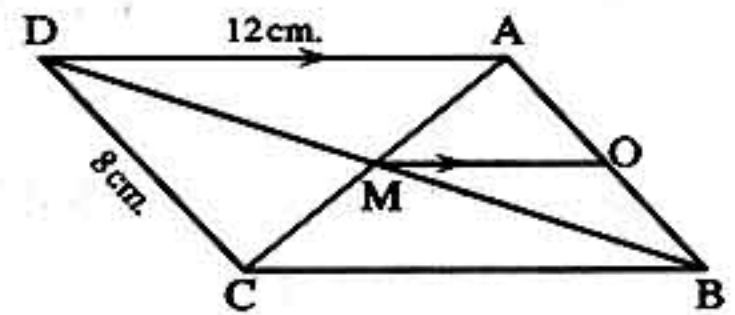
ABCD is a parallelogram , $\overline{AC} \cap \overline{BD} = \{M\}$

Draw $\overline{MO} \parallel \overline{AD}$ to cut \overline{AB} at O

If : $AD = 12$ cm. and $DC = 8$ cm.

, then find : ● The perimeter of ABCD

● The length of \overline{AO}



« 40 cm. , 4 cm. »

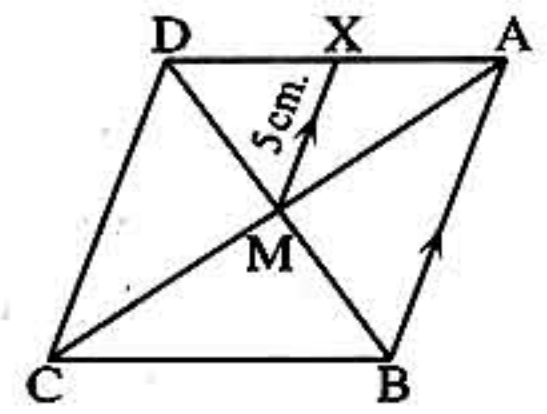
Unit 3

7 In the opposite figure :

ABCD is a parallelogram , its diagonals intersect at M

Draw $\overline{MX} \parallel \overline{BA}$ to intersect \overline{AD} at X

- ① Prove that : X is the midpoint of \overline{AD}
 ② If $MX = 5 \text{ cm.}$, then find the length of \overline{CD}



« 10 cm. »

8 ABCD is a parallelogram , its diagonals intersect at M, $\overline{ME} \parallel \overline{BA}$ and cuts \overline{AD} at E

Prove that : $ME = \frac{1}{2} DC$

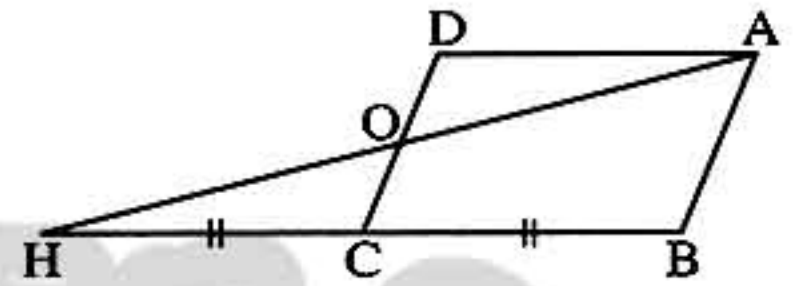
9 In the opposite figure :

ABCD is a parallelogram ,

$BC = CH$, $H \in \overline{BC}$

Draw \overline{AH} to cut \overline{DC} at O

Prove that : $AO = OH$

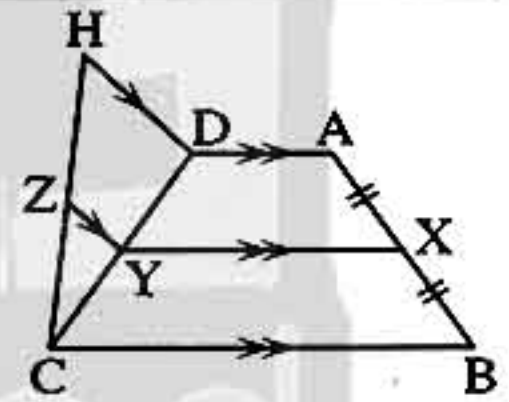


10 In the opposite figure :

ABCD is a trapezium , $\overline{AD} \parallel \overline{BC}$, X is the midpoint of \overline{AB}

If $\overline{AD} \parallel \overline{XY}$ where $Y \in \overline{DC}$, $\overline{YZ} \parallel \overline{DH}$

Prove that : $CZ = ZH$

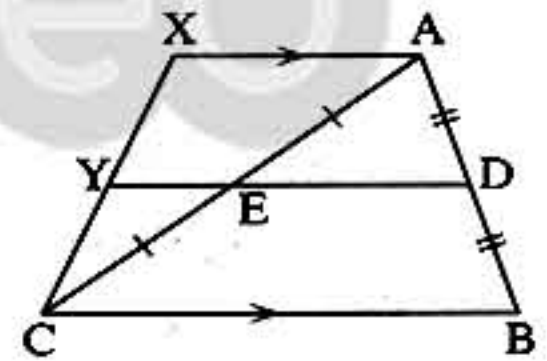


11 In the opposite figure :

$AD = DB$, $AE = EC$,

$\overline{AX} \parallel \overline{BC}$, $\overline{DE} \cap \overline{XC} = \{Y\}$

Prove that : Y is the midpoint of \overline{XC}



12 In the opposite figure :

ABCD is a quadrilateral in which :

X and Z are the midpoints of \overline{AB}

and \overline{AD} respectively and $Y \in \overline{AC}$ such that :

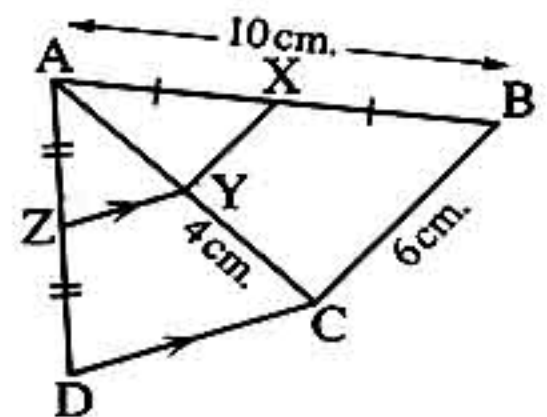
$\overline{YZ} \parallel \overline{CD}$ and $YC = 4 \text{ cm.}$

If $BC = 6 \text{ cm.}$ and $AB = 10 \text{ cm.}$, then

find : ① The length of \overline{AY}

② The perimeter of $\triangle AXY$

« 4 cm. , 12 cm. »

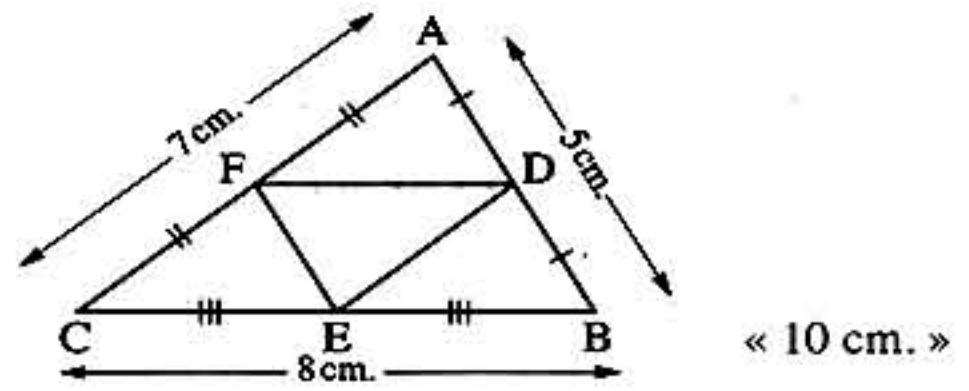


13 In the opposite figure :

$$AB = 5 \text{ cm.}, BC = 8 \text{ cm.},$$

$AC = 7 \text{ cm.}$, D, E and F are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively.

Calculate the perimeter of : ΔDEF



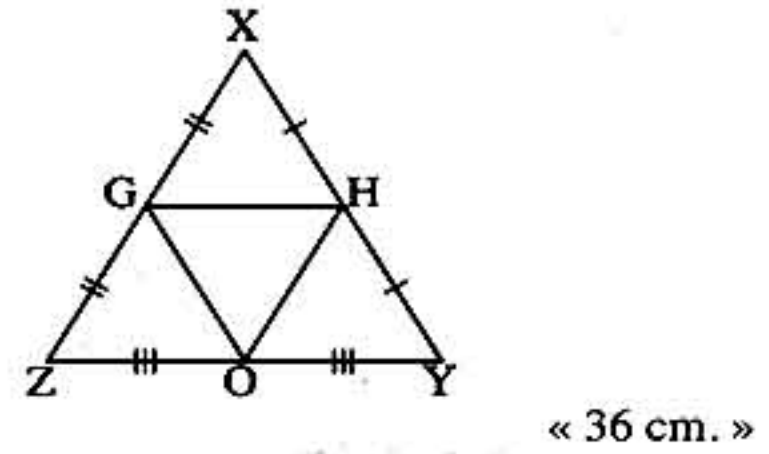
14 In the opposite figure :

XYZ is a triangle in which :

H, O and G are the midpoints of \overline{XY} , \overline{YZ} and \overline{ZX} respectively.

If the perimeter of ΔHOG is 18 cm. ,

then find the perimeter of : ΔXYZ



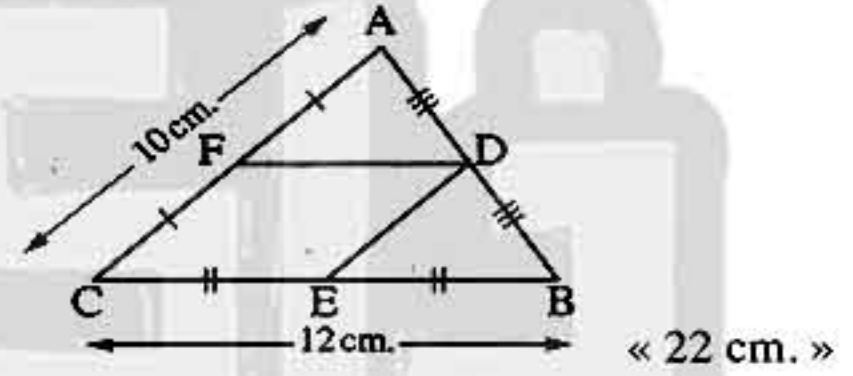
15 ABC is a triangle , if X , Y and Z are the midpoints of \overline{AB} , \overline{BC} and \overline{AC} respectively. **Prove that :** the perimeter of $\Delta XYZ = \frac{1}{2}$ that of ΔABC

16 In the opposite figure :

ABC is a triangle in which D, E and F are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively,

$$BC = 12 \text{ cm.}, AC = 10 \text{ cm.}$$

Find the perimeter of the figure DECF



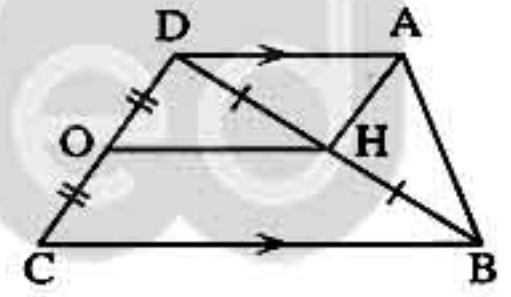
17 In the opposite figure :

$$\overline{AD} \parallel \overline{BC}, AD = \frac{1}{2} \overline{BC},$$

H is the midpoint of \overline{BD} ,

O is the midpoint of \overline{CD}

Prove that : AHOD is a parallelogram.

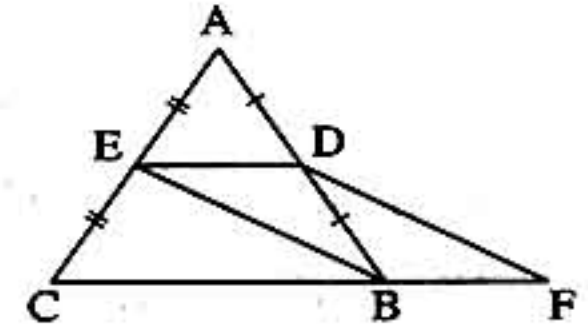


18 In the opposite figure :

D and E are the midpoints of \overline{AB} and \overline{AC} respectively,

$F \in \overline{CB}$ where $BF = \frac{1}{2} BC$

Prove that : BEDF is a parallelogram.



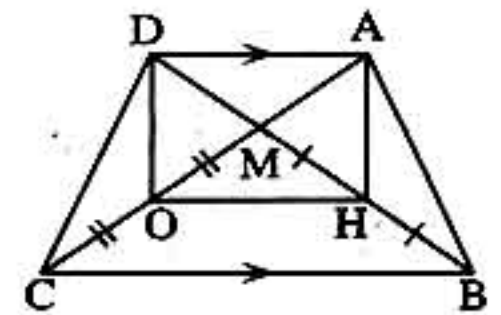
19 In the opposite figure :

ABCD is a trapezium in which $\overline{AD} \parallel \overline{BC}$

and $AD = \frac{1}{2} BC$ and $\overline{AC} \cap \overline{DB} = \{M\}$

Let H and O are the midpoints of \overline{MB} and \overline{MC} respectively.

Prove that : AHOD is a parallelogram.



Unit 3

20 In the opposite figure :

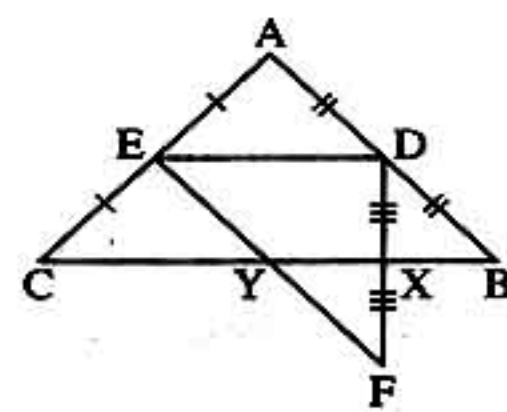
D is the midpoint of \overline{AB} ,

E is the midpoint of \overline{AC} ,

$\overline{DF} \cap \overline{BC} = \{X\}$, $DX = XF$,

$BC = 12$ cm.

Find the length of : \overline{XY}



« 3 cm. »

21 In the opposite figure :

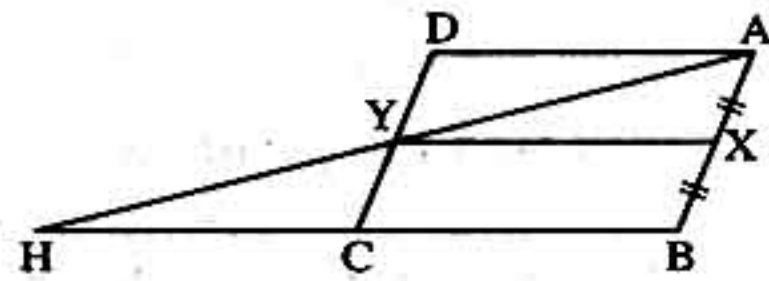
ABCD is a parallelogram,

X is the midpoint of \overline{AB}

Draw $\overline{XY} \parallel \overline{BC}$ to cut \overline{DC} at Y

Draw \overline{AY} to cut \overline{BC} at H

Prove that : C is the midpoint of \overline{BH}



22 In the opposite figure :

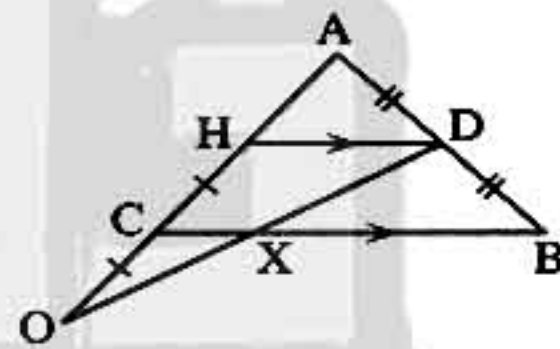
ABC is a triangle , D is the midpoint of \overline{AB} ,

$\overline{DH} \parallel \overline{BC}$, $O \in \overline{AC}$ such that $HC = CO$

Prove that : $CO = \frac{1}{3} AO$

If we draw \overline{DO} to cut \overline{BC} at X , then

prove that : $OX = XD$



23 In the opposite figure :

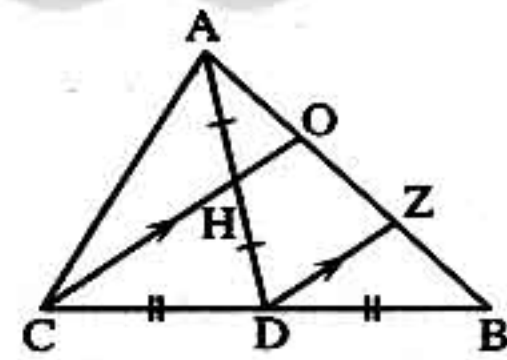
ABC is a triangle , D is the midpoint of \overline{BC}

and H is the midpoint of \overline{AD}

Draw \overline{CH} to cut \overline{AB} at O,

then draw $\overline{DZ} \parallel \overline{CO}$ to cut \overline{AB} at Z

Prove that : $AO = OZ = ZB$



24 ABCD is a parallelogram. M is the intersection point of its diagonals ,

draw $\overline{CE} \parallel \overline{BD}$ to cut \overline{AB} at E and \overline{AD} at F

Prove that : ● $AB = BE$ ● $AD = DF$

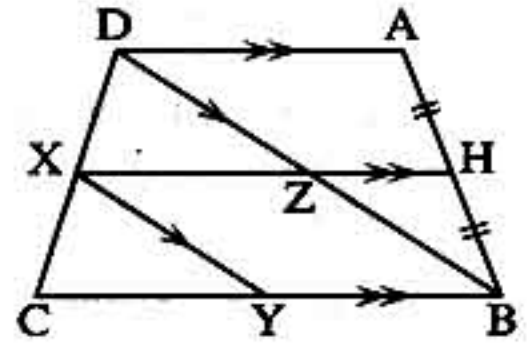
25 In the opposite figure :

ABCD is a trapezium in which $\overline{AD} \parallel \overline{BC}$

Let H be the midpoint of \overline{AB} ,

$\overline{HX} \parallel \overline{BC}$ and $\overline{XY} \parallel \overline{DB}$

Prove that : Y is the midpoint of \overline{BC}



26 ABCD is a trapezium in which $\overline{AD} \parallel \overline{BC}$, E is the midpoint of \overline{AB} , draw $\overline{EX} \parallel \overline{BC}$ to cut \overline{DB} at X, \overline{DC} at Y, and draw $\overline{YZ} \parallel \overline{DB}$ to cut \overline{BC} at Z

Prove that : $XD = YZ$

27 ABC is a triangle in which $AB = 9$ cm. , $AC = 8$ cm. , $D \in \overline{AB}$,

$E \in \overline{AB}$ such that $AD = DE = EB$ and \overline{DX} , \overline{EY} are drawn parallel to \overline{BC} and cutting \overline{AC} at X and Y respectively , where $DX = 4$ cm.

Calculate : the perimeter of the shape DEYX

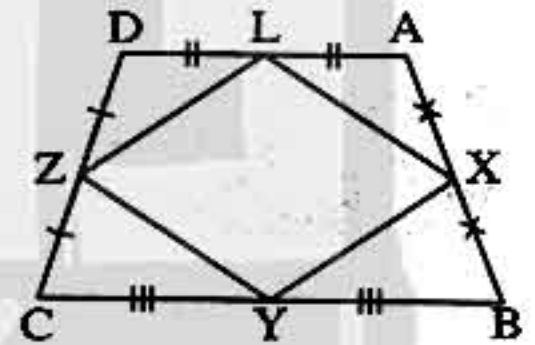
« $17\frac{2}{3}$ cm. »

28 In the opposite figure :

ABCD is a quadrilateral in which X , Y , Z and L

are the midpoints of \overline{AB} , \overline{BC} , \overline{CD} and \overline{DA} respectively.

Prove that : XYZL is a parallelogram.



29 ABC is a triangle in which $AB = AC$, X , Y and Z are the midpoints of \overline{AB} , \overline{BC} and \overline{CA} respectively.

Prove that : AXYZ is a rhombus.

30 In the opposite figure :

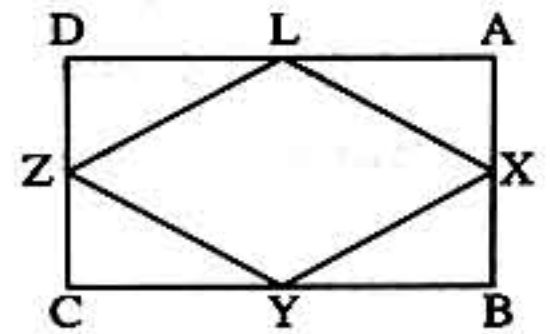
ABCD is a rectangle and X , Y , Z and L

are the midpoints of \overline{AB} , \overline{BC} , \overline{CD} and \overline{DA} respectively.

Prove that :

● XYZL is a rhombus.

● The perimeter of the rhombus = 2 BD



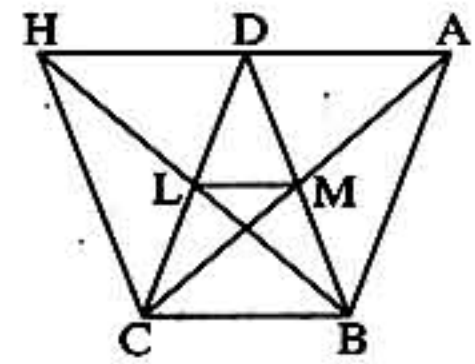
Unit 3

31 In the opposite figure :

ABCD and DBCH are two parallelograms having a common base \overline{BC} and on one side of \overline{BC}

Let $\overline{AC} \cap \overline{BD} = \{M\}$ and $\overline{DC} \cap \overline{BH} = \{L\}$

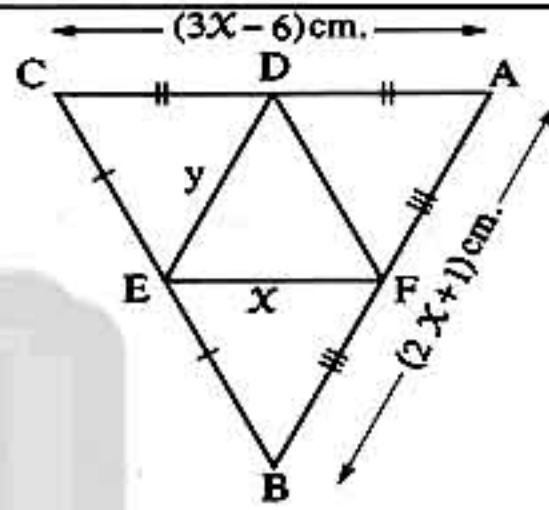
Prove that : ① $\overline{ML} \parallel \overline{BC}$ ② $ML = \frac{1}{4} AH$



32 Connected with algebra :

In the opposite figure :

Find the value of each of : x and y



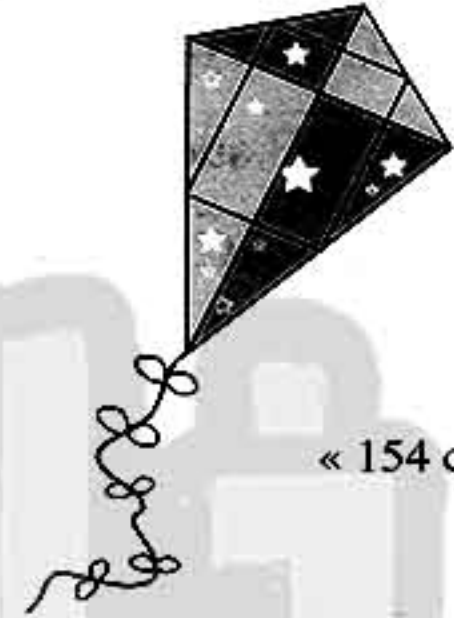
« 6 cm. , 6.5 cm. »



Life Application

33 Sara wants to design a kite whose two diagonals are 64 cm. and 90 cm.

She want to put a stripe to decorate the kite such that the stripe joins between the midpoints of the sides of the kite. How long is the stripe ?



« 154 cm. »



For excellent pupils

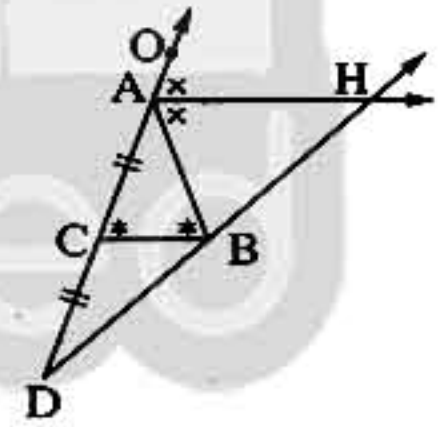
34 In the opposite figure :

ABC is a triangle in which : $m(\angle ABC) = m(\angle ACB)$

, $D \in \overline{AC}$ such that $AC = CD$ and $O \in \overline{CA}$

Let \overline{AH} bisects $\angle BAO$ such that : $\overline{AH} \cap \overline{DB} = \{H\}$

Prove that : $DB = BH$



35 ABCD is a quadrilateral in which $\overline{AC} \perp \overline{BD}$ and X , Y , Z and L are the midpoints of \overline{AB} , \overline{BC} , \overline{CD} and \overline{DA} respectively.

Prove that : XYZL is a rectangle whose area equals $\frac{1}{4} AC \times BD$

EL-MOSSER

At the end of this exercise answer the models of the mid-term examination in Geometry

In El-Mosser notebook

Exercise

7

On Pythagoras' theorem

1 In each of the following figures, find the length of the unknown side :

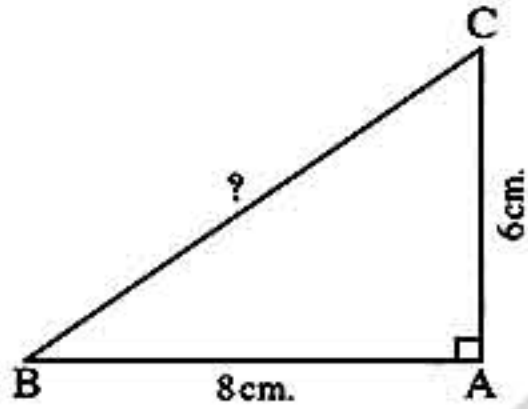


Fig. (1)

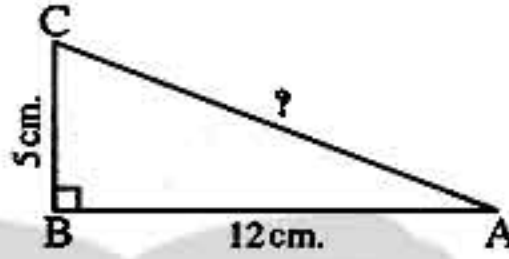


Fig. (2)

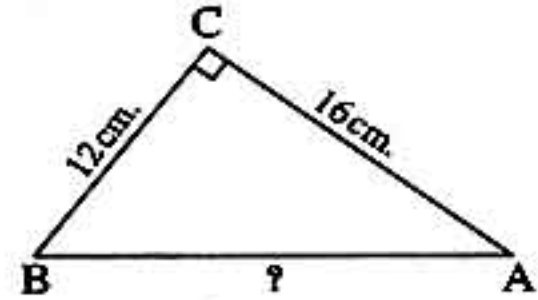


Fig. (3)

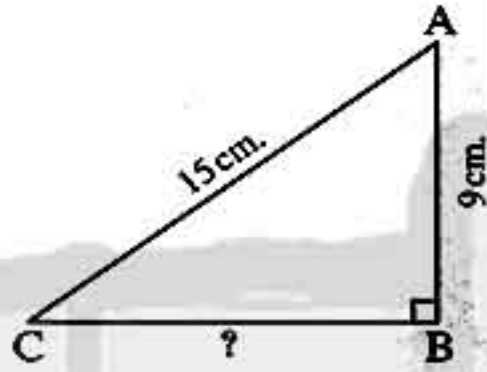


Fig. (4)



Fig. (5)

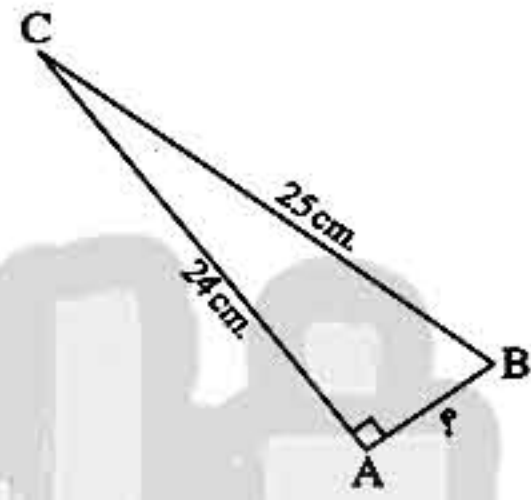


Fig. (6)

2 In the opposite figure :

ABCD is a square whose side length = 4 cm.

and $E \in \overline{BC}$ where $CE = 3$ cm.

Complete the following proof to find the length of \overline{DE}

\therefore ABCD is a square

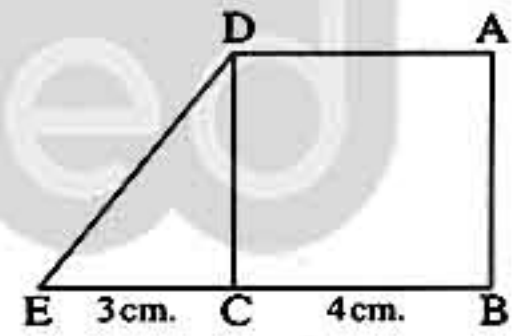
$\therefore DC = \dots\dots\dots$ cm, $m(\angle DCB) = \dots\dots\dots^\circ$

\therefore In $\triangle DCE$: $(DE)^2 = (\dots\dots\dots)^2 + (CE)^2 = (\dots\dots\dots)^2 + (3)^2$

$= \dots\dots\dots + \dots\dots\dots = \dots\dots\dots$

$\therefore DE = \dots\dots\dots$ cm.

(The req.)



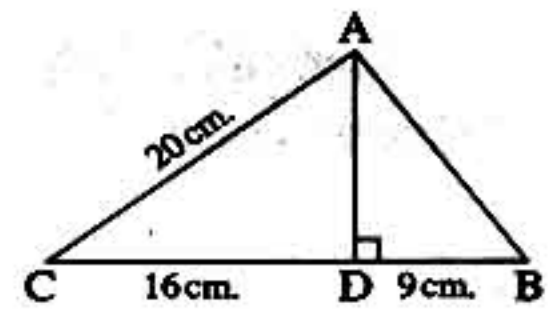
Unit 3

3 In the opposite figure :

$\overline{AD} \perp \overline{BC}$, $BD = 9$ cm. ,
 $DC = 16$ cm. and $AC = 20$ cm.

Find :

- AD
- The area of ΔABC
- AB



« 12 cm. , 15 cm. , 150 cm.² »

4 In the opposite figure :

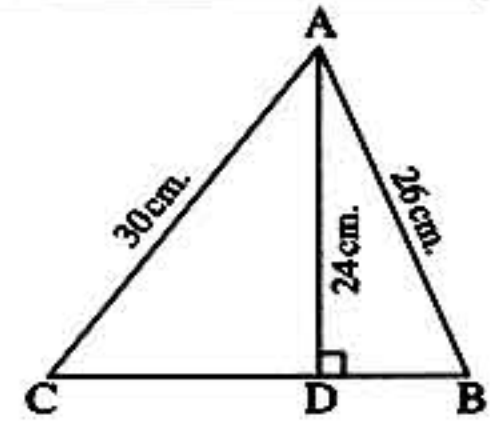
ABC is a triangle and $\overline{AD} \perp \overline{BC}$

If $AD = 24$ cm.

, $AB = 26$ cm.

and $AC = 30$ cm.

find BC and calculate the area of ΔABC



« 28 cm. , 336 cm.² »

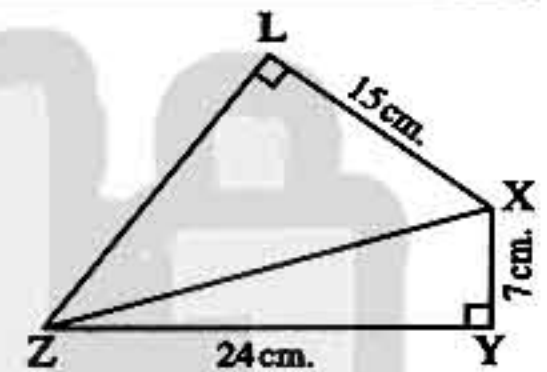
5 In the opposite figure :

XYZL is a quadrilateral in which :

$m(\angle XYZ) = m(\angle XLZ) = 90^\circ$,

$XY = 7$ cm. , $YZ = 24$ cm. and $XL = 15$ cm.

Find the length of each of : \overline{XZ} and \overline{ZL}



« 25 cm. , 20 cm. »

6 In the opposite figure :

$m(\angle B) = m(\angle ACD) = 90^\circ$

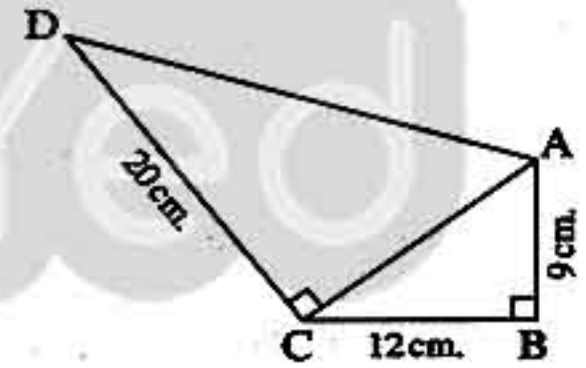
, $AB = 9$ cm. , $BC = 12$ cm.

and $DC = 20$ cm.

Find :

- The length of \overline{AC}
- The perimeter of the figure ABCD
- The length of \overline{AD}
- The area of the figure ABCD

« 15 cm. , 25 cm. , 66 cm. , 204 cm.² »



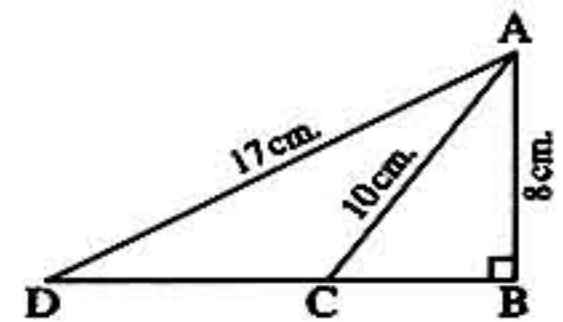
7 In the opposite figure :

ΔABD is a right-angled triangle at B

, $AB = 8$ cm. , $AD = 17$ cm.

and $C \in \overline{BD}$ such that $AC = 10$ cm.

Find the length of each of : \overline{CB} , \overline{BD} and \overline{CD}



« 6 cm. , 15 cm. , 9 cm. »

Lesson Seven

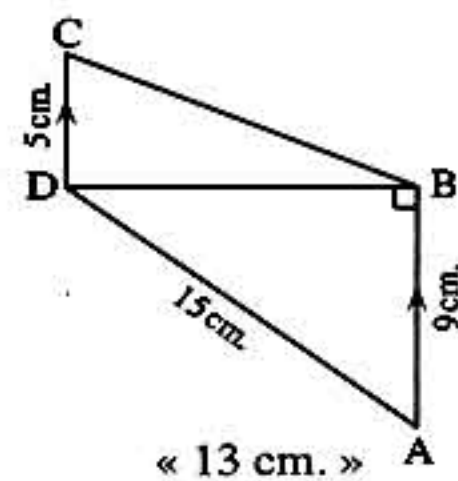
8 In the opposite figure :

$$m(\angle ABD) = 90^\circ, \overline{BA} \parallel \overline{CD}$$

$$, AB = 9 \text{ cm.}, AD = 15 \text{ cm.}$$

$$\text{and } DC = 5 \text{ cm.}$$

Calculate the length of : \overline{BC}



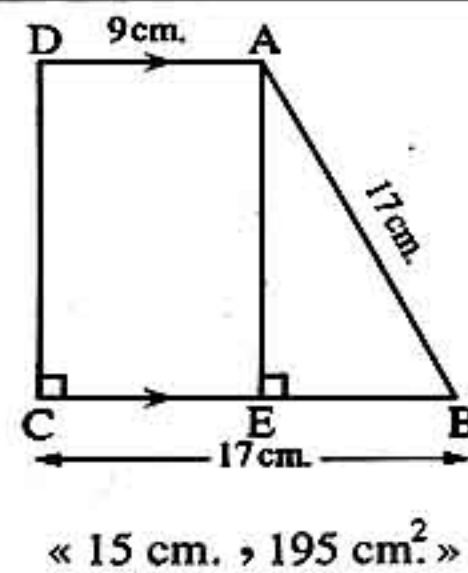
9 In the opposite figure :

ABCD is a trapezium, $\overline{AD} \parallel \overline{BC}$

$$, m(\angle DCB) = 90^\circ, \overline{AE} \perp \overline{BC}$$

$$\text{If : } AB = BC = 17 \text{ cm. and } AD = 9 \text{ cm.}$$

, find the length of \overline{DC} and calculate the area of the trapezium ABCD



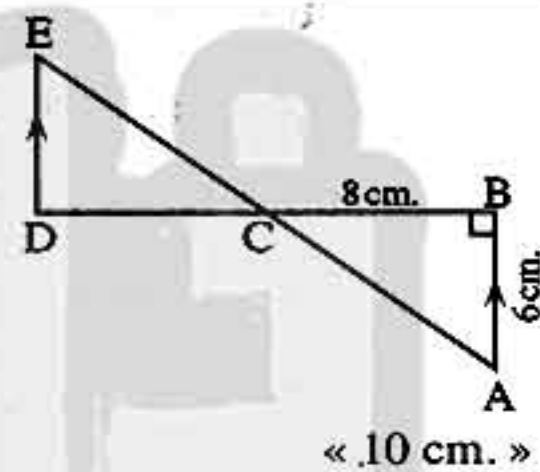
10 In the opposite figure :

$$\overline{BD} \cap \overline{AE} = \{C\}, \overline{AB} \parallel \overline{DE}$$

$$, AB = 6 \text{ cm.}, BC = 8 \text{ cm.}$$

and C is the midpoint of \overline{BD}

Calculate the length of : \overline{CE}



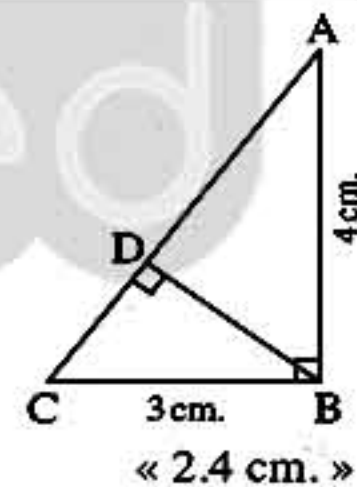
11 In the opposite figure :

ABC is a right-angled triangle at B

$$, \overline{BD} \perp \overline{AC}, AB = 4 \text{ cm.}$$

$$\text{and } BC = 3 \text{ cm.}$$

Calculate the length of : \overline{BD}



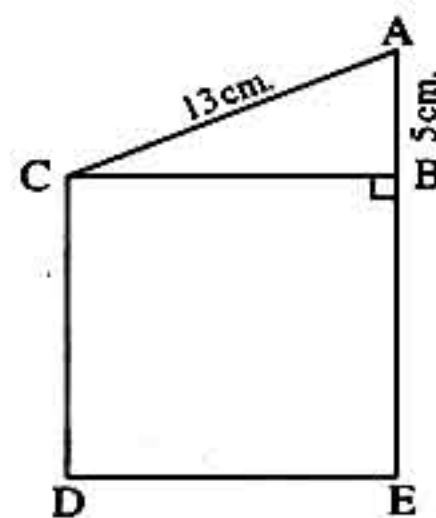
12 Complete the following :

- In the right-angled triangle , the area of the square on the hypotenuse equals
- If XYZ is a right-angled triangle at X , XY = 12 cm. and XZ = 9 cm. , then YZ = cm.
- If ABC is a right-angled triangle at B , AB = 20 cm. and AC = 25 cm. , then BC = cm.

Unit 3

4 In the opposite figure :

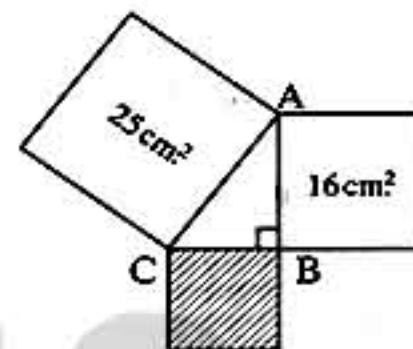
If $m(\angle ABC) = 90^\circ$
 , $AB = 5 \text{ cm}$.
 and $AC = 13 \text{ cm}$.
 , then the area of
 the square $BEDC = \dots\dots\dots \text{ cm}^2$



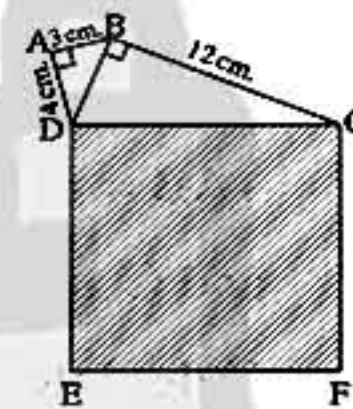
5 A rectangle is of length 8 cm. and width 6 cm. , then the length of its diagonal equals $\dots\dots\dots \text{ cm}$.

6 If the area of a rectangle equals 60 cm^2 and its width is 5 cm. , then the length of its diagonal = $\dots\dots\dots \text{ cm}$.

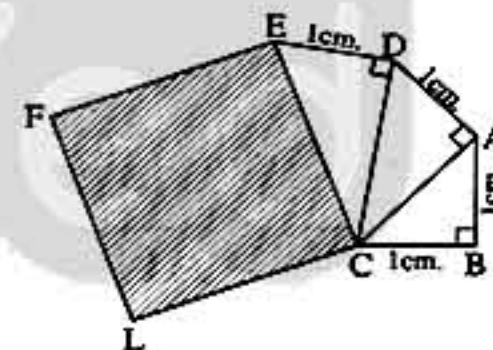
7 If $\triangle ABC$ is right-angled at B ,
 then the side length of the shaded square = $\dots\dots\dots \text{ cm}$.



8 If $\triangle ABD$ is right-angled at A
 and $\triangle BCD$ is right-angled at B ,
 then the area of the shaded square = $\dots\dots\dots \text{ cm}^2$



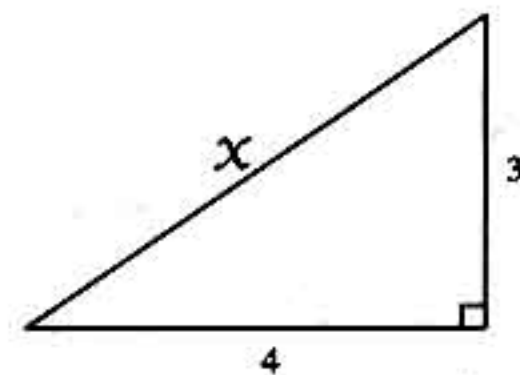
9 If each of the triangles ABC , ACD and DCE
 are right-angled at B , A and D respectively,
 $AB = BC = AD = DE = 1 \text{ cm}$.
 , then the area of the shaded square = $\dots\dots\dots \text{ cm}^2$



13 Choose the correct answer from those given :

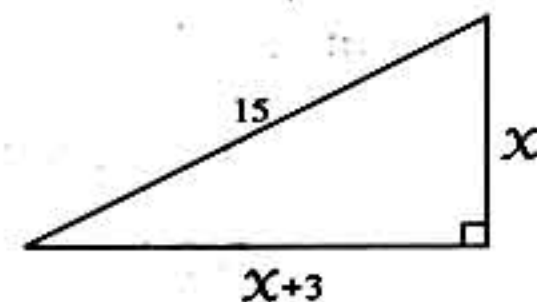
1 In the opposite figure :

Which of the following relations is true ?
 (a) $x = 4^2 + 3^2$ (b) $x^2 = 4^2 - 3^2$
 (c) $x^2 + 9 = 16$ (d) $x^2 = 25$



2 In the opposite figure :

Which of the following relations is true ?
 (a) $x + 3 + x = 15$ (b) $x^2 + 3x = 108$
 (c) $(x + 3)^2 = 15 - x^2$ (d) $x^2 + 6x + 9 = 225$

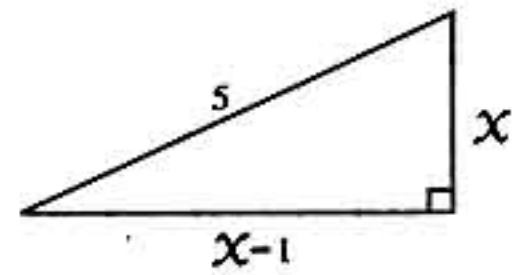


Lesson Seven

3 In the opposite figure :

Which of the following relations is true ?

- (a) $x^2 + (x-1)^2 = 5$ (b) $x + (x-1) = 25$
 (c) $x^2 - x = 12$ (d) $(x-1)^2 - x^2 = 25$



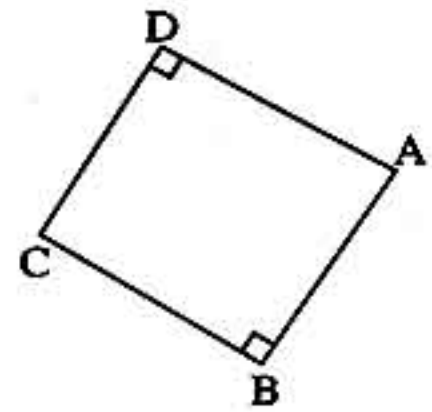
4 If ABCD is a square , then $(AC)^2 = \dots\dots\dots$

- (a) AB (b) $(AB)^2$ (c) $2(AB)^2$ (d) $4(AB)^2$

14 In the opposite figure :

If $m(\angle B) = m(\angle D) = 90^\circ$

Prove that : $(AB)^2 + (BC)^2 = (AD)^2 + (DC)^2$



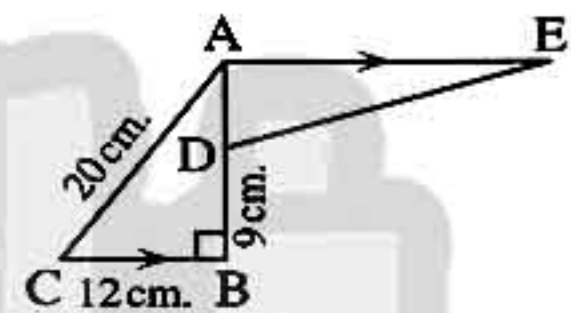
15 In the opposite figure :

ABC is a triangle , $m(\angle B) = 90^\circ$

, $\overline{AE} \parallel \overline{BC}$, If $BC = 12$ cm. , $AC = 20$ cm.

, $D \in \overline{AB}$ where $BD = 9$ cm. and $AE = 2 BC$

, find the length of each of : \overline{AD} and \overline{ED}



« 7 cm. , 25 cm. »



Life Applications

16 A window cleaner has a ladder which is 5 metres long.

He places it so that it reaches
a window sill 4 metres from the ground.

How far is the wall from the foot of the ladder ?



« 3 m. »

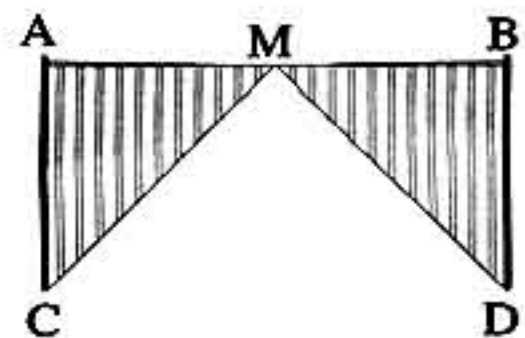
17 A wooden bridge \overline{AB} of length 15 m. is built

horizontally on two vertical walls \overline{AC} and \overline{BD}

resting on two supports \overline{MC} and \overline{MD}

If $AC = 4$ m. and $AM = MB$,

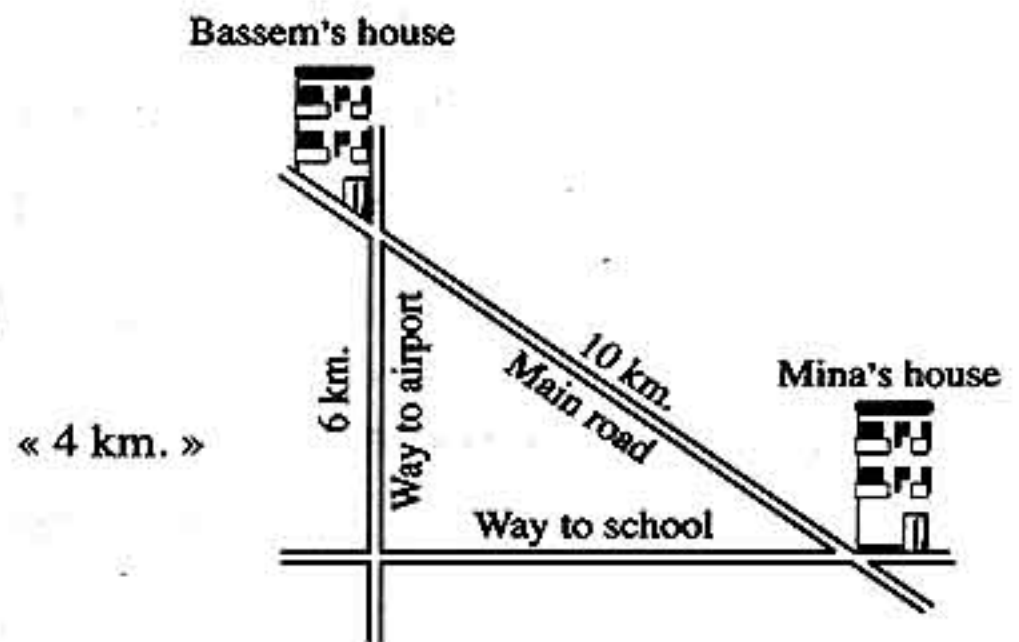
calculate the length of the support \overline{MC}



« 8.5 m. »

Unit 3

- 18 If Mina wants to go to the house of his friend Bassem.
- What is the distance he saves if he takes the main road instead of the other two roads ?



For excellent pupils

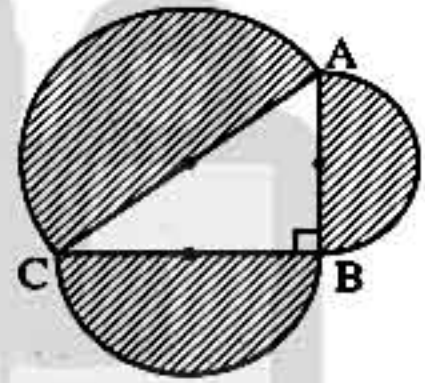
- 19 If ΔABC is right-angled at B , D is the midpoint of \overline{BC} ,

Prove that : $(AC)^2 - (AD)^2 = 3 (BD)^2$

- 20 In the opposite figure :

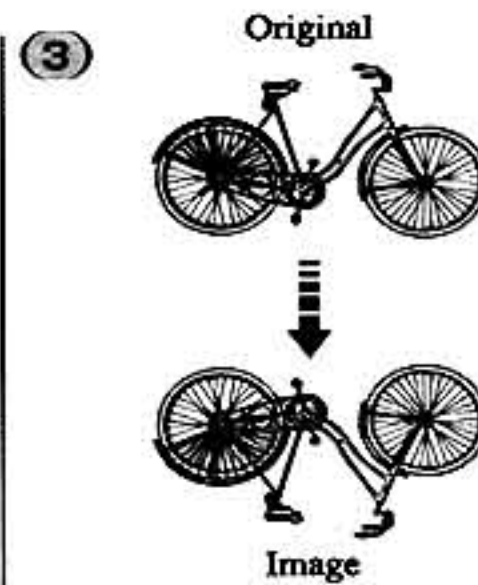
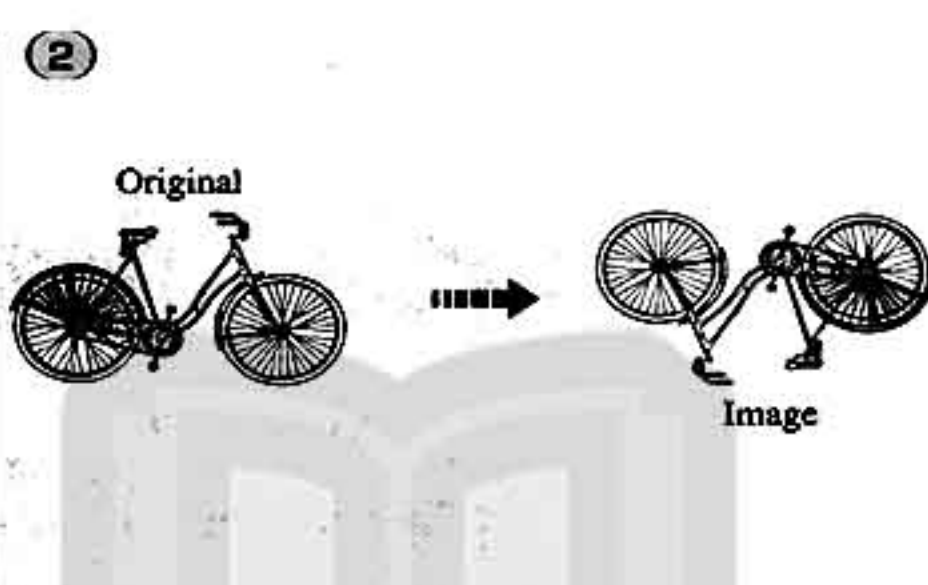
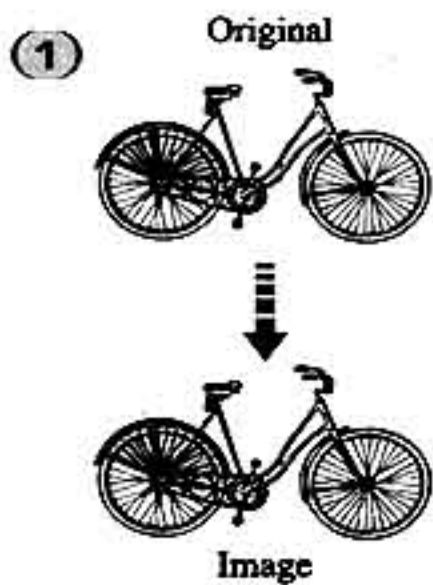
Prove that the sum of areas of the two semicircles drawn on the two sides of the right angle in a right-angled triangle equals the area of the semicircle drawn on the hypotenuse?

[Given the area of the circle = πr^2]

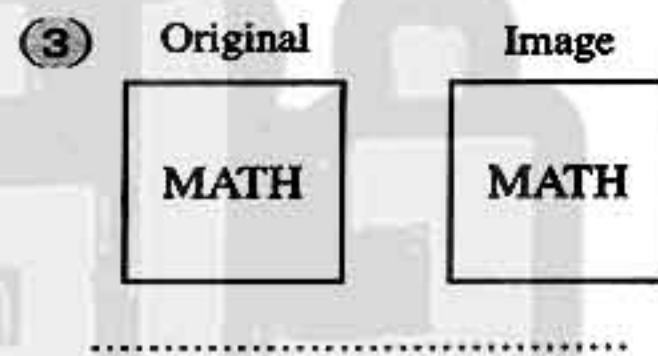
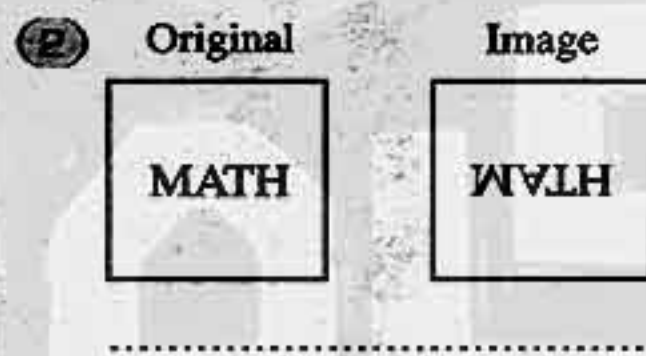
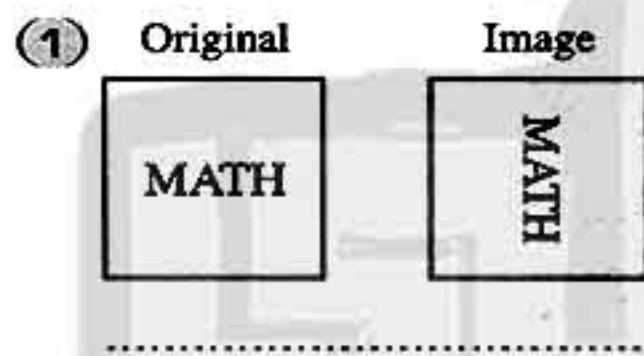


Exercise 8 On geometric transformations

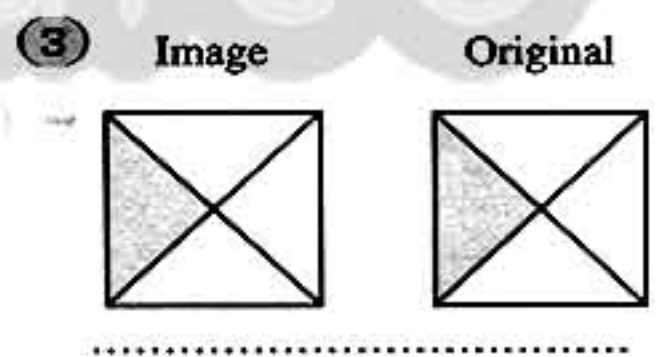
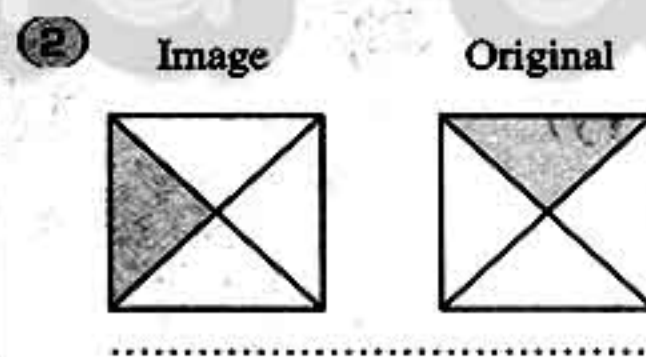
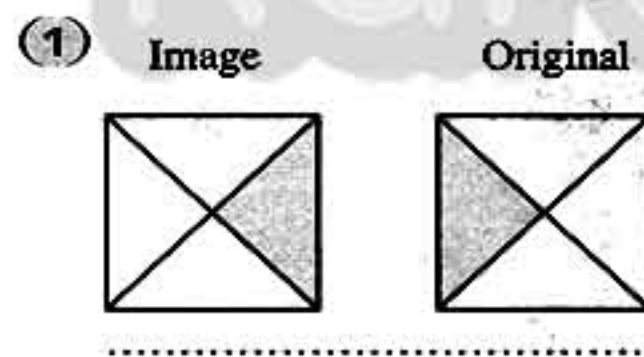
1 Describe the type of the geometric transformation (reflection, translation or rotation) in each of the following :



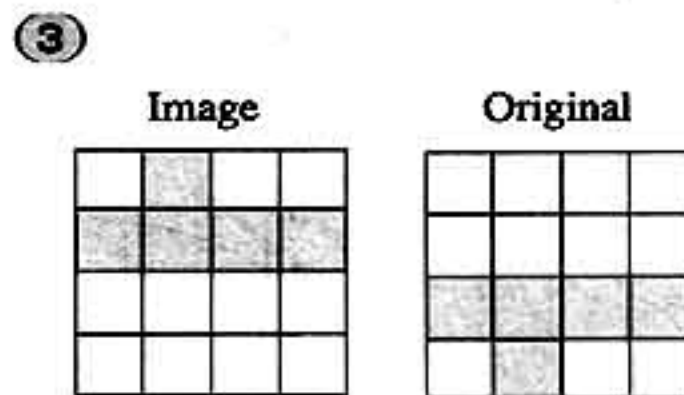
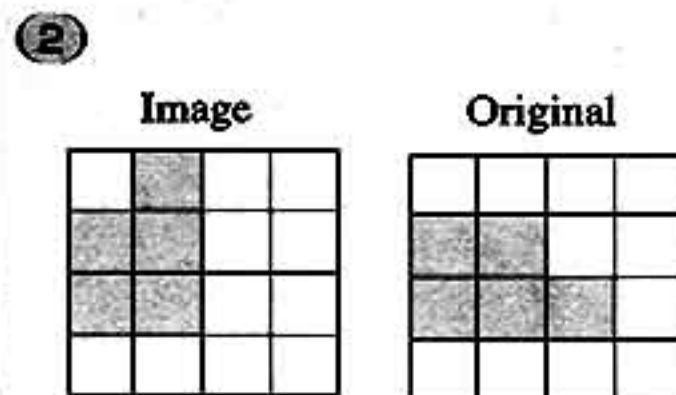
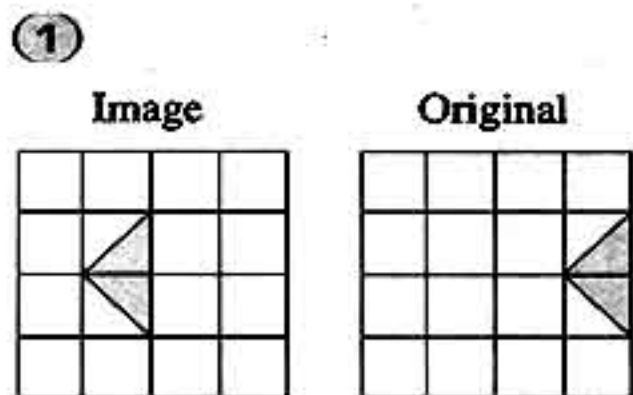
2 Write below each shape the type of the geometric transformation (reflection, translation or rotation) :



3 Write below each shape the type of the geometric transformation (reflection, translation or rotation) :

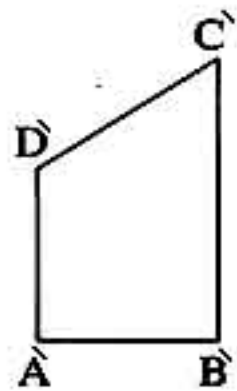
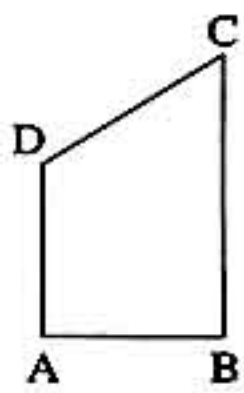


4 Write the type of the geometric transformation in each of the following shapes :

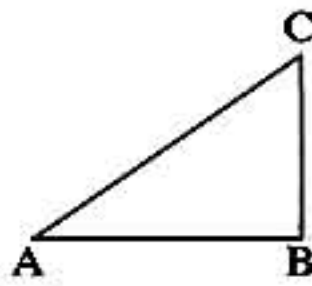
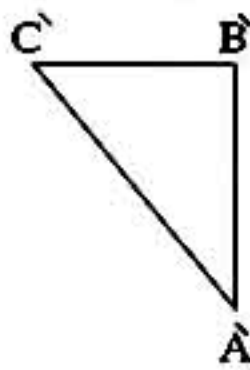


Unit 3

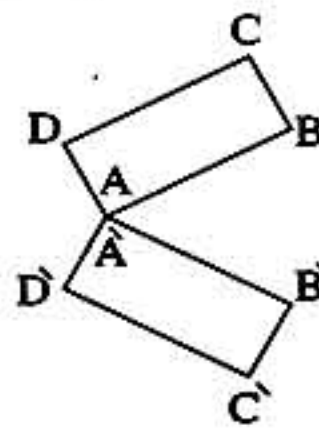
5 Describe the type of transformation in each of the following figures (reflection , translation , rotation) :



(1)

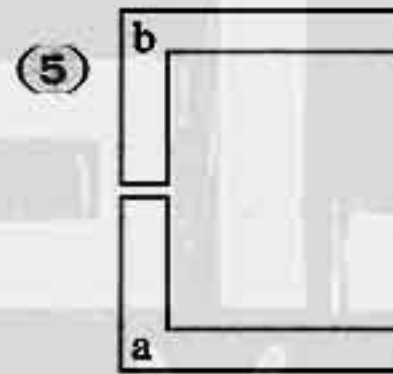
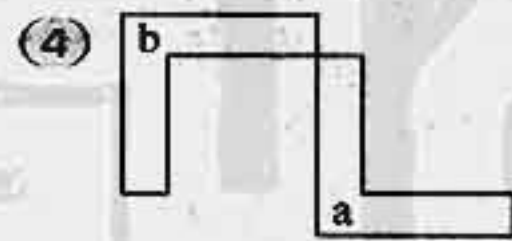
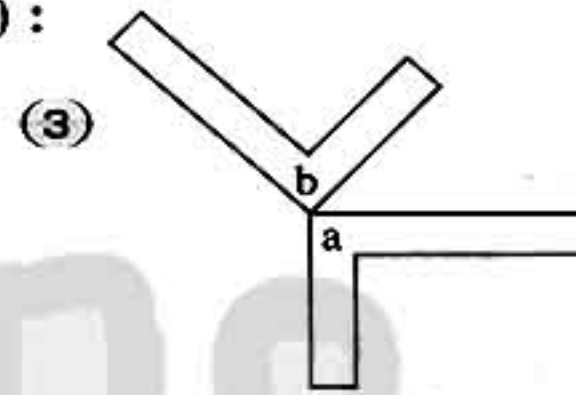
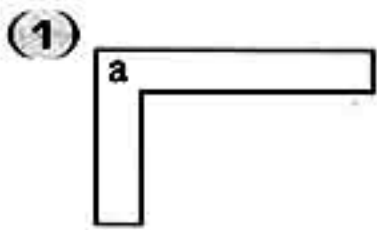


(2)



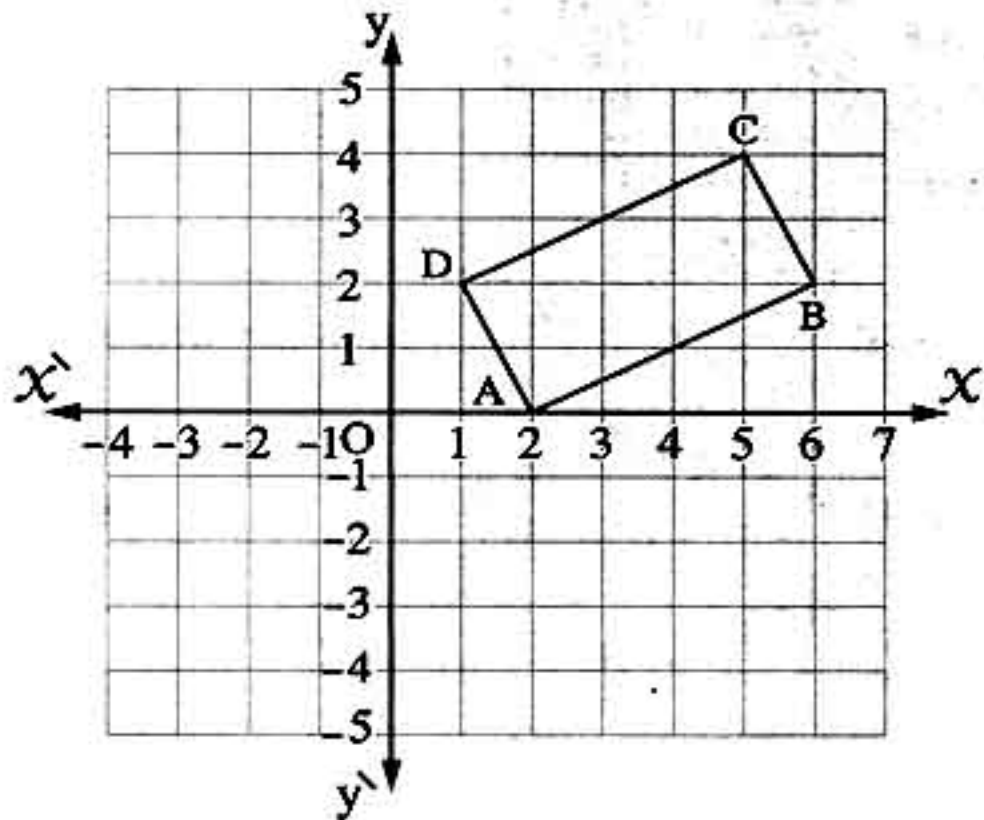
(3)

6 Figure b is the image of figure a by a geometric transformation. Identify each transformation as (a translation , a reflection or a rotation) :

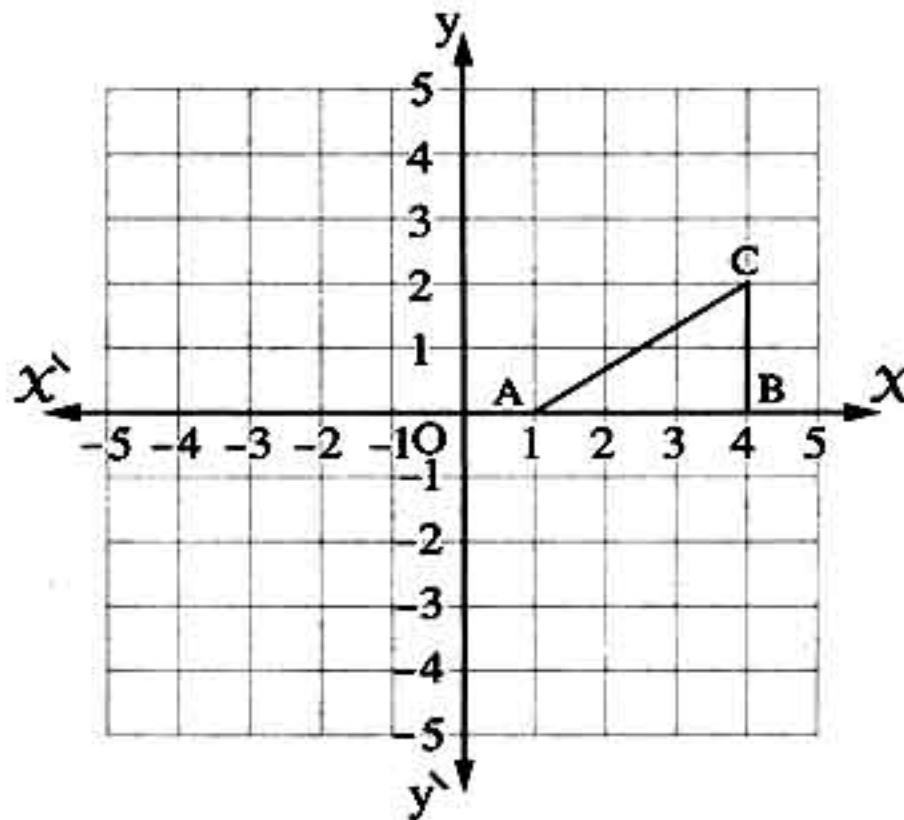


7 Draw the image of each figure according to the shown transformation , then describe each type :

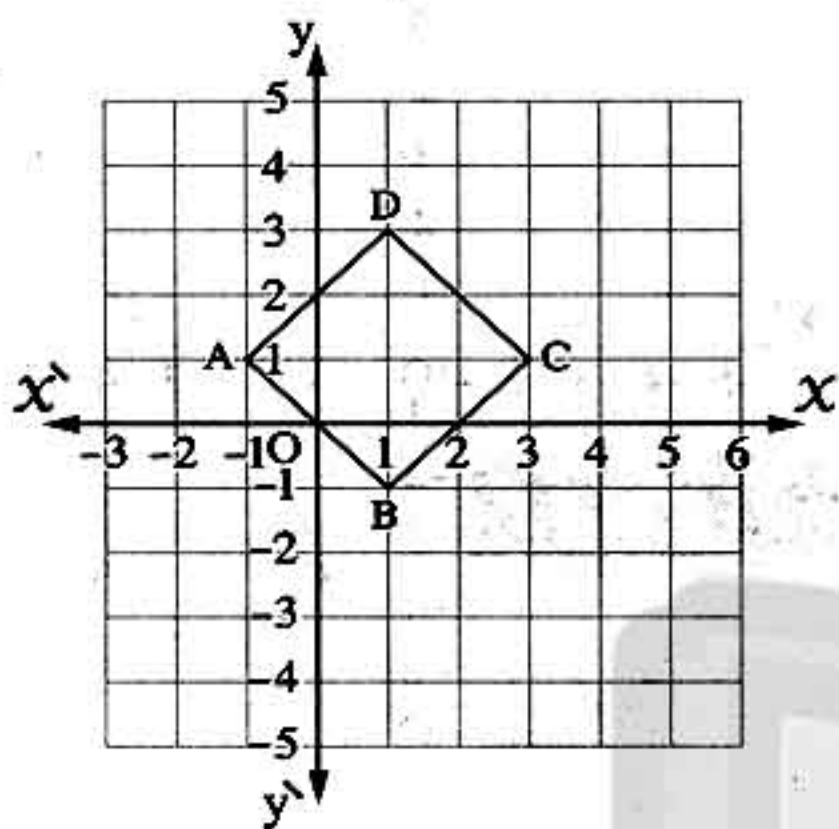
(1) $(x, y) \rightarrow (-x, y)$



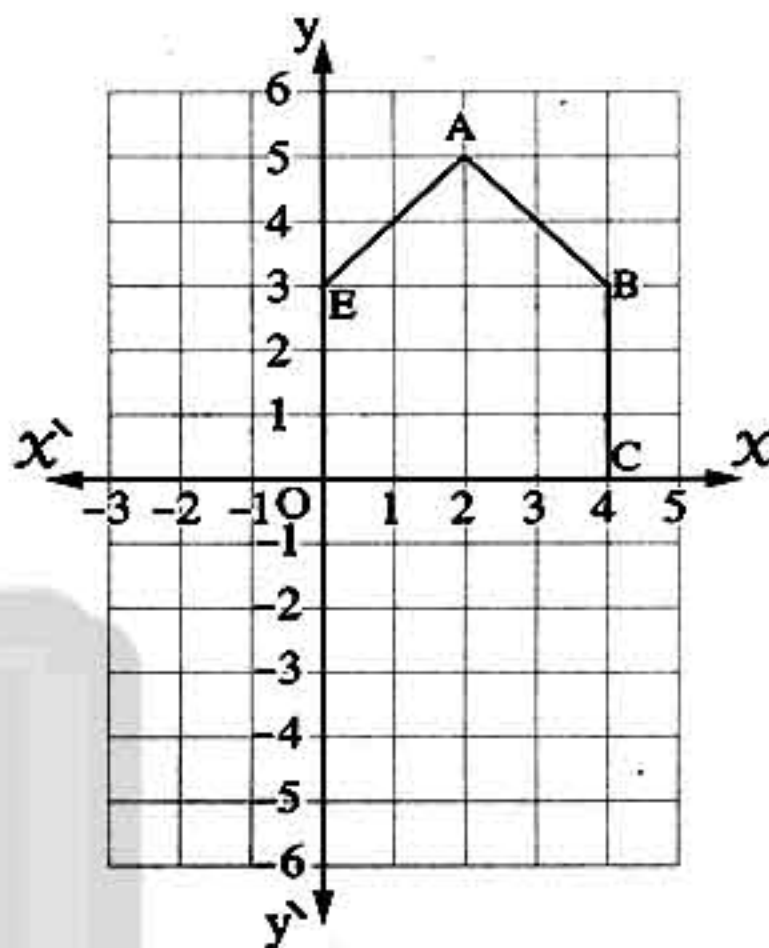
(2) $(x, y) \rightarrow (-x, -y)$



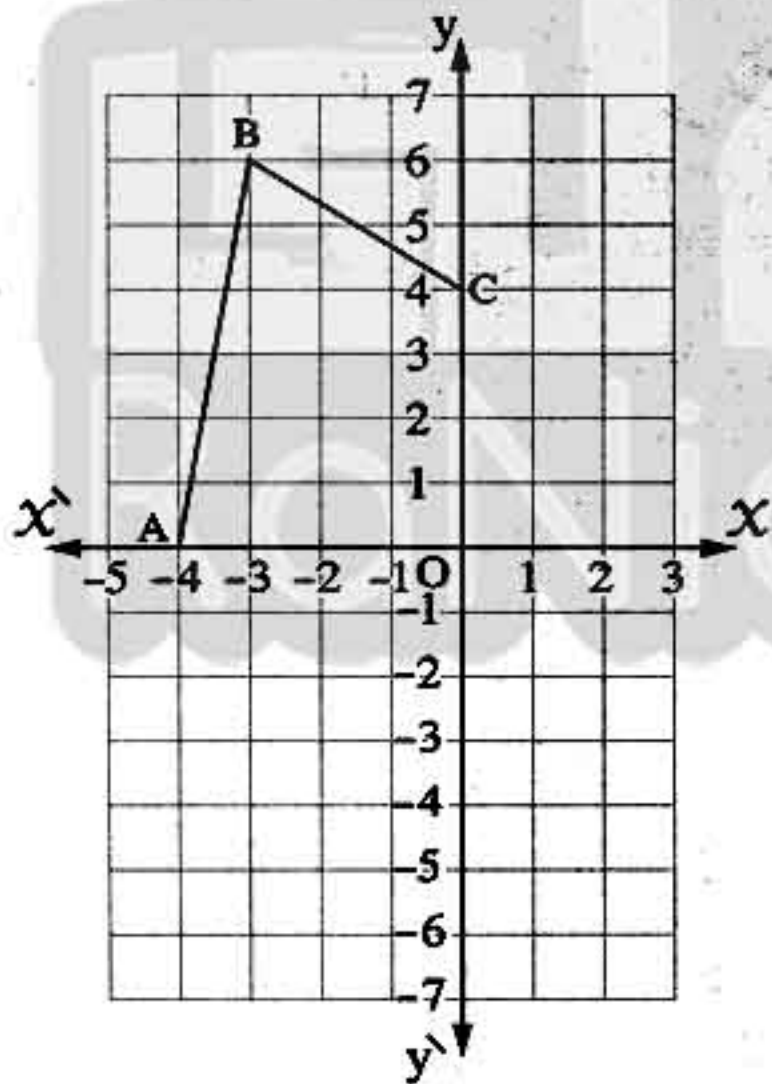
③ $(x, y) \rightarrow (x+2, y+3)$



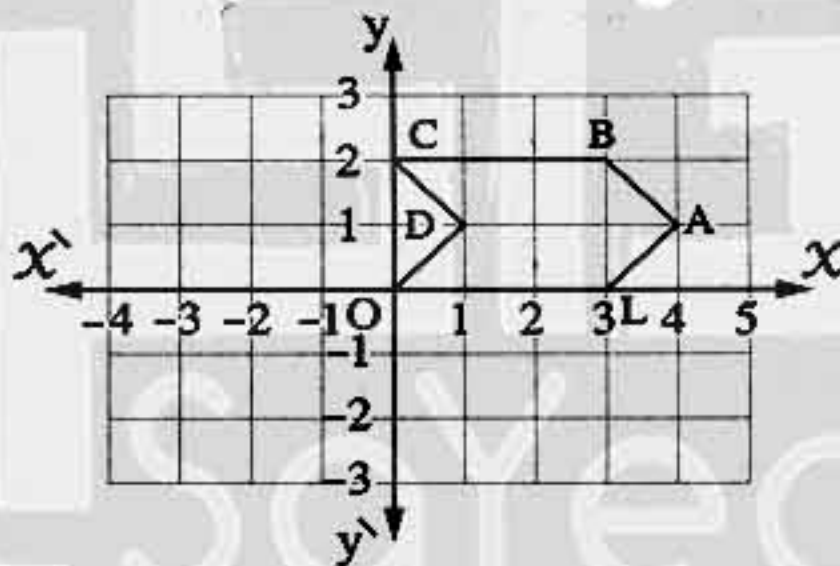
④ $(x, y) \rightarrow (x, y-3)$



⑤ $(x, y) \rightarrow (y, -x)$



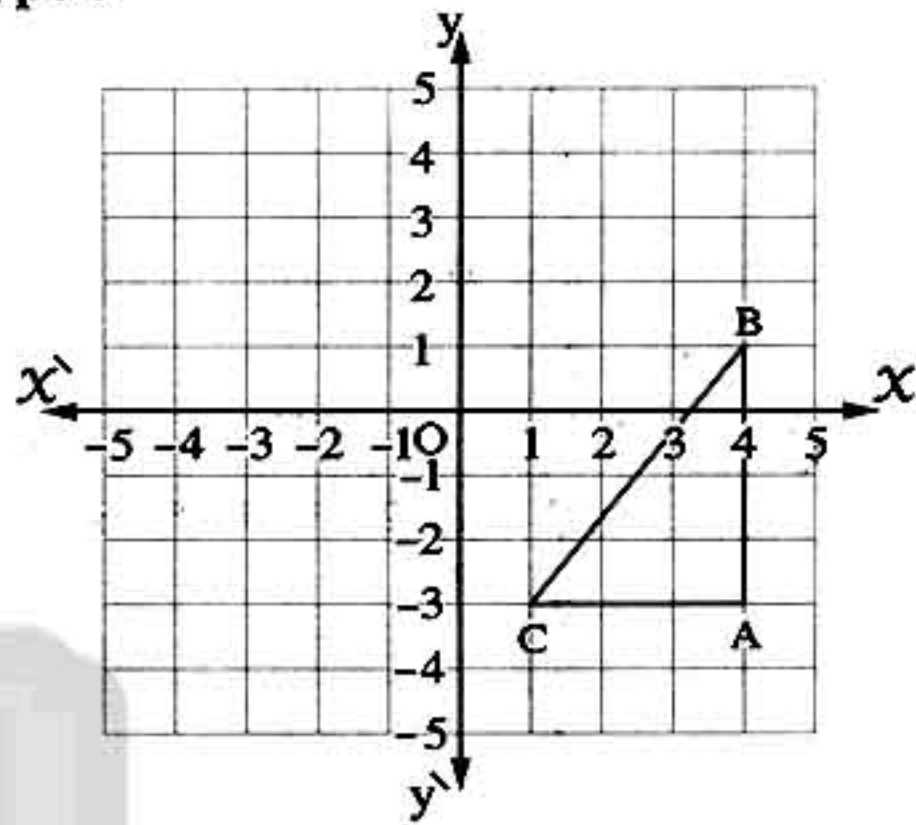
⑥ $(x, y) \rightarrow (-x, y)$



Unit 3

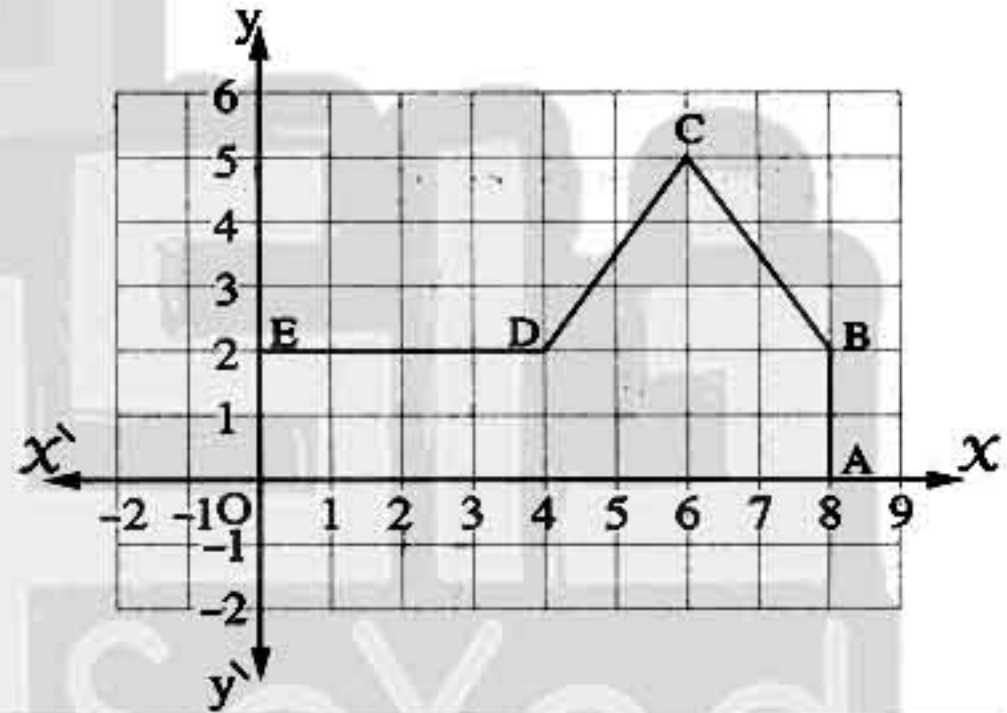
- 8 Map the image of ΔABC where $A(4, -3)$, $B(4, 1)$, $C(1, -3)$ according to the following transformations then describe its type :

- (1) $(x, y) \longrightarrow (-x, y)$
- (2) $(x, y) \longrightarrow (-x, -y)$
- (3) $(x, y) \longrightarrow (x, y - 2)$
- (4) $(x, y) \longrightarrow (-y, x)$



- 9 Draw the image of the polygon ABCDEO according to each transformation and describe the type :

- (1) $(x, y) \longrightarrow (-x, y)$
- (2) $(x, y) \longrightarrow (x, y + 5)$
- (3) $(x, y) \longrightarrow (-x, -y)$
- (4) $(x, y) \longrightarrow (x - 5, y)$
- (5) $(x, y) \longrightarrow (x, -y)$



- 10 Draw the image of ΔABC where $A(1, 2)$, $B(3, 2)$ and $C(3, 5)$ by the following transformations :

- (1) $(x, y) \longrightarrow (x, -y)$
- (2) $(x, y) \longrightarrow (x + 1, y - 3)$
- (3) $(x, y) \longrightarrow (-y, x)$

- 11 On a square lattice, draw ΔABO where $A(3, 1)$, $B(1, 3)$ and O is the origin point, and draw its images by the following transformations then describe its type :

- (1) $(x, y) \longrightarrow (x + 1, y - 2)$
- (2) $(x, y) \longrightarrow (x, -y)$

$$(3) (x, y) \longrightarrow (-y, x)$$

$$(4) (x, y) \longrightarrow (-x, -y)$$

- 12 On a square lattice, draw the quadrilateral ABCD where A (1, 1), B (4, 2), C (3, 4) and D (1, 4), and draw its image by the following transformation, then describe its type :

$$(1) (x, y) \longrightarrow (y, -x)$$

$$(2) (x, y) \longrightarrow (-x, y)$$

$$(3) (x, y) \longrightarrow (x-1, y+1)$$



For excellent pupils

- 13 Draw ΔABC whose image $\Delta \hat{A} \hat{B} \hat{C}$ by the transformation $(x, y) \longrightarrow (-y, x)$ where \hat{A} (1, -1), \hat{B} (3, 1) and \hat{C} (4, -1), then describe the transformation type.

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Unit 3

From the school book

Exercise 9

On reflection in a straight line

First

Problems on reflection in the plane :

- 1 Find the image of each of A , \overline{AB} and $\triangle ABC$ by reflection in the straight line L :

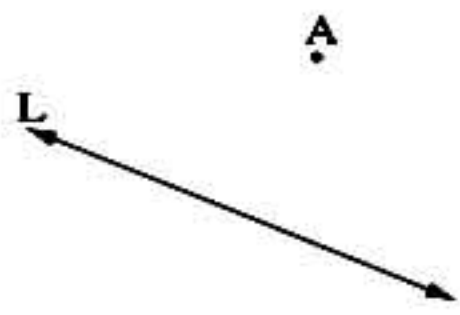


fig. (1)

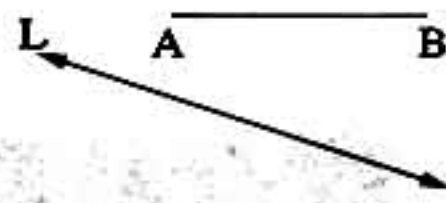


fig. (2)

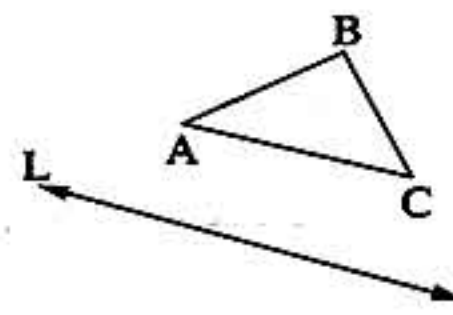
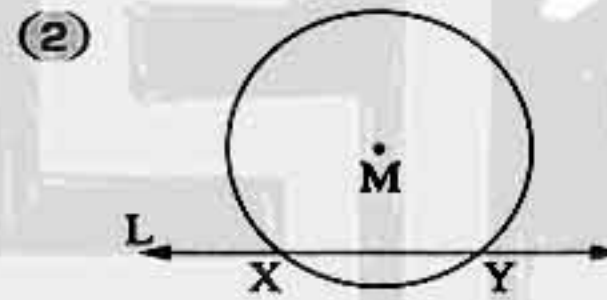
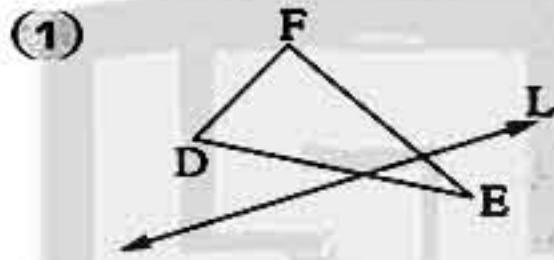
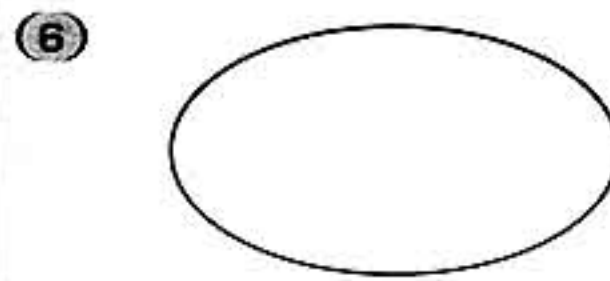
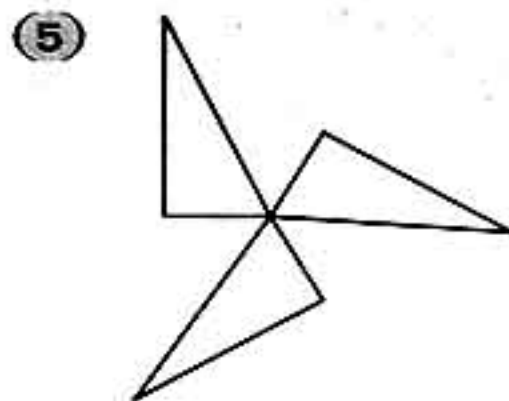
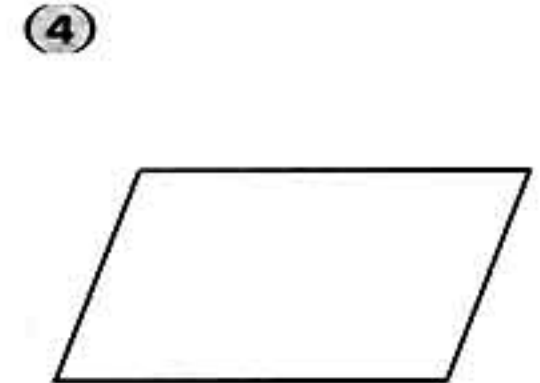
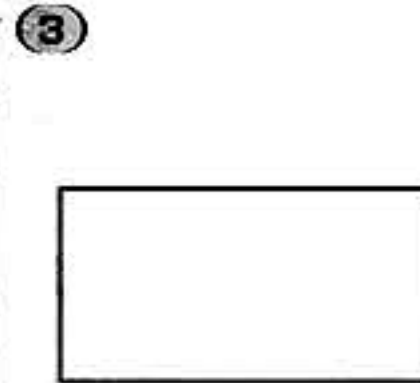
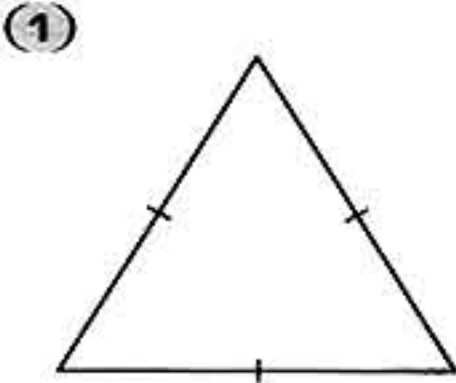


fig. (3)

- 2 Copy the figures below in your notebook, then draw the images of $\triangle DEF$ and the circle M by reflection in L :



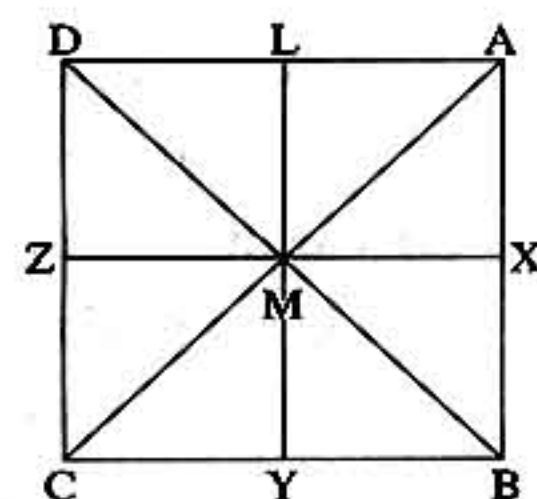
- 3 Draw the axes of symmetry of each of the following figures if they are existed :



- 4 Draw the triangle ABC in which : $AB = 6$ cm. , $m(\angle A) = 90^\circ$ and $m(\angle B) = 30^\circ$
Then draw its image by reflection in \overleftrightarrow{AB}
- 5 Draw the image of ΔABC in which : $AB = 3$ cm. , $BC = 4$ cm. and $AC = 5$ cm.
by reflection in the straight line containing the shortest side.
- 6 Draw the image of ΔXYZ in which : $XY = 3$ cm. , $YZ = 5$ cm. and $ZX = 7$ cm.
by reflection in the straight line containing the longest side.
- 7 Draw ΔABC in which : $AB = 3$ cm. , $BC = 6$ cm. and $m(\angle ABC) = 90^\circ$, then find
its image by reflection in the straight line L which is perpendicular to \overline{BC} at C
- 8 Draw the rectangle ABCD in which : $AB = 6$ cm. and $CB = 4$ cm. , then draw its image
by reflection in \overleftrightarrow{AD} . Say the name of the resulting figure which consists of the
rectangle and its image , then find its perimeter. « 32 cm. »
- 9 Draw the image of the circle M whose radius length is 2 cm. , by reflection in the
straight line which is far from the centre by 1 cm.
- 10 Draw the circle N with radius length 2.5 cm. , then draw its image by reflection in the
straight line which is far from its centre by 2.5 cm.
- 11 Draw ΔABC where $BC = 3$ cm. , $AB = 4$ cm. and $AC = 5$ cm.
If the point D is the image of the point C by reflection in \overleftrightarrow{AB}
Find :
(1) The perimeter of ΔACD
(2) The area of ΔACD « 16 cm. , 12 cm² »
- 12 In the opposite figure :

ABCD is a square. M is the point of intersection of its diagonals
 \overline{X} , \overline{Y} , \overline{Z} and \overline{L} are the midpoints of its sides \overline{AB} , \overline{BC} ,
 \overline{CD} and \overline{DA} respectively. Complete the following :

- (1) The image of the point A by reflection in \overleftrightarrow{LY} is
- (2) The image of the \overline{AM} by reflection in \overleftrightarrow{XM} is
- (3) The image of the ΔALM by reflection in \overleftrightarrow{LY} is
- (4) The image of the ΔALM by reflection in \overleftrightarrow{XZ} is
- (5) The image of the ΔALM by reflection in \overleftrightarrow{AM} is



Unit 3

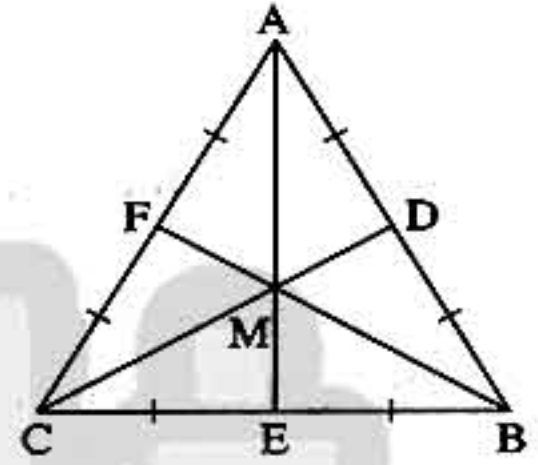
- (6) The image of the ΔAMB by reflection in \overleftrightarrow{LY} is
- (7) The image of the ΔAMB by reflection in \overleftrightarrow{XZ} is
- (8) The image of the square $AXML$ by reflection in \overleftrightarrow{LY} is
and by reflection in \overleftrightarrow{AM} is
- (9) The image of the square $ABCD$ by reflection in \overleftrightarrow{LY} is
- (10) ΔMZD is the image of ΔMZC by reflection in
- (11) ΔAXM is the image of ΔCYM by reflection in

13 In the opposite figure :

ΔABC is an equilateral triangle, where D , E and F are the midpoints of \overline{AB} , \overline{BC} and \overline{AC} respectively, and $\overline{AE} \cap \overline{BF} \cap \overline{CD} = \{M\}$:

Complete :

- (1) Axes of symmetry of ΔABC are
- (2) \overline{AB} is the reflected image of \overline{AC} by reflection in
- (3) The reflected image of \overline{AF} by reflection in \overleftrightarrow{BF} is,
and the reflected image of \overline{CF} in \overleftrightarrow{AE} is
- (4) The reflected image of ΔAMD by reflection in \overleftrightarrow{AE} is
 $\therefore m(\angle AMD) = m(\angle \dots)$, because reflection in a line reserves
- (5) The reflected image of ΔAMB by reflection in \overleftrightarrow{AE} is
- (6) ΔBMC is the reflected image of by reflection in \overleftrightarrow{CD} , and the reflected image of by reflection in \overleftrightarrow{BF}
 $\therefore BM = AM$, and $CM = AM$, because the reflection reserves



14 Complete the following :

- (1) The reflection in a plane reserves :
- (a) (b) (c) (d)
- (2) If the reflection in a straight line transforms the figure to itself then this straight line is called
- (3) The number of axes of symmetry of :
- | | |
|---------------------------------------|---|
| (a) The equilateral triangle is | (b) The isosceles triangle is |
| (c) The scalene triangle is | (d) The parallelogram is |
| (e) The rectangle is | (f) The rhombus is |
| (g) The square is | (h) The trapezium which is not isosceles is |
| (i) The isosceles trapezium | (j) The circle |

Lesson Nine

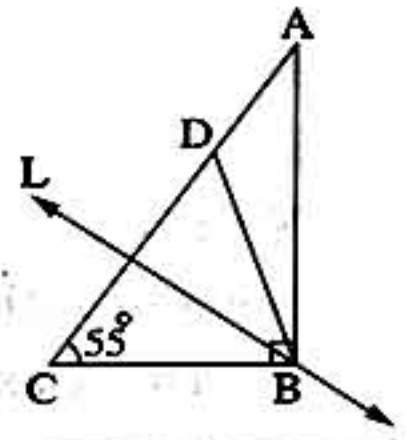
(4) In the opposite figure :

If $m(\angle ABC) = 90^\circ$

and $m(\angle C) = 55^\circ$, the straight line L

is the axis of symmetry of $\triangle DBC$

, then $m(\angle ABD) = \dots\dots\dots^\circ$

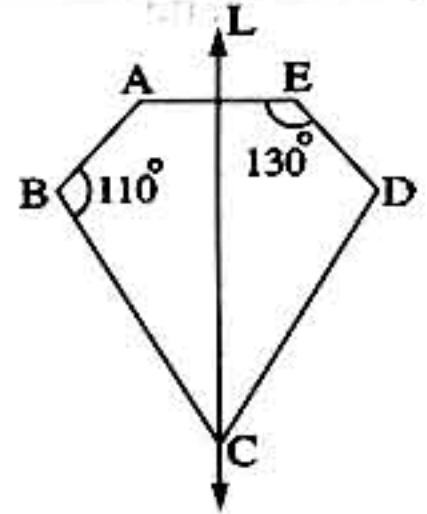


(15) In the opposite figure :

If the straight line L

is the axis of symmetry of the figure ABCDE,

calculate : $m(\angle BCD)$



« 60° »

(16) By using geometric instruments, draw the rectangle ABCD, where $AB = 3$ cm. and $BC = 4$ cm. locate \hat{A} as the reflected image of A by reflection in \overline{CD} and locate \hat{C} as the reflected image of C by reflection in \overline{AB}

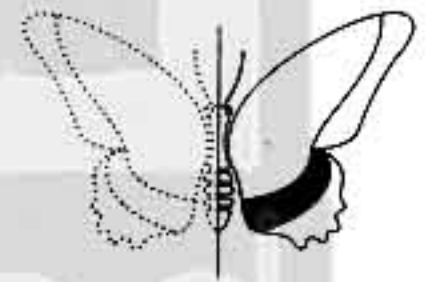
Prove that :

(1) $m(\angle \hat{C}AC) = 2 m(\angle CAB)$

(2) $\overline{AC} \parallel \overline{\hat{A}\hat{C}}$

Life Applications

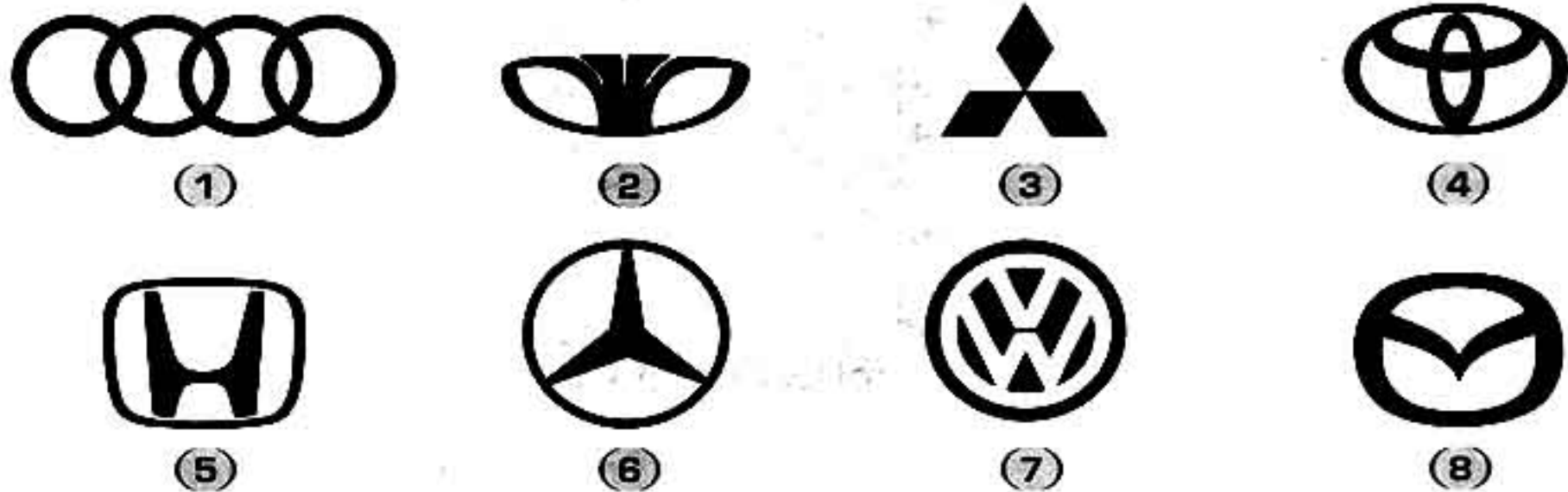
(17) By using the reflection we can complete drawing some of the symmetrical shapes like the butterfly in the opposite figure.



Use the reflection to complete each of the following figures :



(18) In our daily life, we see many figures having one or more axes of symmetry in front of you, there are some signs of cars. Draw their axes of symmetry if they exist :



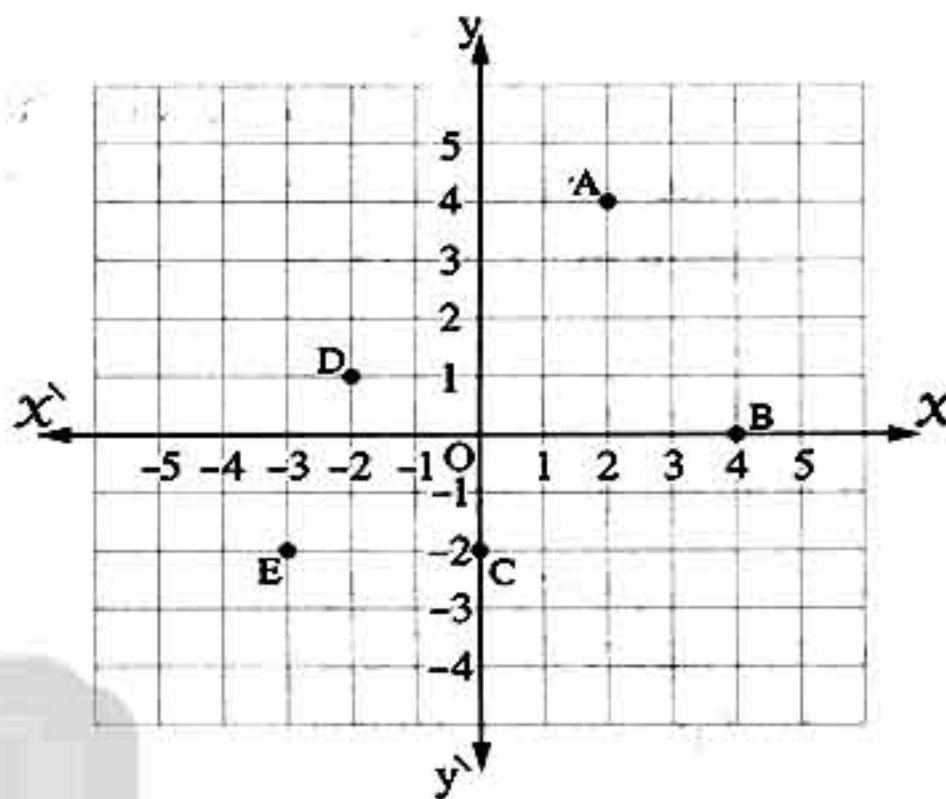
Unit 3

Second Problems on reflection in the Cartesian plane :

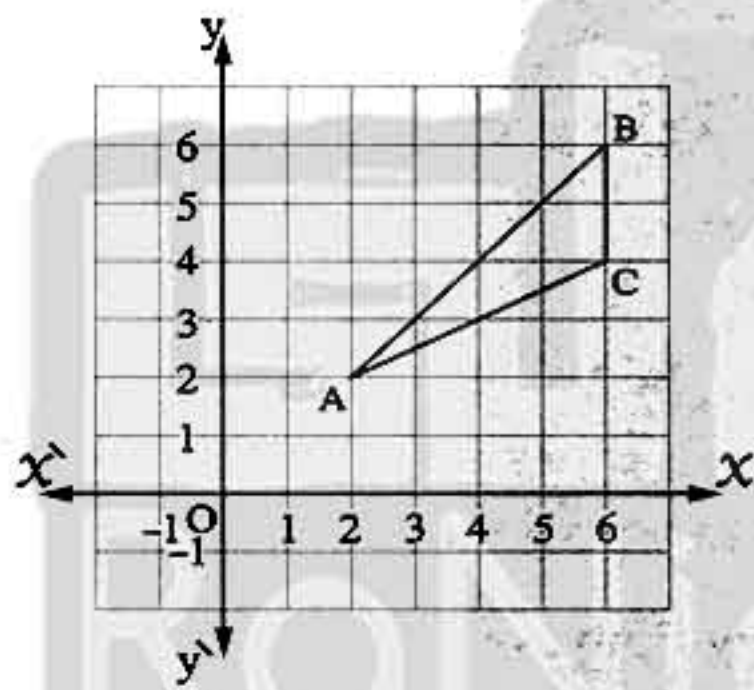
1 In the opposite figure :

Write the coordinates of the image of each point by reflection in :

- (1) The x -axis
- (2) The y -axis

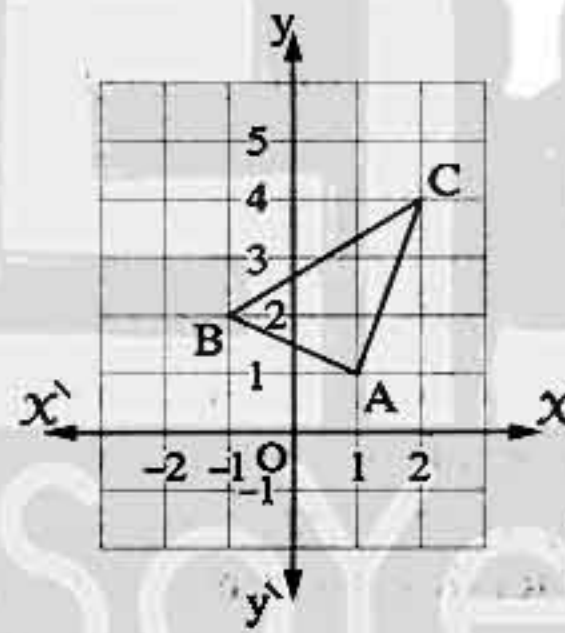


2 Copy each of the following figures on a lattice and draw the images of the figure by a geometric transformation as shown below each figure , then write the coordinates of each vertex of the figure.



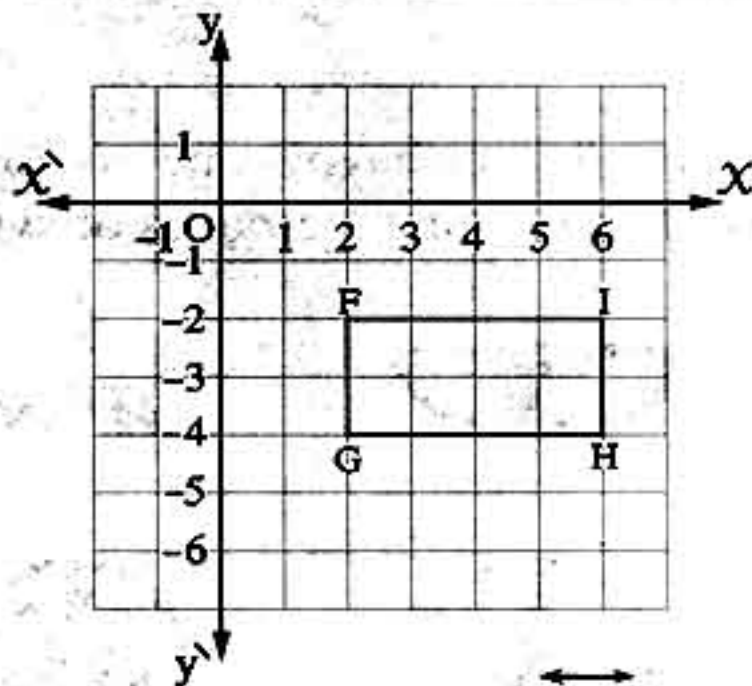
reflection in the x -axis

fig. (1)



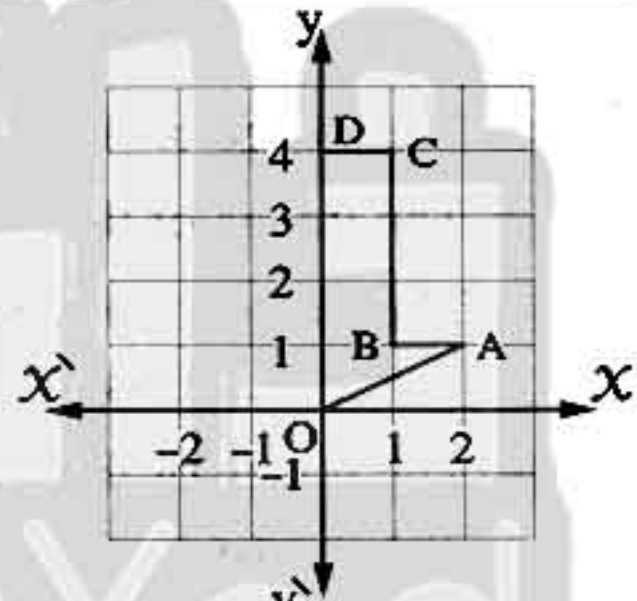
reflection in the y -axis

fig. (2)



reflection in \overrightarrow{FG}

fig. (3)

- 3 Draw \overline{AB} where A (4 , 3) and B (1 , - 2) , then draw its image by reflection in :
- (1) The x -axis (2) The y -axis
- 4 If A (3 , 1) and B (3 , - 2) , find \overline{DC} which is the image of \overline{AB} by reflection in the y -axis and name the figure ABCD and calculate its perimeter. « 18 length units »
- 5 Find the image of ΔABC where A (- 6 , - 1) , B (- 2 , - 1) and C (- 5 , - 6) by reflection in the x -axis
- 6 Draw the image of ΔABC where A (0 , 0) , B (3 , 0) and C (- 1 , 2) by reflection in the y -axis
- 7 On a square lattice , draw ΔABC where A (2 , - 2) , B (3 , 4) and C (- 3 , 2) then draw $\Delta \hat{A}\hat{B}\hat{C}$ which is the image of ΔABC by reflection in the y -axis then draw $\Delta \hat{\hat{A}}\hat{\hat{B}}\hat{\hat{C}}$ which is the image of $\Delta \hat{A}\hat{B}\hat{C}$ by reflection in the x -axis
- 8 Draw the image of the opposite figure by reflection in the x -axis and in the y -axis another time.
- 
- 9 On a square lattice , draw the rectangle whose vertices are A (3 , 2) , B (8 , 2) , C (8 , 6) and D (3 , 6) , then draw its image by reflection in the y -axis
- 10 Graph the square ABCD and its image : by reflection in the x -axis , then compare the length of the sides and the area where A (0 , 2) , B (- 5 , 0) , C (- 3 , - 5) and D (2 , - 3)
- 11 ABCD is a rectangle in which : A (1 , 1) , B (1 , 3) and C (- 3 , 3) Determine the coordinates of D from the graph , then find the image of the rectangle ABCD by reflection in the x -axis.
- 12 Draw the image of the square ABCD where A (2 , 3) and B (2 , - 1) by reflection in the y -axis. What do you notice ?
- 13 Draw the image of the rectangle XYZL where X (2 , 2) and Y (- 3 , 2) with width 3 units by reflection in the x -axis.

Unit 3

14 Complete the following table :

No.	The point	Its image by reflection in the X-axis	Its image by reflection in the y-axis
1	(3 , -2)
2	(1 , 2)
3	(-2 , 4)
4	(0 , 5)
5	(3 , 0)
6	(0 , 0)

15 Complete the following :

- (1) The image of the point (1 , 3) by reflection in the X-axis is
- (2) The image of the point (-2 , 5) by reflection in the y-axis
- (3) The image of the point (2 , -3) by reflection in the is (2 , 3)
- (4) The image of the point (-1 , -4) by reflection in the is (1 , -4)
- (5) The image of the point (0 , 3) by reflection in the is itself.
- (6) The image of the point (-5 , 0) by reflection in the is itself.
- (7) The image of the point (2 , 1) by reflection in the X-axis followed by reflection in the y-axis is
- (8) The image of the point (2 , -3) by reflection in the y-axis followed by reflection in the X-axis is
- (9) If \hat{A} (-2 , 3) is the image of the point A (2 , 3) by reflection in y-axis , then the image of the point \hat{A} by reflection in the y-axis is



For excellent pupils

16 Determine on a square lattice the points A (5 , 4) , B (5 , 1) , C (2 , 1) , \hat{A} (4 , 5) , \hat{B} (1 , 5) and \hat{C} (1 , 2)

- (1) If $\Delta \hat{A}\hat{B}\hat{C}$ is the image of ΔABC by reflection in the straight line L , draw this straight line.
- (2) If the figure $ABB\hat{A}$ is the image of the figure $CBB\hat{C}$ by reflection in the straight line M , draw this straight line.

17 If the geometric transformation $(x , y) \longrightarrow (y , x)$ is a reflection in a straight line L , draw on a square lattice the straight line L

Exercise 10

On reflection in a point

First

Problems on reflection in the plane :

1 Choose the correct answer from the given ones :

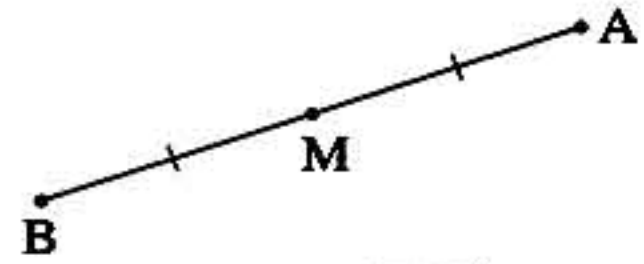
(1) If $\overline{A'B'}$ is the image of \overline{AB} by reflection in M , then $A'B' \dots\dots AB$

- (a) $>$ (b) $<$ (c) $=$ (d) \neq

(2) In the opposite figure :

The image of \overline{AB}
by reflection in the point M is

- (a) \overline{AM} (b) \overline{AB} (c) \overline{BA}

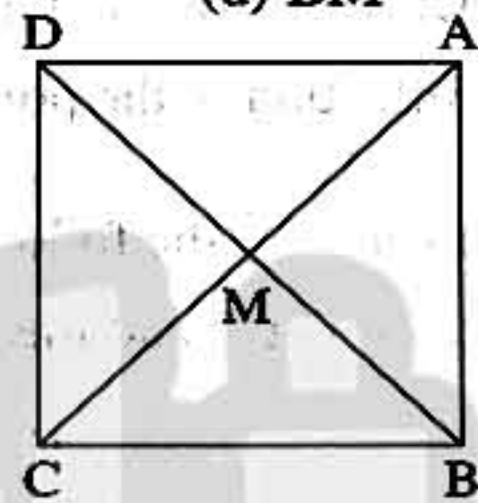


- (d) \overline{BM}

(3) In the opposite figure :

ABCD is a square whose diagonals intersect at M . The image of $\triangle ABM$ by reflection in M is $\triangle \dots\dots$

- (a) $\triangle ADM$ (b) $\triangle BCM$
(c) $\triangle DCM$ (d) $\triangle CDM$



(4) If A' is the image of A by reflection in M and if $MA = 5$ cm., then $AA' = \dots\dots$

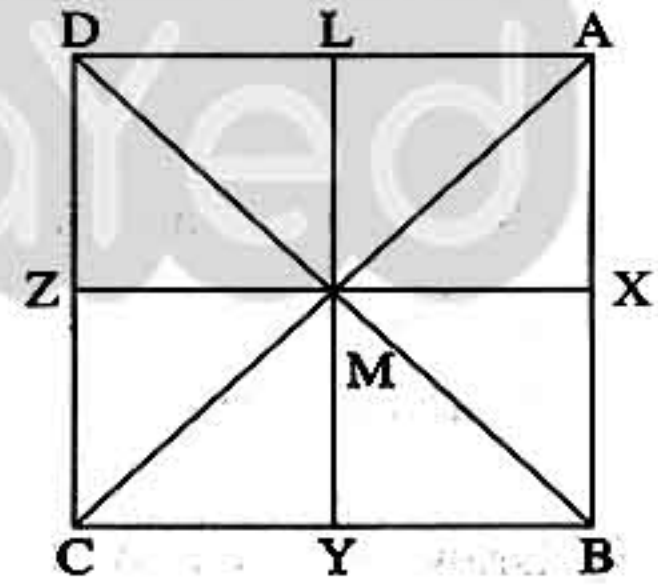
- (a) 5 cm. (b) 7 cm. (c) 10 cm. (d) 15 cm.

2 In the opposite figure :

ABCD is a square whose diagonals intersect at M . X, Y, Z and L are the midpoints of $\overline{AB}, \overline{BC}, \overline{CD}$ and \overline{DA} respectively.

Complete the following :

- (1) The image of the point A by reflection in M is
- (2) The image of the point X by reflection in M is
- (3) The image of \overline{AL} by reflection in M is
- (4) The image of \overline{MZ} by reflection in M is
- (5) The image of \overline{BM} by reflection in M is
- (6) The image of \overline{AX} by reflection in X is
- (7) The image of $\triangle ALM$ by reflection in M is
- (8) The image of $\triangle BXM$ by reflection in M is
- (9) The image of $\triangle AMB$ by reflection in M is
- (10) The image of the square $AXML$ by reflection in M is



Unit 3

- 3 Using the geometric tools, draw the image of each of the following by reflection in A (Answer in the same page of the book):

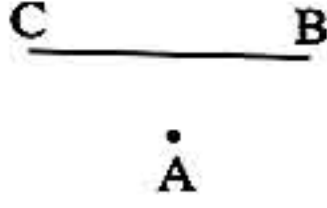


Fig. (1)

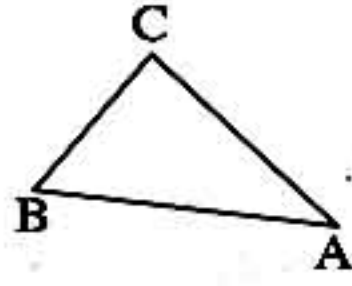


Fig. (2)

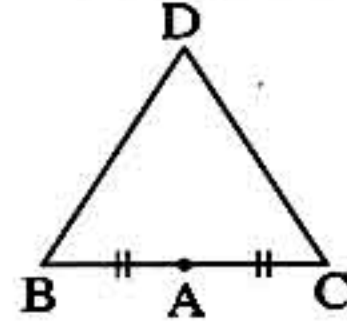


Fig. (3)

- 4 Draw $\triangle ABC$ in which $AB = BC = 4$ cm. and $AC = 5$ cm., then find its image by reflection in the point B

- 5 In each of the following figures, draw $\triangle A'B'C'$ as the image of $\triangle ABC$ by reflection in the point B and mention the name of the figure $A'B'CA'$ giving reason.

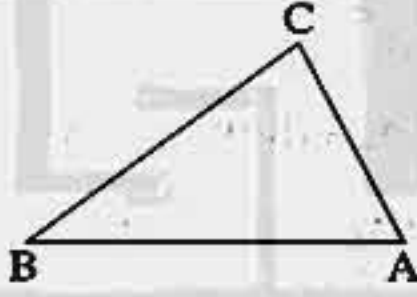


Fig. (1)

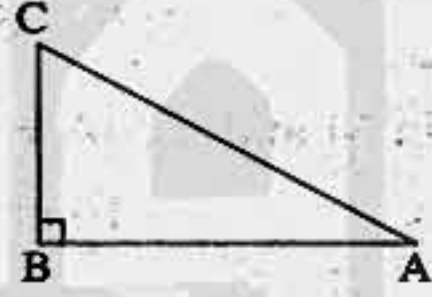


Fig. (2)

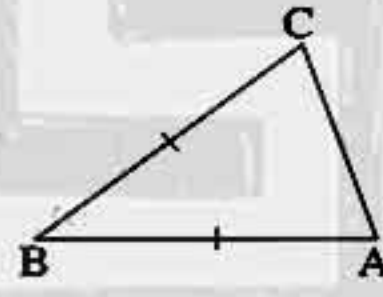


Fig. (3)

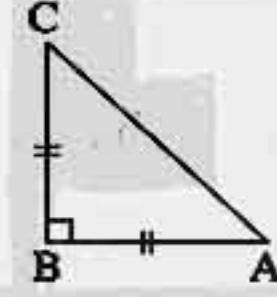


Fig. (4)

- 6 Draw $\triangle ABC$ in which $BC = 3$ cm., $AB = 4$ cm. and $m(\angle B) = 90^\circ$, then draw $\triangle A'B'C'$ as the image of $\triangle ABC$ by reflection in C Prove that the quadrilateral $ABA'B'$ is a parallelogram.

- 7 Draw the square ABCD whose side length is 5 cm. then draw its image by reflection in the point M where M is the point of intersection of its diagonals. What do you observe?

- 8 ABC is a triangle, F is the midpoint of \overline{AC} Draw D as the image of B by reflection in F What is the type of the figure ABCD and what is the type of the triangle ABC required to transfer the figure ABCD to

(1) rectangle.

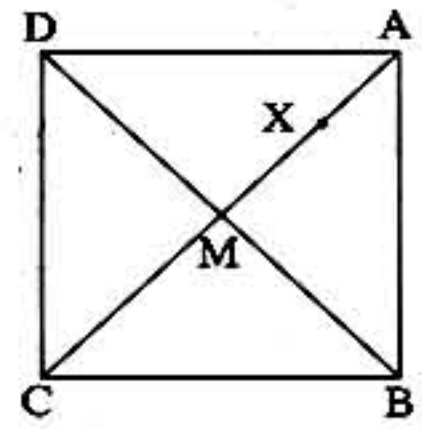
(2) rhombus.

9 In the opposite figure :

ABCD is a square , M is the point of intersection of its diagonals and $X \in \overline{AM}$ Find Y as the image of X by reflection in M then ,

Prove that : (1) $\Delta DAX \cong \Delta BCY$

(2) The figure DXBY is a parallelogram.



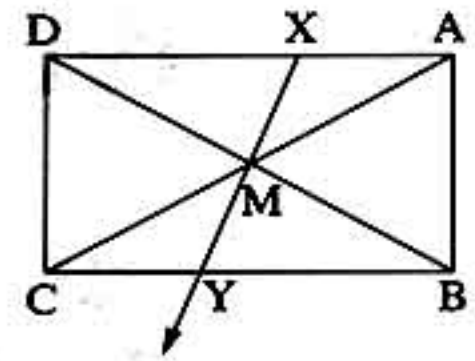
10 In the opposite figure :

ABCD is a rectangle , M is the point of intersection of its diagonals , $X \in \overline{AD}$ and $\overline{XM} \cap \overline{BC} = \{Y\}$

Prove that :

(1) Y is the reflected image of X in M

(2) The figure AXCY is a parallelogram.



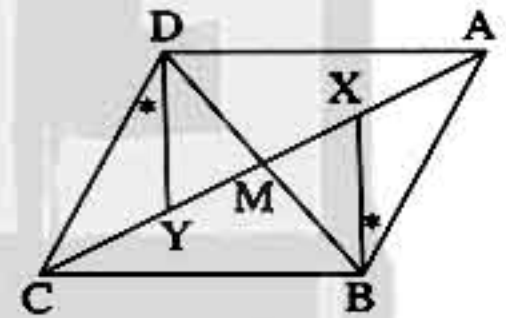
11 In the opposite figure :

ABCD is a parallelogram , M is the point of intersection of its diagonals and $X \in \overline{AC}$, $Y \in \overline{AC}$ such that $m(\angle ABX) = m(\angle CDY)$

Prove that :

(1) ΔABX is the image of ΔCDY by reflection in M

(2) The figure XBYD is a parallelogram.



Unit 3



Life Application

- 12 In front of you , an English letter. Check that if we find the image of this letter by reflection in the midpoint of the inclined line of the letter , then we get the same letter. And we notice that we will see the same figure if we look at it from above or down , right or left. Which of the following figures has the same property ?

N

Enrich information

This point is called "point of symmetry"

M

(1)

I

(2)

H

(3)

E

(4)

A

(5)

Z

(6)

X

(7)

W

(8)

T

(9)

S

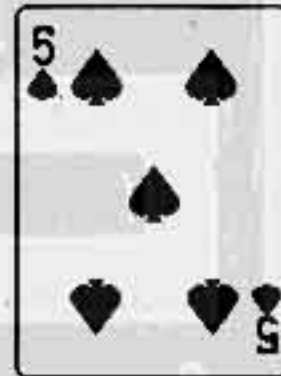
(10)



(11)



(12)



(13)

Second

Problems on reflection in the Cartesian plane :

- 1 Choose the correct answer from those given :

- (1) The image of the point $(-3, 2)$ by reflection in the origin point is
- (a) $(3, 2)$ (b) $(-3, -2)$ (c) $(3, -2)$ (d) $(-3, 2)$
- (2) The point $(5, -2)$ is the image of the point by reflection in the origin point.
- (a) $(5, -2)$ (b) $(-5, -2)$ (c) $(-5, 2)$ (d) $(5, 2)$
- (3) The point whose image by reflection in the origin point is itself is
- (a) $(0, 1)$ (b) $(1, 0)$ (c) $(0, 0)$ (d) $(-1, 0)$
- (4) The image of the point $(3, -2)$ by reflection in the origin point followed by reflection in X-axis is
- (a) $(3, -2)$ (b) $(-3, -2)$ (c) $(-3, 2)$ (d) $(3, 2)$

- 2 On a square lattice, draw ΔABC where $A(3, 1)$, $B(1, 4)$ and $C(0, 0)$, then find its image by reflection in the point C
- 3 In xy -coordinate plane, draw ΔABC , where: $A(-2, 4)$, $B(5, 0)$ and $C(3, -3)$, then find the reflected image of ΔABC in the origin point.
- 4 On a square lattice, draw ΔABC where $A(2, -2)$, $B(3, 4)$ and $C(-3, 2)$, then map $\Delta A'B'C'$ as the image of ΔABC by reflection in y -axis then map $\Delta A''B''C''$ as the image of $\Delta A'B'C'$ by reflection in x -axis. What is the image of ΔABC by reflection in the origin point? What do you deduce?
- 5 $ABCD$ is a rectangle where $A(2, 5)$, $B(6, 5)$, $C(6, 8)$ and $D(2, 8)$, then find the image of the rectangle $ABCD$ by reflection in the origin point.



For excellent pupils

- 6 In the opposite figure:

If \overline{CD} is the image of \overline{BA}

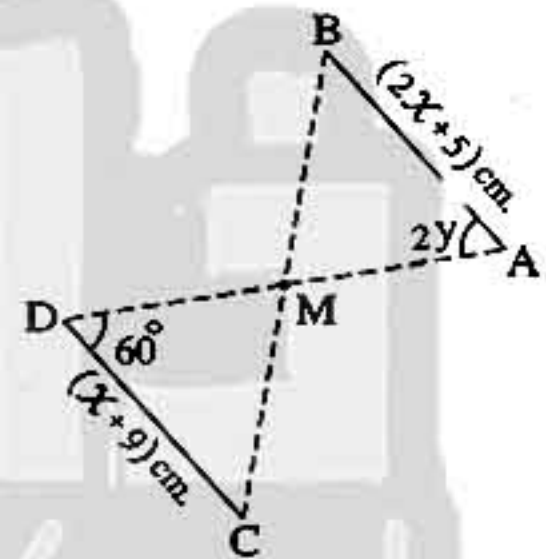
by reflection in the point M and $BA = (2x + 5)$ cm.,

$CD = (x + 9)$ cm., $m(\angle A) = 2y$ and $m(\angle D) = 60^\circ$

Find: (1) The length of \overline{CD}

(2) The value of y

« 13 cm., 30° »



Unit 3

From the school book

Exercise 11

On translation

First

Problems on translation in the plane :

- 1 Using the geometric tools , draw the image of each of the following :
By translation MN in the direction of \overrightarrow{MN} as shown in each case.

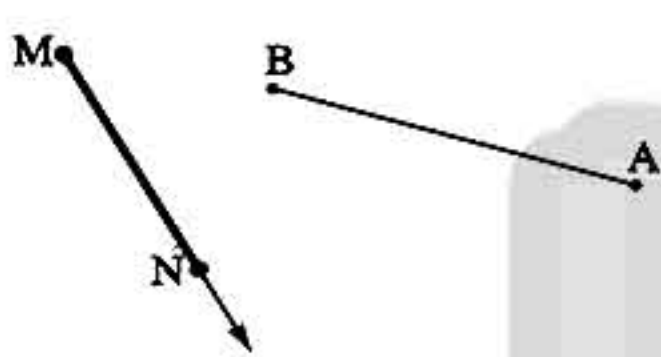


fig. (1)

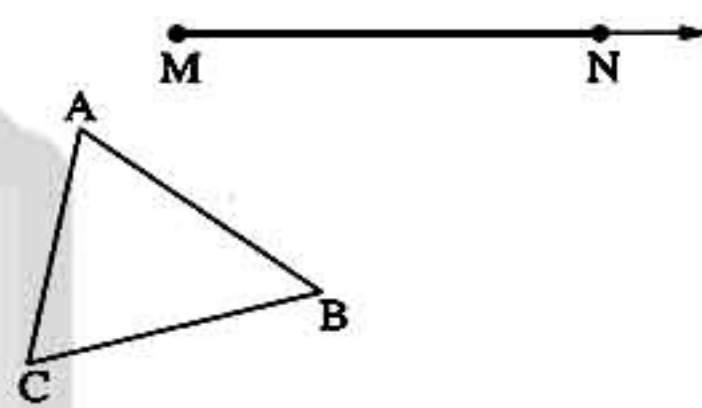
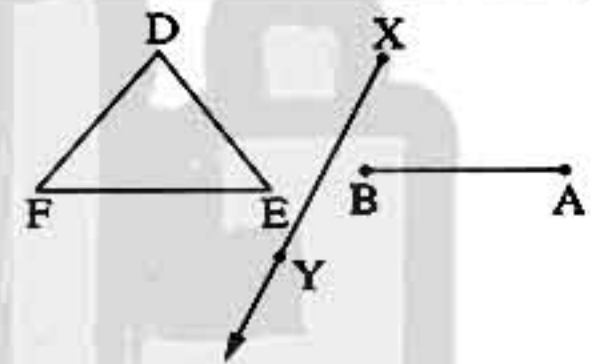


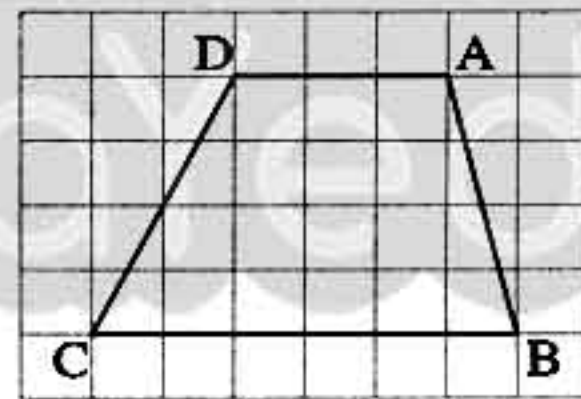
fig. (2)

- 2 In the opposite figure :

Using the geometric tools , find the image of the following figures by the translation of displacement XY in the direction of \overrightarrow{XY}



- 3 Using the grid , draw the image of the figure ABCD by the translation of 4 units in the direction of \overrightarrow{BC}



- 4 Draw a line segment \overline{AB} where $AB = 5$ cm. , then draw the image of \overline{AB} by a translation of magnitude of 8 cm. in the direction of \overrightarrow{AB}
- 5 Using the geometric instruments , draw the square ABCD whose side length is 4 cm. , then draw its image by translation of magnitude of 4 cm. in the direction of \overrightarrow{AB}
- 6 Draw ΔABC in which $AB = 4$ cm. , $BC = 6$ cm. and $CA = 5$ cm. , then draw the image of ΔABC by a translation of magnitude of 3 cm. in the direction of \overrightarrow{CB}

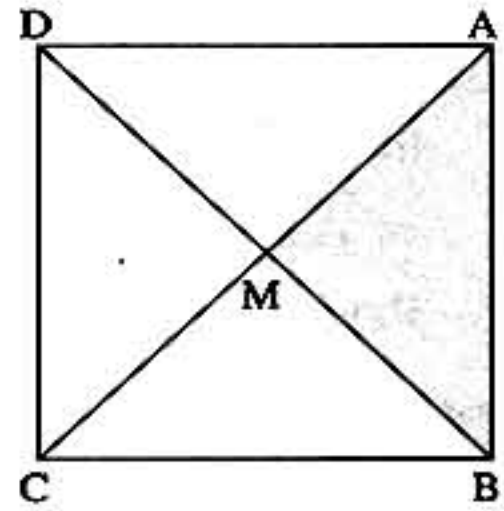
Lesson Eleven

7 In the opposite figure :

ABCD is a square whose side length is 4 cm.

M is the point of intersection of its diagonals. Draw :

- ① The image of $\triangle MAB$ by the translation of distance 2 cm. in the direction of \overrightarrow{AD}
- ② The image of $\triangle AMB$ by the translation AM in the direction of \overrightarrow{AM}

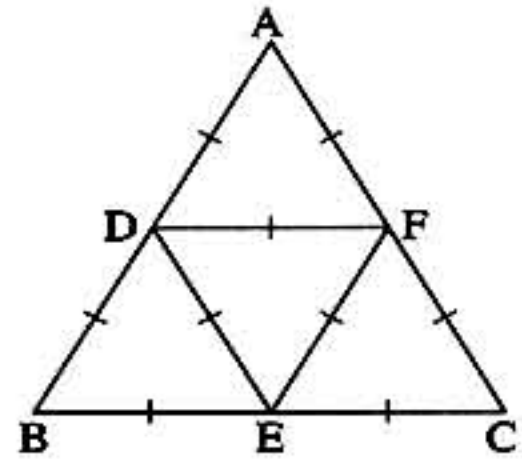


8 In the opposite figure :

The triangles ADF , BDE , DEF and EFC are congruent.

Complete :

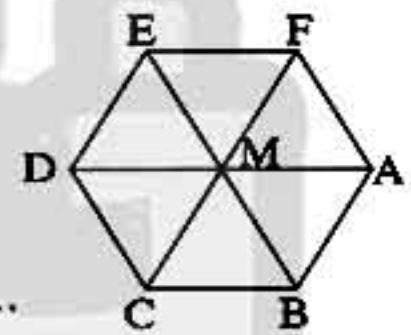
- ① The image of $\triangle ADF$ by a translation of magnitude of AD in the direction of \overrightarrow{AD} is
- ② $\triangle FEC$ is the image of $\triangle DBE$ by a translation of magnitude in the direction of



9 In the opposite figure :

ABCDEF is a regular hexagon. Complete the following :

- ① The image of the point D by translation DM in the direction of \overrightarrow{DM} is
- ② The image of \overline{AF} by translation ED in the direction of \overrightarrow{ED} is
- ③ The image of $\triangle MCD$ by translation EF in the direction of \overrightarrow{EF} is
- ④ The translation which makes $\triangle DME$ the image of $\triangle MAF$ is

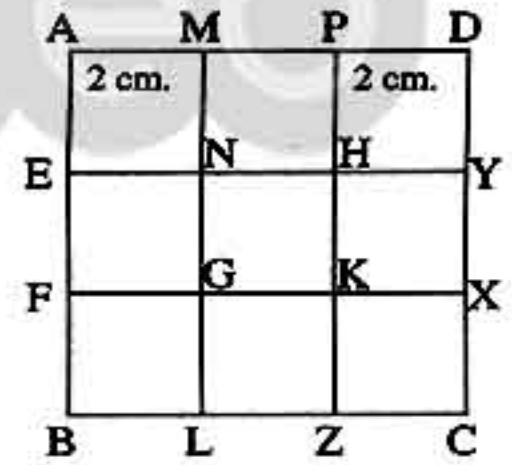


10 In the opposite figure :

ABCD is a square and all the interior squares are congruent.

Complete :

- ① The image of \overline{AE} by a translation of magnitude of 2 cm. in the direction of \overrightarrow{GK} is
- ② The image of the square AENM by a translation of magnitude of 4 cm. in the direction of \overrightarrow{PK} is
- ③ The square MNHP is the image of the square GLZK by a translation of magnitude in the direction of



11 $\triangle ABC$ is right-angled at B where $AB = 3$ cm. and $BC = 4$ cm. If $\triangle A'B'C'$ is the image of $\triangle ABC$ by translation of a distance 3 cm. in the direction of \overrightarrow{CB}
Prove that : The figure $AA'C'C$ is a parallelogram.

Unit 3

- 12 Draw ΔABC which is right-angled at B, in which $AB = BC = 3$ cm. then find the image of ΔABC by translation of a distance 3 cm. in the direction of \overrightarrow{AB} , then

Prove that : The figure $BB'C'C$ is a square.

- 13 $ABCD$ is a rectangle, where $E \in \overline{AD}$ Find the translated image of ΔABE by translation of a magnitude DA in the direction of \overrightarrow{AD} If E' is the image of E by the same translation.

Prove that : The figure $BC'E'E$ is a parallelogram.

- 14 $ABCD$ is a parallelogram, $\overline{BE} \perp \overline{AD}$ cutting it at E Find $\Delta A'B'D'$ as the image of ΔABE by translation of a distance ED in the direction of \overrightarrow{AD} , then prove that the figure $EBB'D'$ is a rectangle.

Second Problems on translation in the Cartesian plane :

- 1 Complete the following :

- (1) The image of the point $(2, 5)$ by translation $(x, y) \longrightarrow (x + 2, y + 1)$ is
- (2) The image of the point $(3, 2)$ by translation $(x, y) \longrightarrow (x + 3, y - 2)$ is
- (3) The image of the point $(-5, 4)$ by translation $(x, y) \longrightarrow (x + 4, y - 5)$ is
- (4) The image of the point $(-2, -5)$ by translation $(x, y) \longrightarrow (x - 2, y)$ is
- (5) The image of the point $(3, -2)$ by translation $(x, y) \longrightarrow (x, y + 3)$ is

- 2 Choose the correct answer from those given :

- (1) The image of the point $(-1, 2)$ by translation of magnitude of 3 units in the positive direction of the X-axis is
 (a) $(-1, 5)$ (b) $(2, 2)$ (c) $(-2, 2)$ (d) $(-1, 3)$
- (2) The image of the point $(-3, 4)$ by translation of magnitude of 4 units in the negative direction of the y-axis is
 (a) $(-3, 0)$ (b) $(-7, 4)$ (c) $(-3, 8)$ (d) $(-1, 4)$
- (3) If $A'(3, -3)$ is the image of A by translation $(x, y) \longrightarrow (x - 1, y - 4)$, then the point A is
 (a) $(2, -7)$ (b) $(4, 1)$ (c) $(-4, -1)$ (d) $(2, 1)$
- (4) The image of the point $(-1, 4)$ by the translation $(3, -2)$ followed by reflection in the X-axis is
 (a) $(2, 2)$ (b) $(-2, 2)$ (c) $(-2, -2)$ (d) $(2, -2)$
- (5) If the point $(a, -1)$ is the image of $(2, 4)$ by the translation $(x, y) \longrightarrow (x + 1, y - b)$, then (a, b) is
 (a) $(3, 3)$ (b) $(1, 3)$ (c) $(3, 5)$ (d) $(1, -5)$

(6) If : \hat{A} is the image of the point A (2 , 3) by reflection in the y-axis , then A is the image of \hat{A} by the translation

(a) $(x, y) \longrightarrow (x + 4, y)$

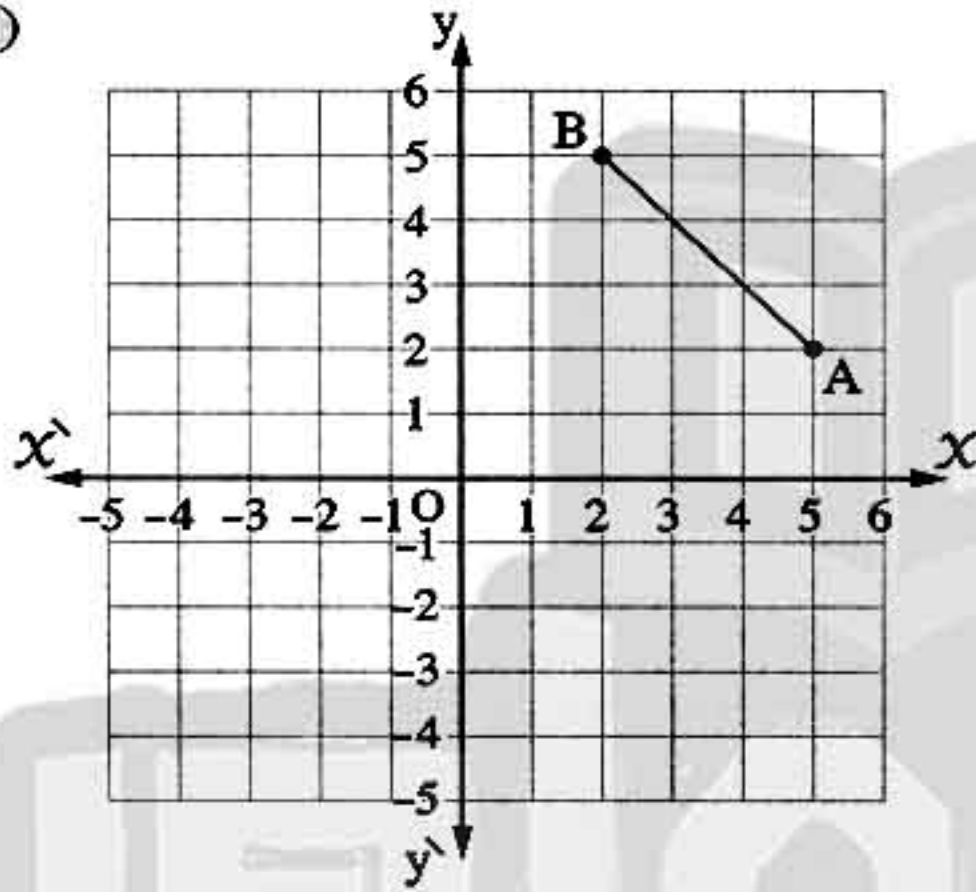
(b) $(x, y) \longrightarrow (x, y + 6)$

(c) $(x, y) \longrightarrow (x - 4, y)$

(d) $(x, y) \longrightarrow (x, y - 6)$

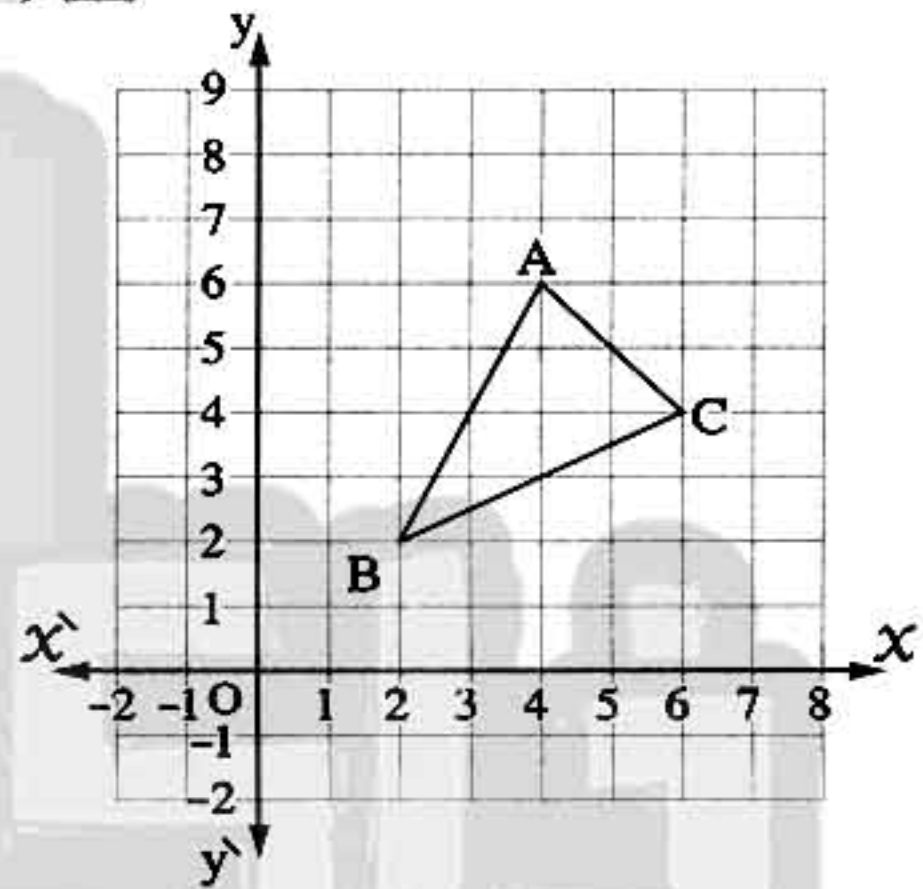
(3) Find the image of each of the following figures by the translation shown under each figure :

(1)



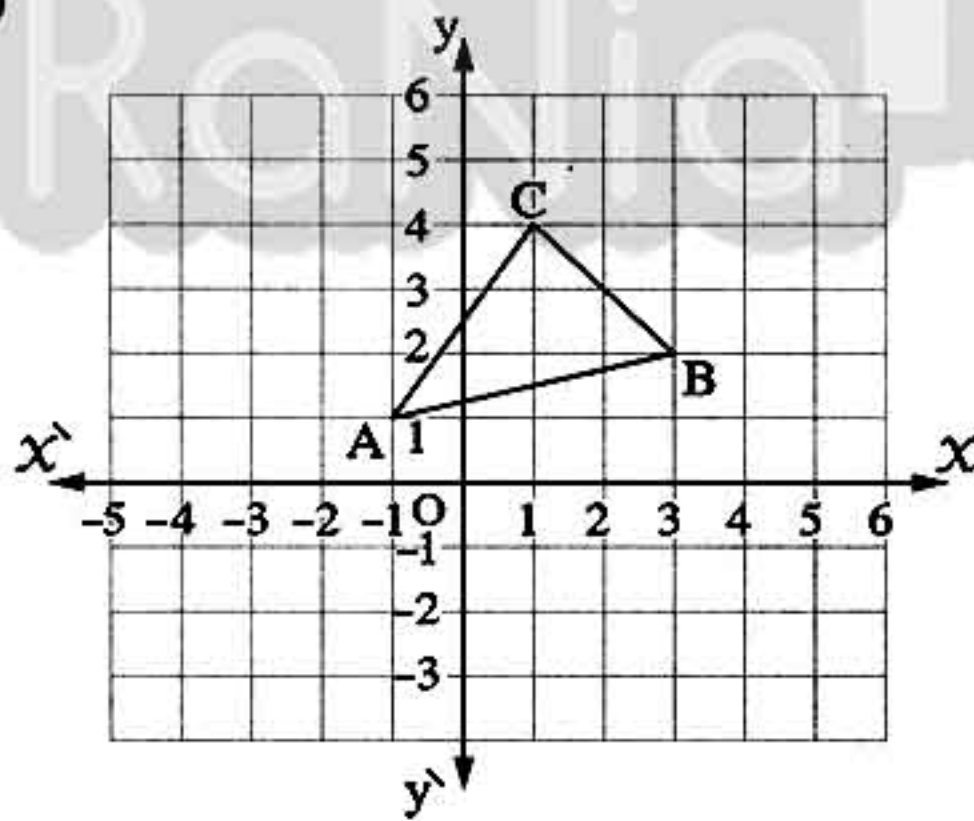
$(x, y) \longrightarrow (x - 3, y - 4)$

(2)



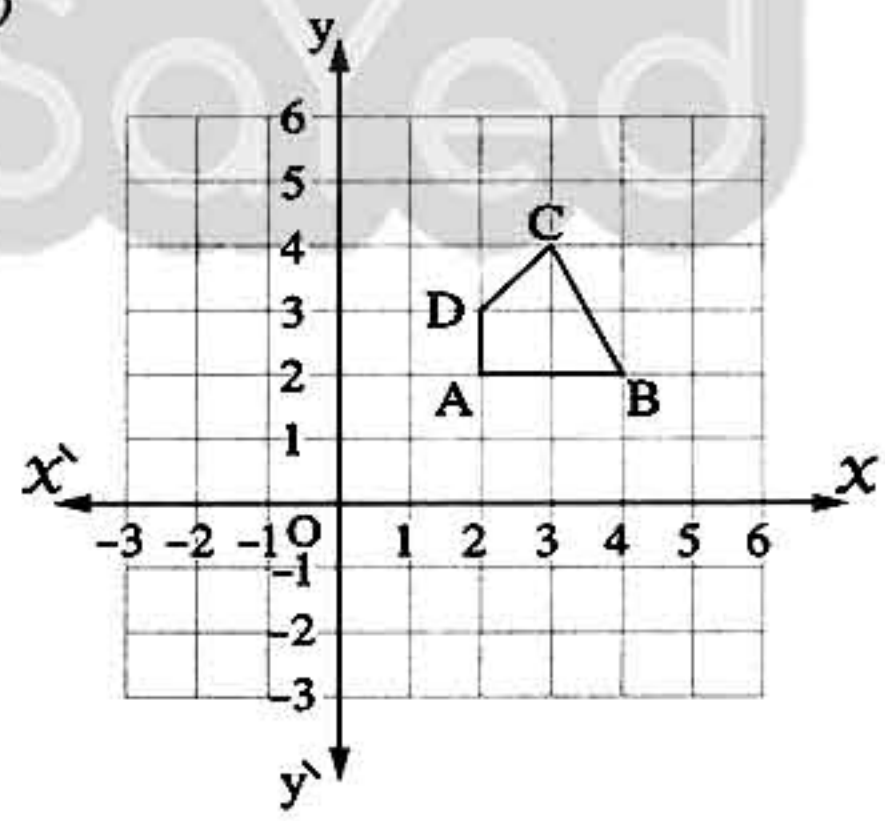
$(x, y) \longrightarrow (x + 2, y + 3)$

(3)








$(x, y) \longrightarrow (x + 2, y)$

(4)



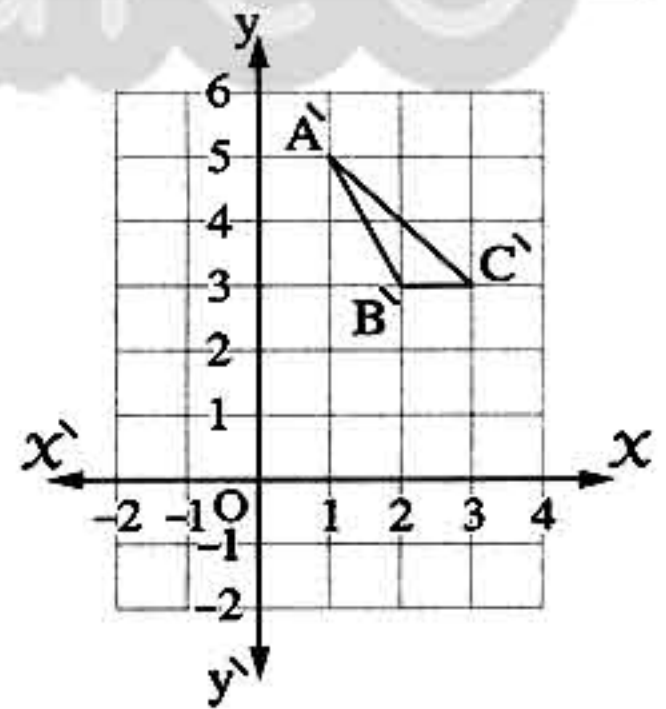
$(x, y) \longrightarrow (x + 3, y - 2)$

- 10 On a square lattice, draw ΔABC where $A(2, 1)$, $B(1, -1)$ and $C(0, 1)$, then draw its image by a translation of $2AB$ in the direction of \overrightarrow{AB}
- 11  A square has vertices $A(1, 1)$, $B(4, 2)$, $C(3, 5)$ and $D(0, 4)$
- (1) Graph the square and its image under the translation which maps vertex A onto vertex B
 - (2) Write the mapping rule for the translation.
- 12  Use the translation: $(x, y) \longrightarrow (x + 2, y + 3)$ to locate the point whose image is $(2, 3)$
- 13  If the image of the point $A(1, 1)$ by translation in the plane is $\hat{A}(2, 2)$, find the images of the points $O(0, 0)$, $B(-1, 3)$ and $C(-3, 5)$ by the same translation.
- 14 If $A(-3, 1)$ and $B(1, -2)$, write the mapping rule of the translation that makes B the image of A
- 15 If $A(3, 2)$, $B(5, 1)$, find:
- (1) \hat{C} which is the image of $C(1, -1)$ under translation of AB in the direction of \overrightarrow{AB}
 - (2) D whose image is $\hat{D}(2, 1)$ under translation of AB in the direction of \overrightarrow{AB}
- 16  The point $\hat{A}(3, -3)$ is the image of the point A by the translation $(x, y) \longrightarrow (x - 1, y - 4)$. Locate A then by the same translation, draw the image of ΔABC where $B(5, 0)$ and $C(-1, -2)$

- 17  In the opposite figure:

Copy the graph, then draw the triangle ABC whose image is $\Delta \hat{A}\hat{B}\hat{C}$ by the translation

$$(x, y) \longrightarrow (x + 2, y + 3)$$



- 18 If $A(-2, 1)$ and $B(1, 3)$, find on a square lattice the image of \overline{AB} by reflection in x -axis followed by the translation $(x, y) \longrightarrow (x + 4, y)$

Unit 3

19 State whether the graph shows a reflection or a translation :

(1) Name the line of reflection.

(2) Describe the translation.

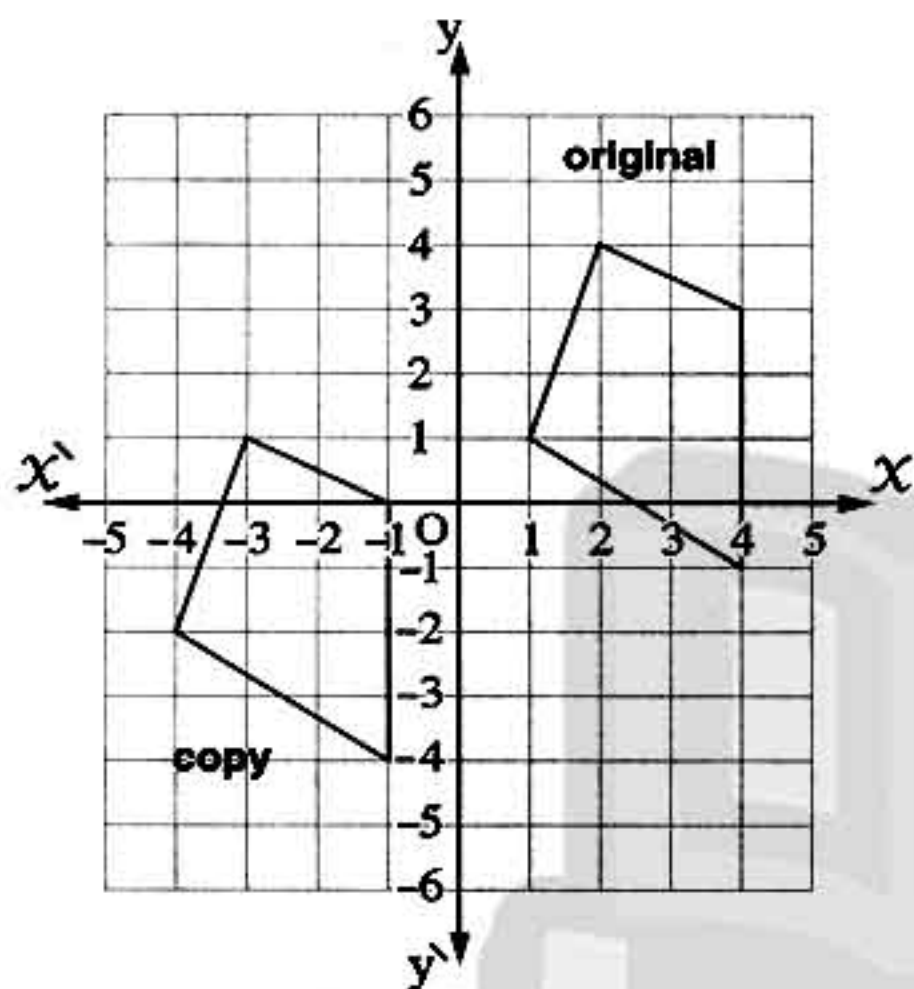


fig. (1)

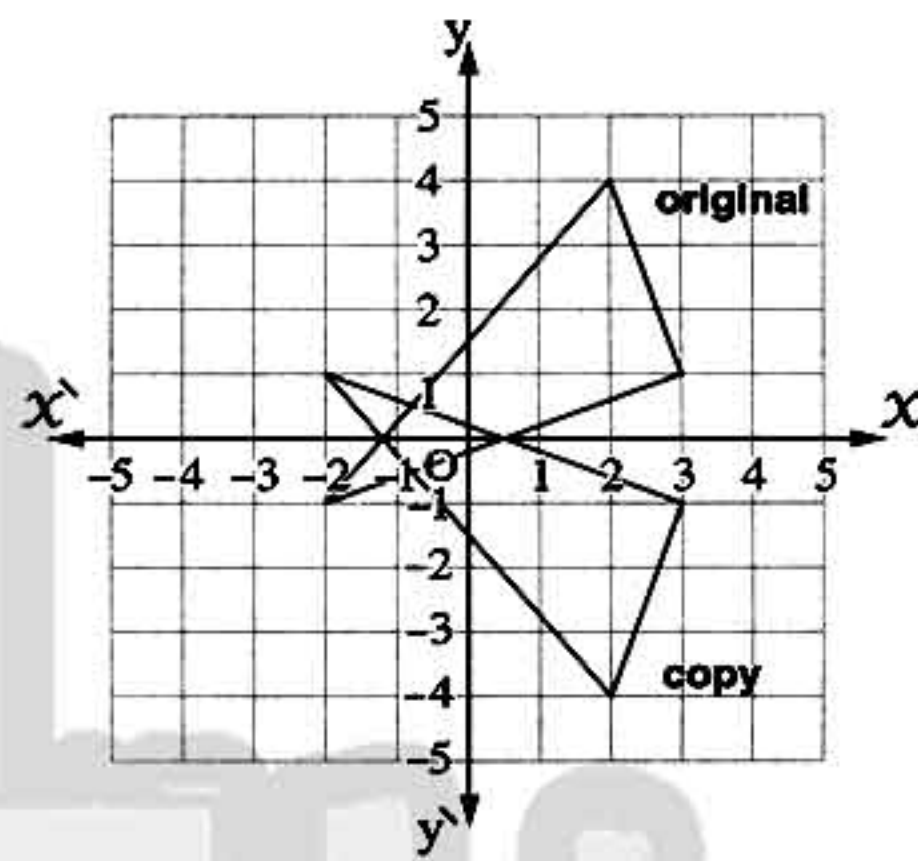


fig. (2)

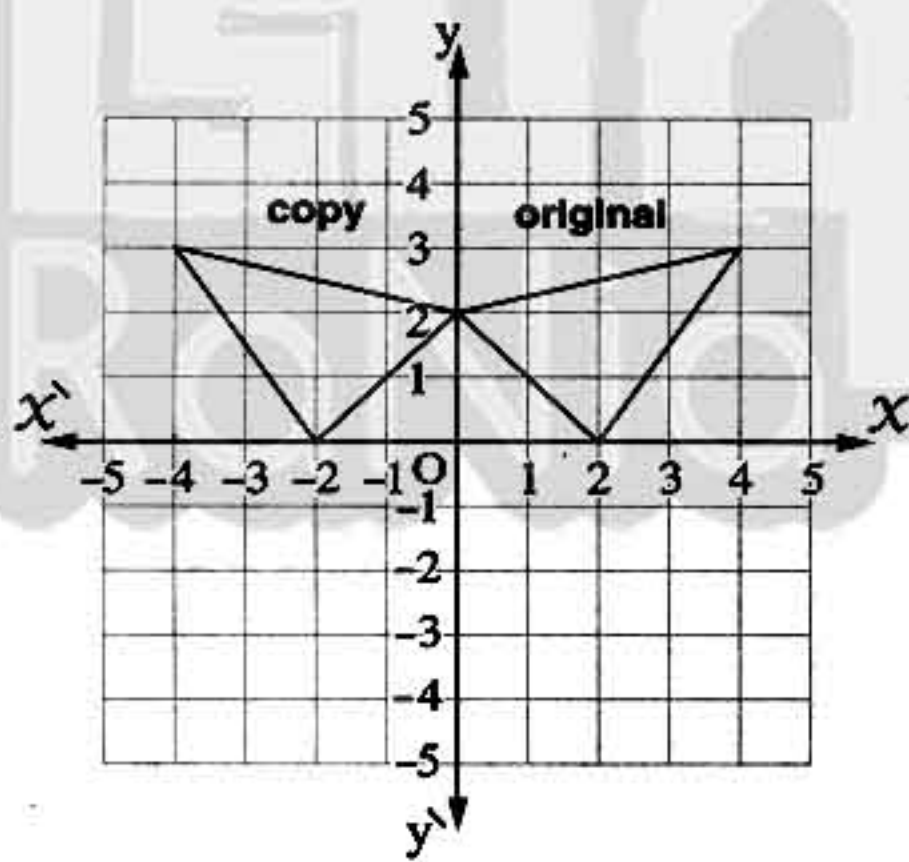


fig. (3)

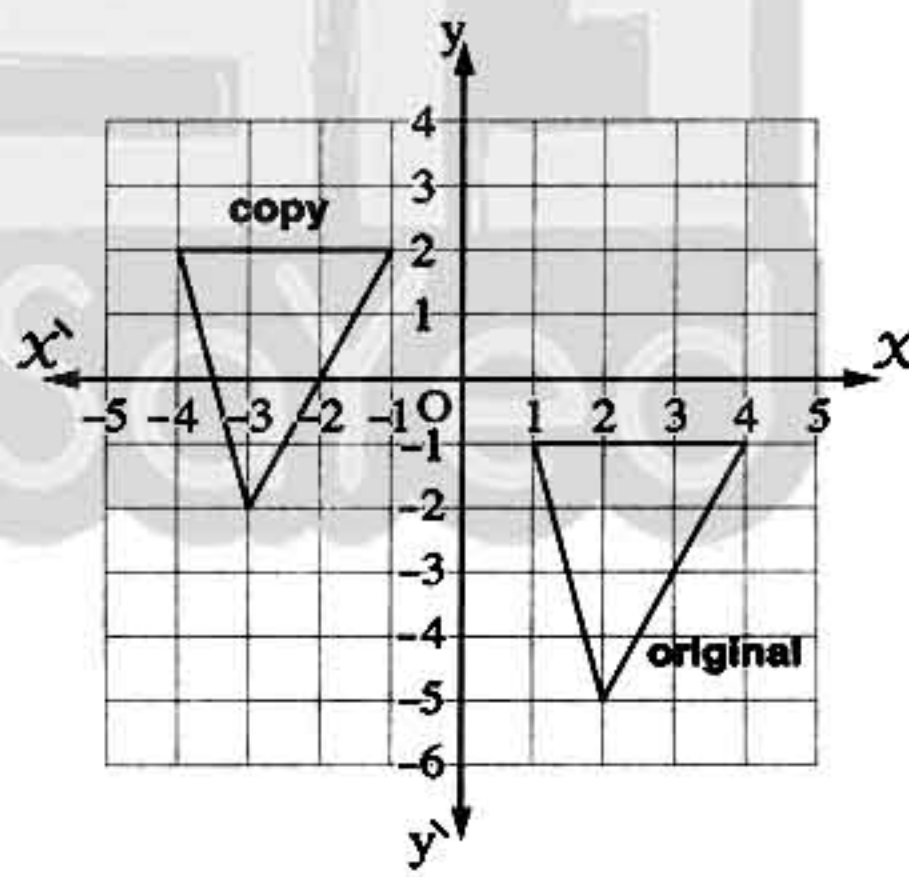


fig. (4)



Worksheet 5 till lesson 5 unit 3

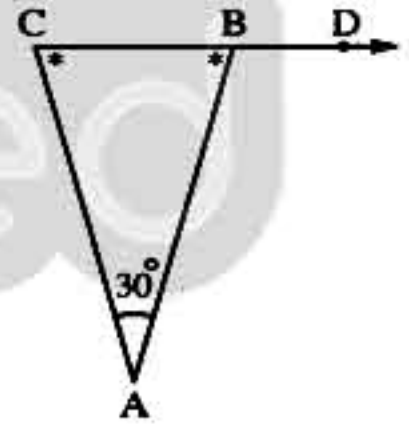
Answer the following questions :

1 Choose the correct answer from those given :

- (1) The sum of measures of the interior angles of the triangle =
 (a) 108° (b) 180° (c) 630° (d) 360°
- (2) If the measures of two angles in a triangle are 40° and 45° , then the triangle is
 (a) acute-angled (b) right-angled (c) obtuse-angled (d) equilateral
- (3) In the parallelogram ABCD, if $\angle A$ is acute, then $\angle C$ is
 (a) acute. (b) obtuse.
 (c) right. (d) reflex.
- (4) The parallelogram in which one of its angles is right is
 (a) a trapezium. (b) a square. (c) a rhombus. (d) a rectangle.
- (5) The measure of the exterior angle of the equilateral triangle =
 (a) 30° (b) 60° (c) 90° (d) 120°
- (6) The number of sides of the regular polygon in which the measure of an interior angle = 120° is
 (a) 5 (b) 6 (c) 7 (d) 8

2 Complete the following :

- (1) The measure of the exterior angle of the triangle equals
- (2) In the opposite figure :
 $D \in \overline{CB}$, $m(\angle A) = 30^\circ$,
 then $m(\angle ABD) = \dots\dots\dots^\circ$
- (3) In the parallelogram ABCD,
 if $m(\angle A) = \frac{1}{2} m(\angle B)$, then $m(\angle B) = \dots\dots\dots$
- (4) The two diagonals of the rhombus are and

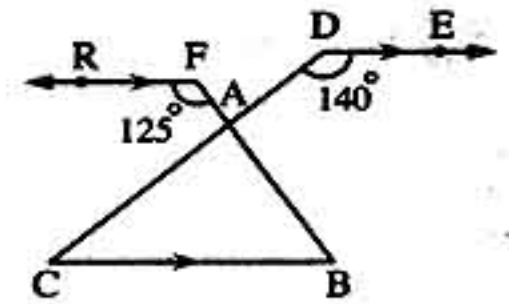


3 In the opposite figure :

$$\overline{DE} \parallel \overline{FR} \parallel \overline{BC}$$

$$m(\angle D) = 140^\circ, m(\angle F) = 125^\circ$$

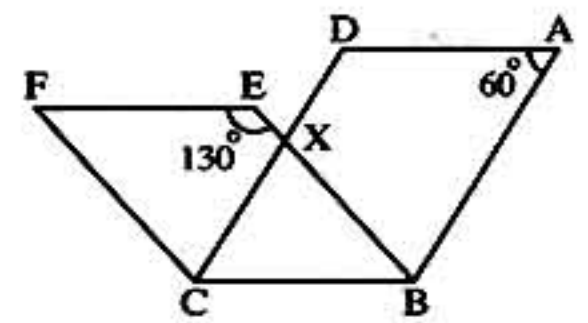
Calculate the measures of the angles of ΔABC



4 In the opposite figure :

ABCD and EBCF are two
 parallelograms, $m(\angle A) = 60^\circ$
 $m(\angle E) = 130^\circ$

Find : by proof $m(\angle BXC)$



Worksheets on Geometry



The answer of worksheet

5

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| 1 | a | b | c | d |
| 2 | a | b | c | d |
| 3 | a | b | c | d |
| 4 | a | b | c | d |
| 5 | a | b | c | d |
| 6 | a | b | c | d |



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Worksheet 6 till lesson 6 unit 3

Answer the following questions :

1 Choose the correct answer from those given :

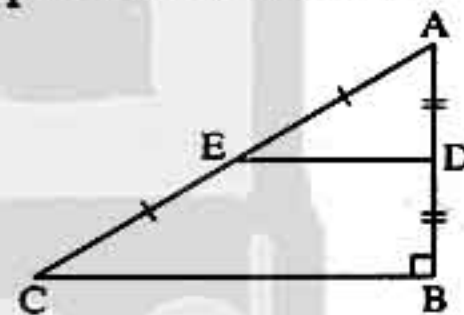
- (1) The sum of measures of the interior angles of the heptagon =
 - (a) 540°
 - (b) 720°
 - (c) 900°
 - (d) 180°
- (2) The side length of a rhombus is 5 cm. , then its perimeter = cm.
 - (a) 10
 - (b) 15
 - (c) 20
 - (d) 25
- (3) The concave polygon should has a angle.
 - (a) acute
 - (b) right
 - (c) obtuse
 - (d) reflex
- (4) ABCD is a parallelogram in which $m(\angle A) + m(\angle C) = 160^\circ$, then $m(\angle B) = \dots\dots\dots$
 - (a) 20°
 - (b) 80°
 - (c) 100°
 - (d) 110°
- (5) The sum of measures of the interior angles of the triangle = the measure of angle.
 - (a) a right.
 - (b) a straight.
 - (c) acute.
 - (d) reflex.
- (6) The length of the line segment joining the midpoints of two sides of a triangle equals the length of the third side.
 - (a) $\frac{1}{4}$
 - (b) twice
 - (c) $\frac{1}{2}$
 - (d) $\frac{1}{3}$

2 Complete the following :

- (1) The measure of each interior angle in a regular polygon of n sides =
- (2) The ray which is drawn from the midpoint of a side of a triangle parallel to one of the other sides

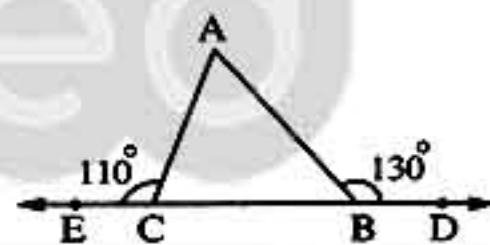
(3) In the opposite figure :

If $m(\angle B) = 90^\circ$, D and E are the midpoints of \overline{AB} and \overline{AC} respectively then $m(\angle ADE) = \dots\dots\dots^\circ$



(4) In the opposite figure :

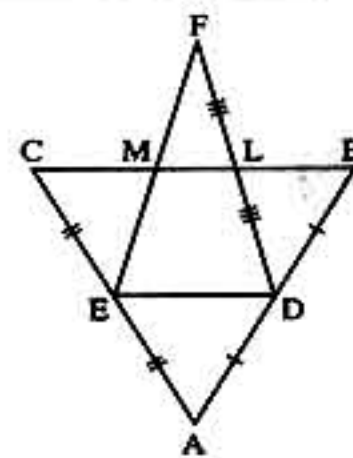
If $D \in \overline{CB}$ and $E \in \overline{BC}$, then $m(\angle A) = \dots\dots\dots^\circ$



3 In the opposite figure :

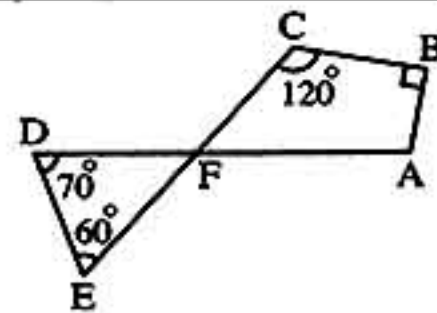
D is the midpoint of \overline{AB} ,
E is the midpoint of \overline{AC} ,
L is the midpoint of \overline{FD}
 $BC = 20$ cm.

Find : the length of \overline{LM}



4 In the opposite figure :

$AD \cap CE = \{F\}$, $m(\angle B) = 90^\circ$
 $m(\angle C) = 120^\circ$, $m(\angle E) = 60^\circ$, $m(\angle D) = 70^\circ$
Find : $m(\angle A)$



Worksheets on Geometry



The answer of worksheet

6

Total
mark

15



35

1 Shade the circle that represents your choice for the correct answer :

- | | | | |
|-------|---|---|---|
| (1) a | b | c | d |
| (2) a | b | c | d |
| (3) a | b | c | d |
| (4) a | b | c | d |
| (5) a | b | c | d |
| (6) a | b | c | d |

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(4)

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Worksheet 7 till lesson 7 unit 3

Answer the following questions :

1 Choose the correct answer from those given :

- (1) The measure of the interior angle of a regular hexagon =
 (a) 120° (b) 102° (c) 180° (d) 360°
- (2) In $\triangle ABC$, if $m(\angle A) = m(\angle B) = 50^\circ$, then $m(\angle C) = \dots\dots\dots$
 (a) 130° (b) 100° (c) 80° (d) 50°
- (3) The parallelogram whose one of its angles is a right angle is called
 (a) trapezium. (b) square. (c) rhombus. (d) rectangle.
- (4) A rectangle whose length = 4 cm. and width = 3 cm., then the length of its diagonal = cm.
 (a) 3 (b) 4 (c) 5 (d) 25
- (5) The number of sides of the regular polygon which the measure of one of its interior angles is $144^\circ = \dots\dots\dots$
 (a) 4 sides. (b) 6 sides. (c) 8 sides. (d) 10 sides.
- (6) In $\triangle ABC$, if $m(\angle B) = m(\angle A) + m(\angle C)$, then $\angle B$ is
 (a) acute. (b) right. (c) obtuse. (d) reflex.

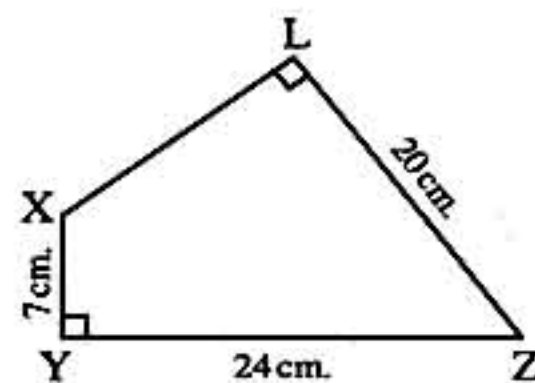
2 Complete the following :

- (1) In the right-angled triangle, the area of the square on the hypotenuse equals
- (2) The square is with a right angle.
- (3) The line segment joining the midpoints of two sides of a triangle is the third side and its length equals
- (4) If ABCD is a parallelogram in which $m(\angle A) = 40^\circ$, then $m(\angle B) = \dots\dots\dots^\circ$

3 In the opposite figure :

$m(\angle Y) = m(\angle L) = 90^\circ$
 $XY = 7$ cm. , $YZ = 24$ cm.
 and $LZ = 20$ cm.

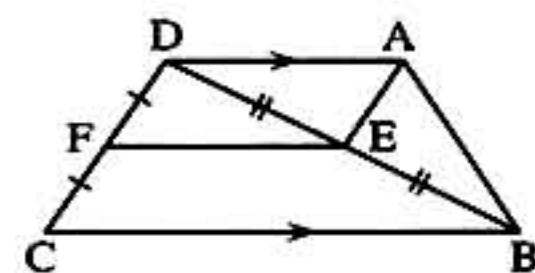
Find : the length of \overline{XL}



4 In the opposite figure :

$\overline{AD} \parallel \overline{BC}$, $AD = \frac{1}{2} BC$
 E is the midpoint of \overline{BD}
 and F is the midpoint of \overline{CD}

Prove that : AEFD is a parallelogram.





The answer of worksheet

7



Total mark

15



37

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| ① | a | b | c | d |
| ② | a | b | c | d |
| ③ | a | b | c | d |
| ④ | a | b | c | d |
| ⑤ | a | b | c | d |
| ⑥ | a | b | c | d |

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Worksheet 8 till lesson 8 unit 3

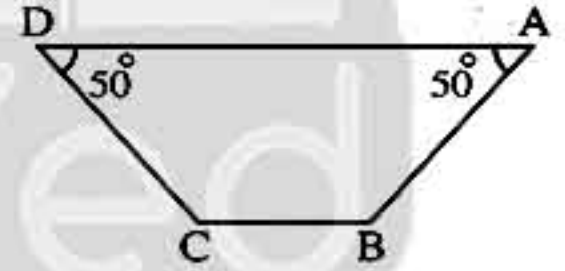
Answer the following questions :

1 Choose the correct answer from those given :

- (1) The sum of measures of the interior angles of the hexagon =
 (a) 4 right angles. (b) 5 right angles. (c) 6 right angles. (d) 8 right angles.
- (2) If ABCD is a square, then $(AC)^2 = \dots\dots\dots$
 (a) AB (b) $(AB)^2$ (c) $2(AB)^2$ (d) $4(AB)^2$
- (3) In $\triangle ABC$, if $m(\angle B) = \frac{1}{2} m(\angle A) = 30^\circ$, then the triangle will be triangle.
 (a) acute-angled (b) right-angled (c) equilateral (d) isosceles
- (4) The image of the point (1, 2) by the transformation $(x, y) \rightarrow (x, -y)$ is
 (a) (-1, 2) (b) (-1, -2) (c) (1, -2) (d) (2, -1)
- (5) The sum of measures of the exterior angles of a polygon of n sides equals
 (a) 180° (b) 360° (c) $(n-2) \times 180^\circ$ (d) $\frac{(n-2) \times 180}{n}$
- (6) In $\triangle ABC$, if D and E are the midpoints of \overline{AB} and \overline{AC} respectively and $BC = 8$ cm., then $DE = \dots\dots\dots$ cm.
 (a) 16 (b) 12 (c) 4 (d) 2

2 Complete the following :

- (1) If two straight lines intersect, then each two vertically opposite angles are
- (2) If $\triangle XYZ$ is a right-angled triangle at Z, then $(XZ)^2 = \dots\dots\dots$
- (3) In the opposite figure :
 $m(\angle A) = m(\angle D) = 50^\circ$
 \overline{AB} and \overline{DC} intersect at E
 not shown in the figure.
 , then $m(\angle E) = \dots\dots\dots$
- (4) The quadrilateral in which two opposite sides are parallel is



[a] If the ratio among the measures of the interior angles of a quadrilateral is 2 : 2 : 3 : 5, find the measure of the greatest angle in the quadrilateral.

[b] In the opposite figure :

ABC is a triangle in which

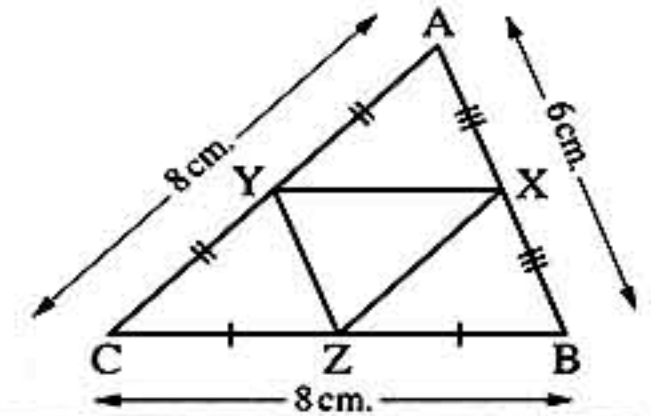
X, Y and Z are the midpoints

of \overline{AB} , \overline{AC} and \overline{BC} respectively

It $AB = 6$ cm., $BC = 8$ cm., $AC = 8$ cm.,

(1) calculate the perimeter of $\triangle XYZ$

(2) determine the type of the figure $XYZZ$



4 On lattice, draw $\triangle ABC$ where $A(1, 2)$, $B(4, 2)$, $C(4, 4)$, then map its image by the transformation $(x, y) \rightarrow (y, -x)$

Worksheets on Geometry

The answer of worksheet **8**

Total mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|---|---|---|---|
| ① | a | b | c | d |
| ② | a | b | c | d |
| ③ | a | b | c | d |
| ④ | a | b | c | d |
| ⑤ | a | b | c | d |
| ⑥ | a | b | c | d |



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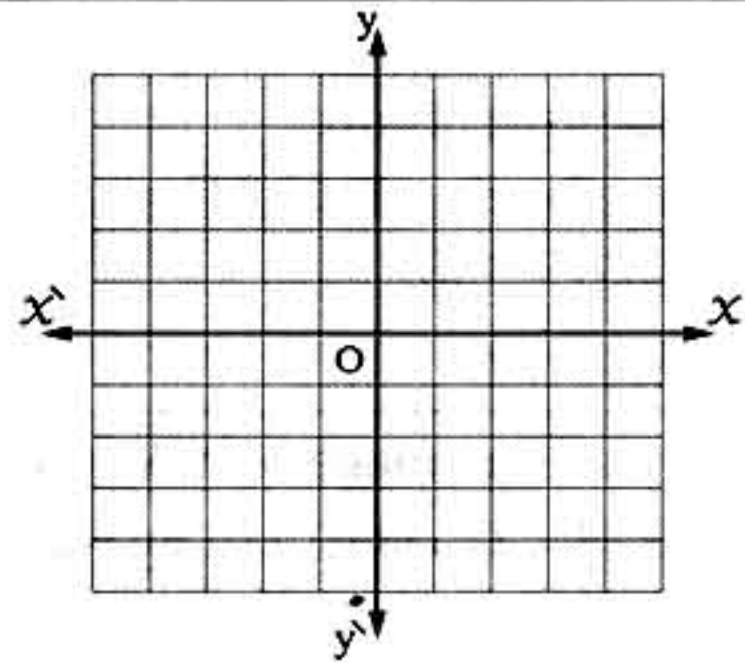
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Worksheet 9 till lesson 9 unit 3

Answer the following questions :

1 Choose the correct answer from those given :

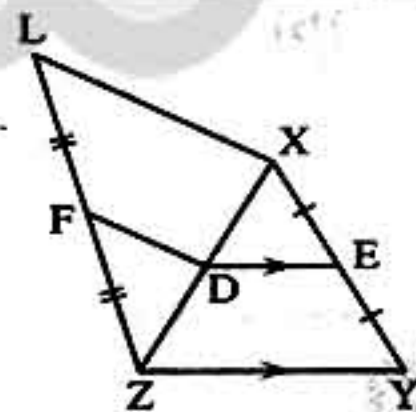
- (1) The number of axes of symmetry of the square is
- (a) 1 (b) 2 (c) 3 (d) 4
- (2) The image of the point $(3, -5)$ by the reflection in X -axis is
- (a) $(3, 5)$ (b) $(-3, 5)$ (c) $(-3, -5)$ (d) $(3, -5)$
- (3) ABC is a triangle in which $m(\angle A) = 60^\circ$, $m(\angle B) = 2m(\angle C)$, then $m(\angle B) = \dots\dots\dots$
- (a) 40° (b) 60° (c) 70° (d) 80°
- (4) The image of the point $(2, 3)$ by the reflection in y -axis is
- (a) $(-2, 3)$ (b) $(2, -3)$ (c) $(-2, -3)$ (d) $(3, 2)$
- (5) The sum of measures of the exterior angles of the octagon =
- (a) 540° (b) 360° (c) 720° (d) 1080°
- (6) ABC is a right - angled triangle at B in which $AB = 3$ cm. and $BC = 4$ cm. , then $AC = \dots\dots\dots$ cm.
- (a) 2.5 (b) 5 (c) 16 (d) 9

2 Complete the following :

- (1) The measure of the exterior angle of the triangle equals
- (2) The image of the point $(-5, 4)$ by the transformation $(X, y) \rightarrow (-y, X)$ is
- (3) If ABCD is a rhombus , then $\dots\dots\dots \perp \dots\dots\dots$
- (4) The reflection in a straight line keeps $\dots\dots\dots$, $\dots\dots\dots$, $\dots\dots\dots$, $\dots\dots\dots$

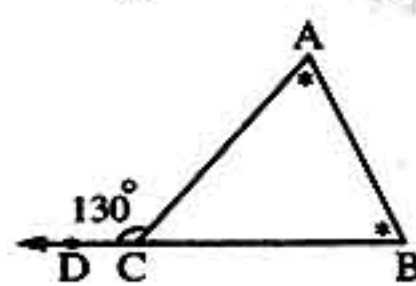
3 [a] In the opposite figure :

$XE = EY$, $\overline{ED} \parallel \overline{YZ}$
 F is the midpoint of \overline{ZL}
 Prove that : $\overline{DF} \parallel \overline{XL}$



[b] In the opposite figure :

ABC is a triangle , $D \in \overline{BC}$
 $m(\angle ACD) = 130^\circ$
 Find : $m(\angle B)$



4 On lattice , find the image of ΔABO where
 $A(2, 2)$, $B(4, 2)$, $O(0, 0)$ by reflection in y -axis.

Worksheets on Geometry



The answer of worksheet

9

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | | |
|---|-----|-----|-----|-----|
| ① | (a) | (b) | (c) | (d) |
| ② | (a) | (b) | (c) | (d) |
| ③ | (a) | (b) | (c) | (d) |
| ④ | (a) | (b) | (c) | (d) |
| ⑤ | (a) | (b) | (c) | (d) |
| ⑥ | (a) | (b) | (c) | (d) |



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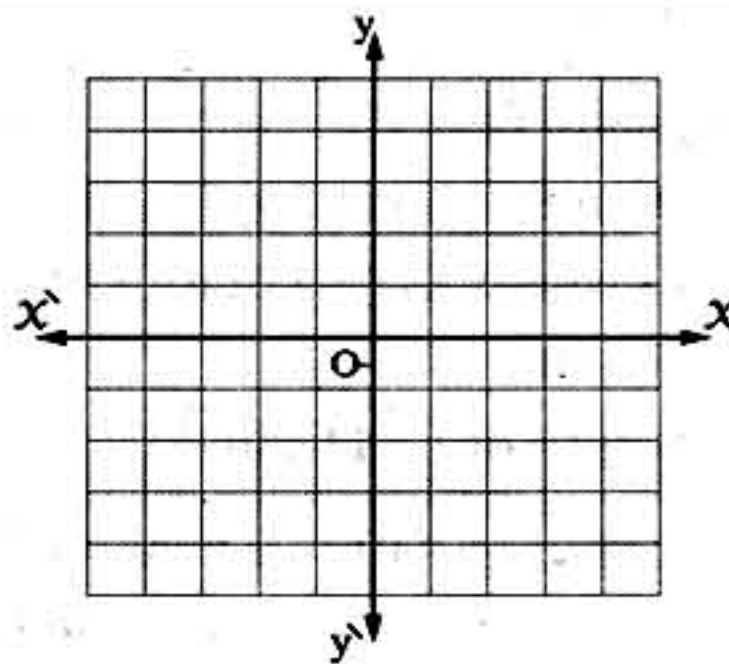
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Worksheets on Geometry



Worksheet 10 till lesson 10 unit 3

Answer the following questions :

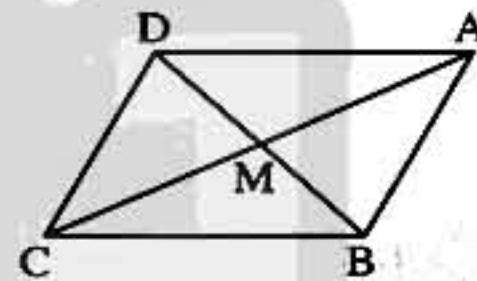
1 Choose the correct answer from those given :

- (1) The point $(2, -4)$ is the image of the point by reflection in the origin point.
 (a) $(2, 4)$ (b) $(-2, 4)$ (c) $(-2, -4)$ (d) $(2, -4)$
- (2) The measure of the exterior angle of a triangle is the measure of any interior angle of the triangle except its adjacent angle.
 (a) $>$ (b) $<$ (c) $=$ (d) \leq
- (3) If ABCD is a rectangle, then $AC = \dots\dots\dots$
 (a) AB (b) BC (c) BD (d) CD
- (4) The parallelogram whose two diagonals are perpendicular and the measure of one of its angles is 90° is called
 (a) rectangle. (b) rhombus. (c) square. (d) trapezium.
- (5) The number of axes of symmetry of the rectangle is
 (a) 1 (b) 2 (c) 3 (d) 4

(6) In The opposite figure :

If ABCD is a parallelogram, then the image of ΔAMD by reflection in the point M is $\Delta \dots\dots\dots$

- (a) AMB (b) DMC
 (c) CMB (d) DMA

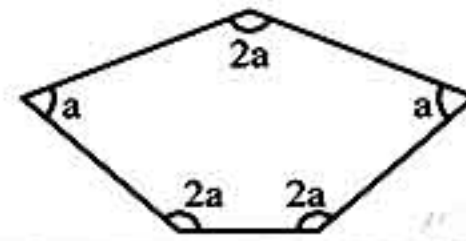


2 Complete the following :

- (1) If the reflection in a straight line transforms the figure to itself, then this straight line is called
- (2) The sum of the measures of the accumulative angles at a point is
- (3) The ray drawn from the midpoint of a side of a triangle parallel to another side the third side.

(4) In the opposite figure :

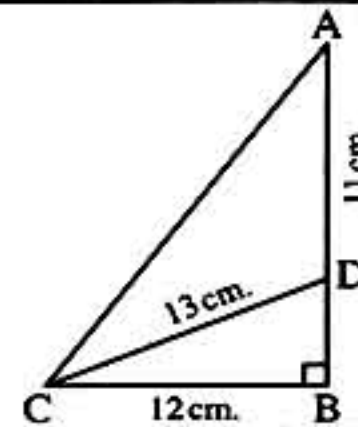
The value of $a = \dots\dots\dots$



3 In the opposite figure :

ABC is a triangle in which $m(\angle B) = 90^\circ$,
 $D \in \overline{AB}$, where $AD = 11 \text{ cm.}$, $BC = 12 \text{ cm.}$
 and $DC = 13 \text{ cm.}$

Find the length of : \overline{BD} and \overline{AC}



4 Draw on a lattice ΔABC , where $A(5, 1)$, $B(2, 1)$ and $C(5, 3)$, then draw its image by reflection in the origin point.

Worksheets on Geometry



The answer of worksheet

10

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

- | | | | |
|---------|-----|-----|-----|
| (1) (a) | (b) | (c) | (d) |
| (2) (a) | (b) | (c) | (d) |
| (3) (a) | (b) | (c) | (d) |
| (4) (a) | (b) | (c) | (d) |
| (5) (a) | (b) | (c) | (d) |
| (6) (a) | (b) | (c) | (d) |

3

2

- (1)
- (2)
- (3)
- (4)

2

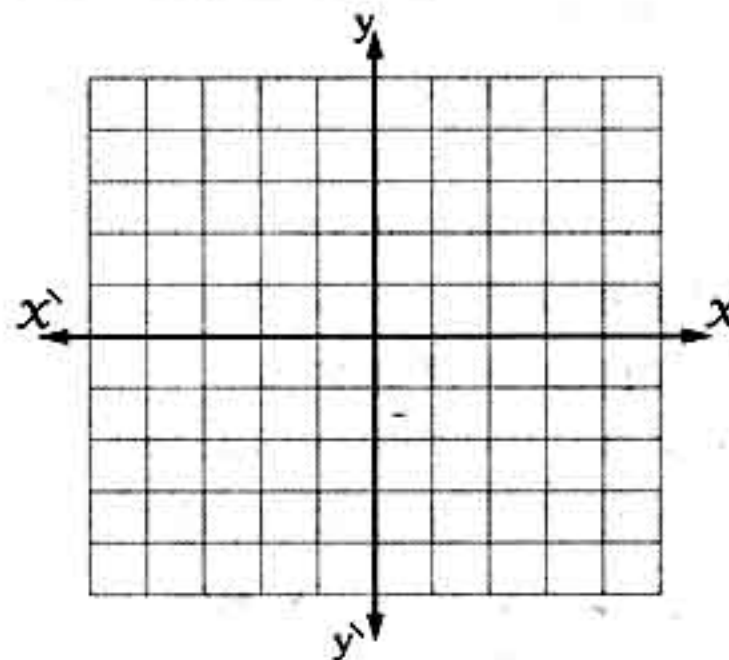
3

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5

4

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5



Worksheet 11 till lesson 11 unit 3

Answer the following questions :

1 Choose the correct answer from those given :

- (1) ABC is a triangle in which $m(\angle A) = 4x^\circ$, $m(\angle B) = 2x^\circ$ and $m(\angle C) = 3x^\circ$, then $\angle A$ is
- (a) acute. (b) right. (c) obtuse. (d) reflex.
- (2) The quadrilateral in which each two opposite sides are equal in length is
- (a) a parallelogram. (b) a trapezium. (c) a square. (d) a rectangle.
- (3) The image of the point $(-2, 3)$ by a translation of magnitude 5 units in the positive direction of the x -axis is
- (a) $(-2, -2)$ (b) $(-7, 3)$ (c) $(-2, 8)$ (d) $(3, 3)$
- (4) The image of the point $(0, 5)$ by reflection in the x -axis is
- (a) $(0, 5)$ (b) $(0, -5)$ (c) $(5, 0)$ (d) $(-5, 0)$
- (5) The image of the point $(x, -y)$ by reflection in the origin point is
- (a) (x, y) (b) $(-x, y)$ (c) $(x, -y)$ (d) $(-x, -y)$
- (6) If $A'(3, 5)$ is the image of the point A by the translation $(x, y) \rightarrow (x+4, y-2)$, then the point A is
- (a) $(7, 3)$ (b) $(7, 7)$ (c) $(-1, 7)$ (d) $(-1, 3)$

2 Complete the following :

- (1) If the measure of an exterior angle of a regular polygon = 30° , then the number of sides of the polygon =
- (2) The line segment which joins the two midpoints of the two sides of a triangle and
- (3) The translation keeps,
- (4) The translation is determined by two things, they are and

3 On lattice, draw $\triangle ABC$ where $A(-3, 2)$, $B(-1, 1)$ and $C(-2, 4)$ then draw its image.

- (1) by the translation $(x, y) \rightarrow (x+4, y-3)$
 (2) by reflection in x -axis.

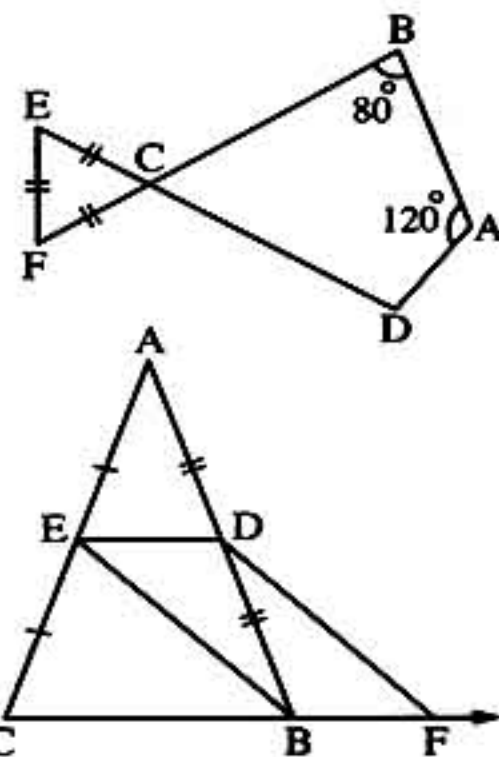
4 [a] In the opposite figure :

ABCD is a quadrilateral in which
 $m(\angle A) = 120^\circ$, $m(\angle B) = 80^\circ$
 $\triangle CEF$ is an equilateral
 Find by proof : $m(\angle D)$

[b] In the opposite figure :

D and E are the two midpoints
 of \overline{AB} and \overline{AC} respectively,
 $F \in \overline{CB}$ where $BF = \frac{1}{2} BC$

Prove that : the figure BEDF is a parallelogram.



Worksheets on Geometry



The answer of worksheet

11

Total
mark

15

1 Shade the circle that represents your choice for the correct answer :

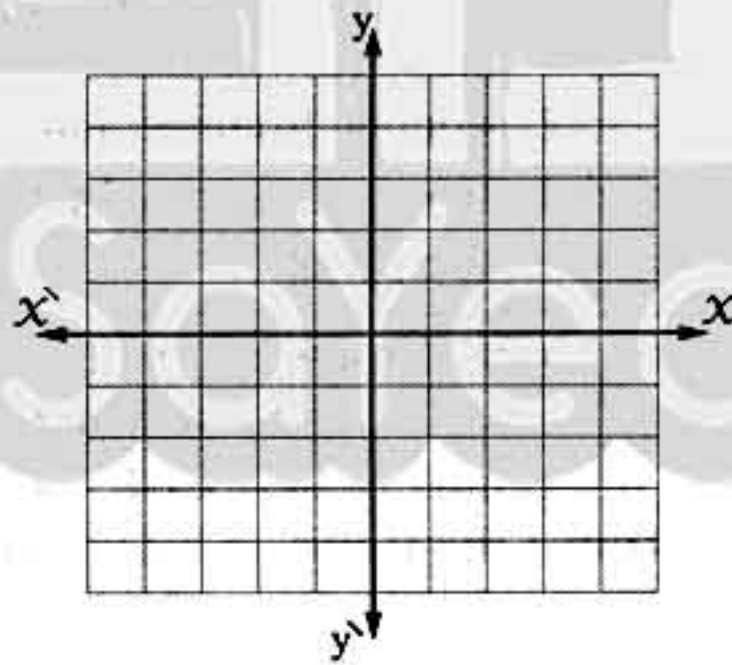
- | | | | | |
|---|-----|-----|-----|-----|
| ① | (a) | (b) | (c) | (d) |
| ② | (a) | (b) | (c) | (d) |
| ③ | (a) | (b) | (c) | (d) |
| ④ | (a) | (b) | (c) | (d) |
| ⑤ | (a) | (b) | (c) | (d) |
| ⑥ | (a) | (b) | (c) | (d) |

3

- 2
- ①
- ②
- ③
- ④

2

- 3
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-
-
-



5

- 4 [a]
-
-
- [b]
-
-

5